Package 'LARF'

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Type Package

Title Local Average Response Functions for Instrumental Variable
Estimation of Treatment Effects

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Description Provides instrumental variable estimation of treatment effects when both the endogenous treatment and its instrument are binary. Applicable to both binary and continuous outcomes.

Imports Formula

License GPL-3

NeedsCompilation no

Repository CRAN

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Contents

c401k	*c401k*

Description

Cross-sectional data with 9,275 observations including 11 variables on eligibility for and participation in 401(k) along with income and demographic information.

Usage

```
data(c401k)
```

Format

pira participation in IRA, participation = 1

nettfa net family financial assets in $1000

p401k participation in 401(k), participation = 1

e401k eligibility for 401(k), eligible = 1

inc income

incsq income square

marr marital status, married = 1

male sex, male = 1

age age

agesq age square

fsize family size

Details

An exemplary data to illustrate the usage of [larf](#). The data includes both a binary outcome (pira) and a continuous outcome (nettfa). The treatment is participation in 401k, p401k. Eligibility for 401(k), e401k, is used as an instrument for p401k.

Source

The Wooldridge Data Sets (Wooldridge 2010), originally entitled "401ksubs.dta" in Stata format, available at http://www.stata.com/texts/eacsap/.

References

Wooldridge, Jeffrey M. 2010. *Econometric Analysis of Cross Section and Panel Data*. 2nd Edition. MIT Press.

See Also

[larf](#), [larf.fit](#)

Examples

```
data(c401k)
```

---

cvlm	*Cross-validation of a Linear Regression Model*

Description

Provides cross-validation of a linear regression model

Usage

```
cvlm(form.lm, data, m=10, seed = NULL)
```

Arguments

form.lm	formula of the regression model.
data	data including outcome and covaraites.
m	the number of folds to be used in cross-validation.
seed	random starting number used to replicate cross-validation.

Details

This function finds the optimal order of the covariates power series through cross-validation.

Value

sumres	Sum of residual squares divided by degree of freedom.
df	Degree of freedom which equals to the number of valid predictions minus the number of parameters.
m	the number of folds to be used in cross-validation.
seed	The random seed.

Note

In making the code, we adopted part of the `CVlm` in `DAAG` (Maindonald and Braun, 2015).
<https://cran.r-project.org/package=DAAG>

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See Also

larf, npse

Generate.Powers   *Generating Powers Series of Variables*

Description

Internal function used by npse to generate covariates power series.

Usage

```
Generate.Powers(X, lambda)
```

Arguments

X	covariates.
lambda	the maximal order of power series.

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See Also

larf, npse

---

larf   *Local Average Response Functions for Instrumental Variable Estima-*
                                  tion of Treatment Effects

Description

The function provides instrumental variable estimation of treatment effects when both the endogenous treatment and its instrument are binary. Applicable to both binary and continuous outcomes.

Usage

```
larf(formula, treatment, instrument, data, method = "LS",
    AME = FALSE, optimizer = "Nelder-Mead", zProb = NULL)
```

Arguments

formula	specification of the outcome model in the form like either y ~ x1 + x2 or y ~ X where X is a matrix containing all the covariates excluding the treatment. Also support multi-part formulas (Zeileis and Croissant, 2010). For example, y + d ~ x1 + x2	z, where d represents the treatment and z the instrument.
treatment	A vector containing the binary treatment.
instrument	A vector containing the binary instrument for the endogenous treatment.
data	an optional data frame. If unspecified, the data will be taken from the working environment.
method	the estimation method to be used. The default is "LS", standing for least squares. "ML", standing for maximum likelihood, is an alternative.
AME	whether average marginal effects (AME) should be reported. The default is FALSE, in which case marginal effects at the means (MEM) are reported.
optimizer	the optimization algorithm for the ML method. It should be one of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", or "Brent". See optim in R for more detail.
zProb	a vector containing the probability of receiving the treatment inducement (i.e., instrument = 1) that have been estimated by semiparametrical methods.

Details

larf is the high-level interface to the work-horse function larf.fit. A set of standard methods (including print, summary, coef, vcov, fitted, resid, predict) can be used to extract the corresponding information from a larf object.

The function provides instrumental variable estimation of treatment effects when both the endogenous treatment and its instrument (i.e., the treatment inducement) are binary. The method (Abadie, 2003) involves two steps. First, pseudo-weights are constructed from the probability of receiving the treatment inducement. By default the function estimates the probability by a Probit regression. But it also allows users to employ the probability that has been estimated by semiparametric methods. Second, the pseudo-weights are used to estimate the local average response function of the outcome conditional on the treatment and covariates. The function provides both least squares and maximum likelihood estimates of the conditional treatment effects.

Value

coefficients	Estimated coefficients.
SE	Standard errors of the estimated coefficients.
MargEff	Estimated marginal effects, available only for binary outcomes.
MargStdErr	Standard errors of the estimated marginal effects, available only for binary outcomes.
vcov	Variance covariance matrix of the estimated coefficients.
fitted.values	Predicted outcomes based on the estimated model. They are probabilities when the outcome is binary.

Note

We derived part of the code from the Matlab code written by Professor Alberto Abadie, available at http://www.hks.harvard.edu/fs/aabadie/larf.html. We thank Onur Altindag and Behzad Kianian for helpful suggestions on improving the computation.

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References

Abadie, Alberto. 2003. "Semiparametric Instrumental Variable Estimation of Treatment Response Models." *Journal of Econometrics* 113: 231-263.
An, Weihua and Xuefu Wang. 2016. "LARF: Instrumental Variable Estimation of Causal Effects through Local Average Response Functions." *Journal of Statistical Software* 71(1): 1-13.
Zeileis, Achim and Yves Croissant. 2010. "Extended Model Formulas in R: Multiple Parts and Multiple Responses." *Journal of Statistical Software* 34(1): 1-13. http://www.jstatsoft.org/v34/i01/.

See Also

larf.fit, c401k

Examples

```
data(c401k)
attach(c401k)

## Not run:
# Continuous outcome. Treatment effects of participation in 401(k)
# on net family financial assest
est1 <- larf(nettfa ~ inc + age + agesq + marr + fsize, treatment = p401k,
instrument = e401k, data = c401k)
summary(est1)

# Nonparametric estimates of the probability of
# receiving the treatment inducement
library(mgcv)
firstStep <- gam(e401k ~ s(inc) + s(age) + s(agesq) + marr + s(fsize),
data=c401k, family=binomial(link = "probit"))
zProb <- firstStep$fitted
est2<- larf(nettfa ~ inc + age + agesq + marr + fsize, treatment = p401k,
instrument = e401k, data = c401k, zProb = zProb)
summary(est2)

# Binary outcome. Treatment effects of participation in 401(k)
# on participation in IRA
est3 <- larf(pira ~ inc + age + agesq + marr + fsize, treatment = p401k,
instrument = e401k, data = c401k)
summary(est3)
```

```
## End(Not run)
```

---

larf.fit   *Fitting the Local Average Response Function*

Description

It is the work-horse function for its high-level interface larf.

Usage

```
larf.fit(Y, X, D, Z, method, AME, optimizer, zProb)
```

Arguments

Y	a vector containing the outcome.
X	a matrix containing the covariates excluding the treatment.
D	a vector containing the binary treatment.
Z	a vector containing the binary instrument for the endogenous treatment.
method	the estimation method to be used. The default is "LS", standing for least squares. "ML", standing for maximum likelihood, is an alternative.
AME	whether average marginal effects (AME) should be reported. The default is FALSE, in which case marginal effects at the means (MEM) are reported.
optimizer	the optimization algorithm for the ML method. It should be one of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", or "Brent". See optim in R for more detail.
zProb	a vector containing the probability of receiving the treatment inducement (i.e., instrument = 1) that have been estimated by semiparametrical methods.

Author(s)

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See Also

larf, c401k

---

npse   *Nonparametric Power Series Estimation*

Description

Use the optimal order of power series of covariates to predict outcome. The optimal order of power series is determined by cross-validation.

Usage

```
npse(formula, order = 3, m = 10, seed = NULL)
```

Arguments

formula	specification of the outcome model in the form like either z ~ x1 + x2 or z ~ X where X is the covariate matrix.
order	the maximal order of power series to be used.
m	the number of folds to be used in cross-validation.
seed	random starting number used to replicate cross-validation.

Details

This function predicts the outcome based on the optimal order of covariates power series. The optimal order of the power series is determined by cross-validation. For example, it can be used to predict the probabilty of receiving treatment inducment based on covariates.

Value

fitted	Predicted outcomes based on the estimated model. They are probabilities when the outcome is binary.
Lambda	The optimal order of power series determined by cross-validation.
Data.opt	The data including z and the optimal covariates power series.
CV.Res	The residual sum of squares of the cross-validations.
seed	The random seed.

Author(s)

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References

Abadie, Alberto. 2003. "Semiparametric Instrumental Variable Estimation of Treatment Response Models." *Journal of Econometrics* 113: 231-263.

See Also

[larf](), [larf.fit]()

Examples

```
data(c401k)
attach(c401k)

## Not run:
# binary outcome
Z <- c401k$e401k

# covariates
X <- as.matrix(c401k[,c("inc", "male", "fsize"  )])

# get nonparametric power series estimation of the regression of Z on X
zp <- npse(Z~X, order = 5, m = 10, seed = 681)

# sum of residual squares of the cross-validations
zp$CV.Res

# the opitimal order of the power series
zp$Lambda

# summary of the predictions based on the optimal power series
summary(zp$fitted)

## End(Not run)
```

---

predict.larf   *Predictions Based on the Estimated LARF*

Description

Predict new outcomes based on the model fitted by [larf]().

Usage

```
## S3 method for class 'larf'
predict(object, newCov, newTreatment, ...)
```

Arguments

object	an object of class larf as fitted by [larf]().
newCov	A matrix containing the new covariates.
newTreatment	A vector containing the new binary treatment.
...	currently not used.

Details

Predicted outcomes are based on the estimated coefficients and new covariates and/or new treatment. The predicted outcomes are probabilities when the outcome is binary.

Value

predicted.values

The function returns a vector of the predicted outcomes.

Author(s)

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See Also

[larf](), [larf.fit]()

---

print.larf   *Print Results of the Estimated LARF*

Description

Methods to display brief results of a [larf]() object.

Usage

```
## S3 method for class 'larf'
print(x, digits = 4, ...)
```

Arguments

x	an object of class "larf" as fitted by [larf]().
digits	The number of significant digits to be printed in the reports of the results.
...	currently not used.

Author(s)

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See Also

[larf](), [larf.fit]()

---

summary.larf *Summary of the Estimated LARF*

Description

Summary of an object in the [larf](#) class.

Usage

```
## S3 method for class 'larf'
summary(object, ...)
```

Arguments

object   an object of class "larf" as fitted by [larf](#).

...   currently not used.

Author(s)

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See Also

[larf](#), [larf.fit](#)

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vcov.larf *Variance Covariance Matrix of the Parameters in the Estimated LARF*

Description

Methods to display the variance covariance matrix of the model parameters estimated by [larf](#).

Usage

```
## S3 method for class 'larf'
vcov(object, ...)
```

Arguments

object   an object of class "larf" as fitted by [larf](#).

...   currently not used.

Author(s)

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See Also

larf, larf.fit

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