

# Package ‘WaverideR’

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**Type** Package

**Title** Extracting Signals from Wavelet Spectra

**Version** 0.3.2

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**Depends** R (>= 3.5.0)

**Imports** DecomposeR, DescTools, Hmisc, Matrix,utils,colorednoise,  
doSNOW, fANCOVA,  
foreach,stats,tcltk,matrixStats,reshape2,truncnorm,grDevices,graphics,parallel,astrochron,biwavelet,WaveletComp,RColor

**Description** The continuous wavelet transform enables the observation of transient/non-stationary cyclicity in time-series. The goal of cyclostratigraphic studies is to define frequency/period in the depth/time domain. By conducting the continuous wavelet transform on cyclostratigraphic data series one can observe and extract cyclic signals/signatures from signals. These results can then be visualized and interpreted enabling one to identify/interpret cyclicity in the geological record, which can be used to construct astrochronological age-models and identify and interpret cyclicity in past and present climate systems. The 'WaverideR' R package builds upon existing literature and existing codebase. The list of articles which are relevant can be grouped in four subjects; cyclostratigraphic data analysis,example data sets,the (continuous) wavelet transform and astronomical solutions. References for the cyclostratigraphic data analysis articles are: Stephen Meyers (2019) <doi:10.1016/j.earscirev.2018.11.015>. Mingsong Li, Linda Hinnov, Lee Kump (2019) <doi:10.1016/j.cageo.2019.02.011> Stephen Meyers (2012)<doi:10.1029/2012PA002307> Mingsong Li, Lee R. Kump, Linda A. Hinnov, Michael E. Mann (2018) <doi:10.1016/j.epsl.2018.08.041>. Wouters, S., Crucifix, M., Sinnesael, M., Da Silva, A.C., Zeeden, C., Zivanovic, M., Boulvain, F., Devleeschouwer, X. (2022) <doi:10.1016/j.earscirev.2021.103894>. Wouters, S., Da Silva, A.-C., Boulvain, F., and Devleeschouwer, X. (2021) <doi:10.32614/RJ-2021-039>. Huang, Norden E., Zhaohua Wu, Steven R. Long, Kenneth C. Arnold, Xi-anyao Chen, and Karin Blank (2009) <doi:10.1142/S1793536909000096>. Cleveland, W. S. (1979)<doi:10.1080/01621459.1979.10481038> Hurvich, C.M., Simonoff, J.S., and Tsai, C.L. (1998) <doi:10.1111/1467-9868.00125>, Golub, G., Heath, M. and Wahba, G. (1979) <doi:10.2307/1268518>. References for the example data articles are: Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu (2018) <doi:10.1016/j.epsl.2018.02.010>. Steinhilber, Friedhelm, Abreu, Jacksiel, Beer, Juerg , Brunner, Irene, Christl, Marcus, Fischer, Huber-

tus, Heikkilä, U., Kubik, Peter, Mann, Mathias, McCracken, K., Miller, Heinrich, Miyahara, Hiroko, Oerter, Hans, Wilhelms, Frank. (2012 <doi:10.1073/pnas.1118965109>). Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert (2013) <doi:10.1016/j.palaeo.2012.11.009>. References for the (continuous) wavelet transform articles are: Morlet, Jean, Georges Arens, Eliane Fourgeau, and Dominique Glard (1982a) <doi:10.1190/1.1441328>. J. Morlet, G. Arens, E. Fourgeau, D. Girdard (1982b) <doi:10.1190/1.1441329>. Torrence, C., and G. P. Compo (1998) <https://paos.colorado.edu/research/wavelets/bams\_79\_01\_0061.pdf>, Gouhier TC, Grinsted A, Simko V (2021) <https://github.com/tgouhier/biwavelet>. Angi Roesch and Harald Schmidbauer (2018) <https://CRAN.R-project.org/package=WaveletComp>. Russell, Brian, and Jiajun Han (2016) <https://www.crewes.org/Documents/ResearchReports/2016/CRR201668.pdf>. Gabor, Dennis (1946) <http://genesis.eecg.toronto.edu/gabor1946.pdf>. J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Lestrade, B. (2004) <doi:10.1051/0004-6361:20041335>. Laskar, J., Fienga, A., Gastineau, M., Manche, H. (2011a) <doi:10.1051/0004-6361/201116836>. References for the astronomical solutions articles are: Laskar, J., Gastineau, M., Delisle, J.-B., Farres, A., Fienga, A. (2011b) <doi:10.1051/0004-6361/201117504>. J. Laskar (2019) <doi:10.1016/B978-0-12-824360-2.00004-8>. Zeebe, Richard E (2017) <doi:10.3847/1538-3881/aa8cce>. Zeebe, R. E. and Lourens, L. J. (2019) <doi:10.1016/j.epsl.2022.117595>. Richard E. Zeebe Lucas J. Lourens (2022) <doi:10.1126/science.aax0612>.

**License** GPL (>= 2)

**URL** <https://github.com/stratigraphy/WaveriderR>

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.3

**NeedsCompilation** no

**Repository** CRAN

**Suggests** testthat (>= 3.0.0)

**Config/testthat/edition** 3

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add_wavelet	<i>Add a wavelet plot</i>
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## Description

Generates a plot of a wavelet scalogram which can be integrated into a larger composite plot

## Usage

```
add_wavelet(
  wavelet = NULL,
  lowerPeriod = NULL,
  upperPeriod = NULL,
  lower_depth_time = NULL,
  upper_depth_time = NULL,
  n.levels = 100,
  plot.COI = TRUE,
  color_brewer = "grDevices",
  palette_name = "rainbow",
  plot_dir = FALSE,
  add_lines = NULL,
  add_points = NULL,
  add_abline_h = NULL,
  add_abline_v = NULL,
  plot_horizontal = TRUE,
  period_ticks = 1,
  periodlab = "period (m)",
  main = NULL,
  yaxt = "s",
  xaxt = "s",
  depth_time_lab = "depth (m)"
)
```

## Arguments

wavelet	wavelet object created using the <a href="#">analyze_wavelet</a> function.
lowerPeriod	Lowest period value which will be plotted
upperPeriod	Highest period value which will be plotted

lower_depth_time	lowest depth/time value which will be plotted
upper_depth_time	Highest depth/time value which will be plotted
n.levels	Number of color levels Default=100.
plot.COI	Option to plot the cone of influence Default=TRUE.
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
plot_dir	The direction of the proxy record which is assumed for tuning if time increases with increasing depth/time values (e.g. bore hole data which gets older with increasing depth ) then plot_dir should be set to TRUE if time decreases with depth/time values (eg stratospheric logs where 0m is the bottom of the section) then plot_dir should be set to FALSE plot_dir=TRUE
add_lines	Add lines to the wavelet plot input should be matrix with first axis being depth/time the columns after that should be period values Default=NULL
add_points	Add points to the wavelet plot input should be matrix with first axis being depth/time and columns after that should be period values Default=NULL
add_abline_h	Add horizontal lines to the plot. Specify the lines as a vector e.g. c(2,3,5,6) Default=NULL
add_abline_v	Add vertical lines to the plot. Specify the lines as a vector e.g. c(2,3,5,6) Default=NULL
plot_horizontal	plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default=TRUE
period_ticks	tick mark spacing 1 is all tickmarks and higher value removes tick marks by the fraction of the tick mark spacing value, the opposite is true for value lower than 1 which will add additional tickmarks
periodlab	lable for the the period column
main	main title

yaxt                    turn on of off the yaxis "s" is on "n" is off Default="s"  
 xaxt                    turn on of off the xaxis "s" is on "n" is off Default="s"  
 depth\_time\_lab    lable for the the depth/time column

### Value

returns a plot of a wavelet scalogram

### Author(s)

Code based on the [analyze.wavelet](#) and [wt.image](#) functions of the 'WaveletComp' R package and [wt](#) function of the 'biwavelet' R package which are based on the wavelet MATLAB code written by Christopher Torrence and Gibert P. Compo (1998). The MTM analysis is from the astrochron R package of Meyers et al., (2012)

### References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)
- Morlet, Jean, Georges Arens, Eliane Fourgeau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " Geophysics 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>
- J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. Geophysics 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

### Examples

```
#generate a plot for the magnetic susceptibility data set of Pas et al., (2018)

plot.new()
layout.matrix <- matrix(c(rep(0, 2), 1, 0,0,seq(2, 6, by = 1)),
                        nrow = 2,
                        ncol = 5 ,
                        byrow = TRUE)
graphics::layout(mat = layout.matrix,
                 heights = c(0.25, 1),
                 # Heights of the two rows
                 widths = c(rep(c(1, 2, 4,2,2), 2)))

par(mar = c(0, 0.5, 1, 0.5))
```

```
mag_wt <-
  analyze_wavelet(
    data = mag,
    dj = 1 / 100,
    lowerPeriod = 0.1,
    upperPeriod = 254,
    verbose = FALSE,
    omega_nr = 10
  )

add_wavelet_avg(
  wavelet = mag_wt,
  plot_horizontal = TRUE,
  add_abline_h = NULL,
  add_abline_v = NULL,
  lowerPeriod = 0.15,
  upperPeriod = 80
)

par(mar = c(4, 4, 0, 0.5))

plot(
  x = c(0, 1),
  y = c(max(mag[, 1]), min(mag[, 1])),
  col = "white",
  xlab = "",
  ylab = "Time (Ma)",
  xaxt = "n",
  xaxs = "i",
  yaxs = "i",
  ylim = rev(c(max(mag[, 1]), min(mag[, 1])))
) # Draw empty plot

polygon(
  x = c(0, 1, 1, 0),
  y = c(max(mag[, 1]), max(mag[, 1]), min(mag[, 1]), min(mag[, 1])),
  col = geo_col("Famennian")
)

text(
  0.5,
  (max(mag[, 1]) - min(mag[, 1])) / 2,
  "Fammenian",
  cex = 1,
  col = "black",
  srt = 90
)

par(mar = c(4, 0.5, 0, 0.5))

plot(
```

```

mag[, 2],
mag[, 1],
type = "l",
ylim = rev(c(max(mag[, 1]), min(mag[, 1]))),
yaxs = "i",
yaxt = "n",
xlab = "Mag. suc.",
ylab = ""
)

```

```

add_wavelet(
  wavelet = mag_wt,
  lowerPeriod = 0.15,
  upperPeriod = 80,
  lower_depth_time = NULL,
  upper_depth_time = NULL,
  n.levels = 100,
  plot.COI = TRUE,
  color_brewer = "grDevices",
  palette_name = "rainbow",
  plot_dir = FALSE,
  add_lines = NULL,
  add_points = NULL,
  add_abline_h = NULL,
  add_abline_v = NULL,
  plot_horizontal = TRUE,
  period_ticks = 1,
  periodlab = "period (m)",
  main = NULL,
  yaxt = "n",
  xaxt = "s",
  depth_time_lab = ""
)

```

```

lines(log2(mag_track_solution[,2]),mag_track_solution[,1],lwd=4,lty=4)

```

```

mag_405 <- extract_signal(
  tracked_cycle_curve = mag_track_solution,
  wavelet = mag_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  tracked_cycle_period = 405,
  extract_cycle = 405,
  tune = FALSE,
  plot_residual = FALSE
)

```

```

plot(mag_405[,2],mag_405[,1],type="l",
      yaxt="n", yaxs = "i",
      xlab="405-kyr ecc")

```



```

mag_110 <- extract_signal(
  tracked_cycle_curve = mag_track_solution,
  wavelet = mag_wt,
  period_up = 1.25,
  period_down = 0.75,
  add_mean = TRUE,
  tracked_cycle_period = 405,
  extract_cycle = 110,
  tune = FALSE,
  plot_residual = FALSE
)

mag_110_hil <- Hilbert_transform(mag_110,demean=FALSE)

plot(mag_110[,2],mag_110[,1],type="l",
     yaxt="n", yaxs = "i",
     xlab="110-kyr ecc")

lines(mag_110_hil[,2],mag_110_hil[,1])

```

---

add_wavelet_avg	<i>Add a plot of a the average spectral power of a continous wavelet transform</i>
-----------------	--

---

### Description

Generates a plot of a the average spectral power of a continous wavelet transform which can be added to a larger composite plot

### Usage

```

add_wavelet_avg(
  wavelet = NULL,
  plot_horizontal = TRUE,
  add_abline_h = NULL,
  add_abline_v = NULL,
  lowerPeriod = NULL,
  upperPeriod = NULL
)

```

### Arguments

wavelet	wavelet object created using the <a href="#">analyze_wavelet</a> function.
plot_horizontal	plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default=TRUE

add_abline_h	Add horizontal lines to the plot. Specify the lines as a vector e.g. <code>c(2,3,5,6)</code> Default=NULL
add_abline_v	Add vertical lines to the plot. Specify the lines as a vector e.g. <code>c(2,3,5,6)</code> Default=NULL
lowerPeriod	Lowest period value which will be plotted
upperPeriod	Highest period value which will be plotted

### Value

returns a plot of a the average spectral power of a continuous wavelet transform

### Author(s)

Code based on the [analyze.wavelet](#) and [wt.image](#) functions of the 'WaveletComp' R package and [wt](#) function of the 'biwavelet' R package which are based on the wavelet MATLAB code written by Christopher Torrence and Gilbert P. Compo (1998). The MTM analysis is from the astrochron R package of Meyers et al., (2012)

### References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)
- Morlet, Jean, Georges Arens, Eliane Fourageau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " *Geophysics* 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>
- J. Morlet, G. Arens, E. Fourageau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. *Geophysics* 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

### Examples

#generate a plot for the magnetic susceptibility data set of Pas et al., (2018)

```
plot.new()
layout.matrix <- matrix(c(rep(0, 2), 1, 0,0,seq(2, 6, by = 1)),
                        nrow = 2,
                        ncol = 5 ,
                        byrow = TRUE)
graphics::layout(mat = layout.matrix,
                 heights = c(0.25, 1),
                 # Heights of the two rows
                 widths = c(rep(c(1, 2, 4,2,2), 2)))
```

```
par(mar = c(0, 0.5, 1, 0.5))

mag_wt <-
  analyze_wavelet(
    data = mag,
    dj = 1 / 100,
    lowerPeriod = 0.1,
    upperPeriod = 254,
    verbose = FALSE,
    omega_nr = 10
  )

add_wavelet_avg(
  wavelet = mag_wt,
  plot_horizontal = TRUE,
  add_abline_h = NULL,
  add_abline_v = NULL,
  lowerPeriod = 0.15,
  upperPeriod = 80
)

par(mar = c(4, 4, 0, 0.5))

plot(
  x = c(0, 1),
  y = c(max(mag[, 1]), min(mag[, 1])),
  col = "white",
  xlab = "",
  ylab = "Time (Ma)",
  xaxt = "n",
  xaxs = "i",
  yaxs = "i",
  ylim = rev(c(max(mag[, 1]), min(mag[, 1])))
) # Draw empty plot

polygon(
  x = c(0, 1, 1, 0),
  y = c(max(mag[, 1]), max(mag[, 1]), min(mag[, 1]), min(mag[, 1])),
  col = geo_col("Famennian")
)

text(
  0.5,
  (max(mag[, 1]) - min(mag[, 1])) / 2,
  "Fammenian",
  cex = 1,
  col = "black",
  srt = 90
)
```

```
)  
par(mar = c(4, 0.5, 0, 0.5))  
  
plot(  
  mag[, 2],  
  mag[, 1],  
  type = "l",  
  ylim = rev(c(max(mag[, 1]), min(mag[, 1]))),  
  yaxs = "i",  
  yaxt = "n",  
  xlab = "Mag. suc.",  
  ylab = ""  
)  
  
add_wavelet(  
  wavelet = mag_wt,  
  lowerPeriod = 0.15,  
  upperPeriod = 80,  
  lower_depth_time = NULL,  
  upper_depth_time = NULL,  
  n.levels = 100,  
  plot.COI = TRUE,  
  color_brewer = "grDevices",  
  palette_name = "rainbow",  
  plot_dir = FALSE,  
  add_lines = NULL,  
  add_points = NULL,  
  add_abline_h = NULL,  
  add_abline_v = NULL,  
  plot_horizontal = TRUE,  
  period_ticks = 1,  
  periodlab = "period (m)",  
  main = NULL,  
  yaxt = "n",  
  xaxt = "s",  
  depth_time_lab = ""  
)  
  
lines(log2(mag_track_solution[,2]),mag_track_solution[,1],lwd=4,lty=4)  
  
mag_405 <- extract_signal(  
  tracked_cycle_curve = mag_track_solution,  
  wavelet = mag_wt,  
  period_up = 1.2,  
  period_down = 0.8,  
  add_mean = TRUE,  
  tracked_cycle_period = 405,  
  extract_cycle = 405,  
  tune = FALSE,  
  plot_residual = FALSE  
)
```

```

plot(mag_405[,2],mag_405[,1],type="l",
     yaxt="n", yaxs = "i",
     xlab="405-kyr ecc")

mag_110 <- extract_signal(
  tracked_cycle_curve = mag_track_solution,
  wavelet = mag_wt,
  period_up = 1.25,
  period_down = 0.75,
  add_mean = TRUE,
  tracked_cycle_period = 405,
  extract_cycle = 110,
  tune = FALSE,
  plot_residual = FALSE
)

mag_110_hil <- Hilbert_transform(mag_110,demean=FALSE)

plot(mag_110[,2],mag_110[,1],type="l",
     yaxt="n", yaxs = "i",
     xlab="110-kyr ecc")

lines(mag_110_hil[,2],mag_110_hil[,1])

```

---

age_model_zeeden	<i>Age model of Zeeden et al., (2013) for the (154-174m) interval of the IODP 926 grey scale record</i>
------------------	---

---

### Description

Age model (anchor points) of the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013) Anchored to the eccentricity-tilt-precession model p-0.5t of la 2004.

### Details

Column 1: Depth (meters)  
 Column 2: Age (kyr)

### References

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369,2013,Pages 430-451,ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: *Astron. Astrophys.*, Volume 428, 261-285. <doi:10.1051/0004-6361:20041335>

---

analyze_wavelet	<i>Conduct the continuous wavelet transform on a time series/signal</i>
-----------------	---

---

### Description

Compute the continuous wavelet transform (CWT) using a Morlet wavelet

### Usage

```
analyze_wavelet(
  data = NULL,
  dj = 1/20,
  lowerPeriod = 2,
  upperPeriod = 1024,
  verbose = FALSE,
  omega_nr = 6
)
```

### Arguments

data	Input data, should be a matrix or data frame in which the first column is depth or time and the second column is proxy record.
dj	Spacing between successive scales. The CWT analyses analyses the signal using successive periods which increase by the power of 2 (e.g. $2^0=1, 2^1=2, 2^2=4, 2^3=8, 2^4=16$ ). To have more resolution in-between these steps the dj parameter exists, the dj parameter specifies how many extra steps/spacing in-between the power of 2 scaled CWT is added. The amount of steps is $1/x$ with a higher x indicating a smaller spacing. Increasing the increases the computational time of the CWT Default=1/200.
lowerPeriod	Lowest period to be analyzed Default=2. The CWT analyses the signal starting from the lowerPeriod to the upperPeriod so the proper selection these parameters allows to analyze the signal for a specific range of cycles. scaling is done using power 2 so for the best plotting results select a value to the power or 2.
upperPeriod	Upper period to be analyzed Default=1024. The CWT analyses the signal starting from the lowerPeriod to the upperPeriod so the proper selection these parameters allows to analyze the signal for a specific range of cycles. scaling is done using power 2 so for the best plotting results select a value to the power or 2.
verbose	Print text Default=FALSE.
omega_nr	Number of cycles contained within the Morlet wavelet

### Value

The output is a list (wavelet object) which contain 18 objects which are the result of the continuous wavelet transform (CWT). Object 1: Wave - Wave values of the wavelet Object 2: Phase - Phase of the wavelet Object 3: Ampl - Amplitude values of the wavelet Object 4: Power - Power values of the wavelet Object 5: dt - Step size Object 6: dj - Scale size Object 7: Power.avg - Average power

values Object 8: Period - Period values Object 9: Scale - Scale value Object 10: coi.1 - Cone of influence values 1 Object 11: coi.2 - Cone of influence values 2 Object 12: nc - Number of columns Object 13: nr - Number of rows Object 14: axis.1 - axis values 1 Object 15: axis.2 - axis values 2 Object 16: omega\_nr - Number of cycles in the wavelet Object 17: x - x values of the data set Object 18: y - y values of the data set

### Author(s)

Code based on on the [analyze\\_wavelet](#) function of the 'WaveletComp' R package and [wt](#) function of the 'biwavelet' R package which are based on the wavelet MATLAB code written by Christopher Torrence and Gilbert P. Compo.

### References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)
- Morlet, Jean, Georges Arens, Eliane Fourgeau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " Geophysics 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>
- J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. Geophysics 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

### Examples

```
#Example 1. Using the Total Solar Irradiance data set of Steinhilber et al., (2012)
TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = FALSE,
    omega_nr = 6
  )
```

```
#Example 2. Using the magnetic susceptibility data set of Pas et al., (2018)
mag_wt <-
  analyze_wavelet(
    data = mag,
    dj = 1/100,
    lowerPeriod = 0.1,
```

```

upperPeriod = 254,
verbose = FALSE,
omega_nr = 10
)

#Example 3. Using the greyscale data set of Zeeden et al., (2013)
grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )

```

---

anchor2time

*Convert a proxy record to the time domain using anchor points*

---

### Description

Convert a proxy record to the time domain using anchor points made using the [astro\\_anchor](#) function.

### Usage

```

anchor2time(
  anchor_points = NULL,
  data = NULL,
  genplot = FALSE,
  keep_editable = FALSE
)

```

### Arguments

anchor_points	Anchor points made using the <a href="#">astro_anchor</a> function or a matrix in which the first column is depth and the second column is time.
data	Data set which needs to be converted from the depth to time domain using set anchor points. The data set should consist of a matrix with 2 column the first column should be depth and the second column should be a proxy value.
genplot	If genplot=FALSE then 3 plots stacked on top of each other will be plotted. Plot 1: the original data set Plot 2: the depth time plot Plot 3: the data set in the time domain set to TRUE to allow for anchoring using the GUI
keep_editable	Keep option to add extra features after plotting Default=FALSE



**Value**

The output is a matrix with 2 columns. The first column is time. The second column sedimentation proxy value.

If `genplot=TRUE` then 3 plots stacked on top of each other will be plotted. Plot 1: the original data set. Plot 2: the depth time plot. Plot 3: the data set in the time domain.

**Examples**

```
# Use the age_model_zeeden example anchor points of Zeeden et al., (2013)
#to anchor the grey data set of Zeeden et al., (2013) in the time domain.
```

```
anchored2time <- anchor2time(anchor_points=age_model_zeeden,
data=grey,
genplot=FALSE,
keep_editable=FALSE)
```

---

anchor\_points\_Bisciaro\_al

*XRF records of the Bisciaro Fm*

---

**Description**

data set consist of the tie points between the Bisciaro\_al record of Arts (2014) and the la2011 solution of laskar et al., (2011)

**Details**

The data set is a matrix with the 4 columns. The first column is the depth/time of the al proxy record tie-points. The second column is the time value of the la2011 astronomical solution tie-points. The third column is the AI value of the a; tie-point. The fourth column is the eccentricity value of the la2011 astronomical solution tie-point.

**References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

Laskar, J., M. Gastineau, J. B. Delisle, A. Farrés, and A. Fienga (2011b), Strong chaos induced by close encounters with Ceres and Vesta, *Astron. Astrophys.*, 532, L4,<doi:10.1051/0004-6361/201117504>

---

anchor\_points\_grey     *Example anchor points for the grey scale data set of Zeeden et al., (2013)*

---

### Description

An example of anchor points generated using [astro\\_anchor](#) function  
The anchor points were generated for the [grey](#) grey data set of Zeeden et al., (2013) and anchored to the [codeastrosignal\\_example](#) astronomical solution which is a pre-generated ETP (eccentricity-tilt-precession) solution(p-0.5t based on the la2004 solution) based on Laskar et al., (20004) astronomical solution.

### Details

Column 1: depth proxy record  
Column 2: time astronomical solution  
Column 3: y-scale value proxy record  
Column 4: y-scale value astronomical solution

### References

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, Palaeogeography, Palaeoclimatology, Palaeoecology, Volume 369,2013,Pages 430-451,ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: Astron. Astrophys., Volume 428, 261-285. <doi:10.1051/0004-6361:20041335>

---

astrosignal\_example     *An ETP astronomical solution*

---

### Description

The [astrosignal\\_example](#) is a pre-generated ETP (eccentricity-tilt-precession) (p-0.5t based on the la2004 solution) the [astrosignal\\_example](#) can be used to anchor the [grey](#) data set to an astronomical solution eg. [astrosignal\\_example](#) using the [astro\\_anchor](#) function. the data set was generated using the [etp](#) function of the 'astrochron' R package. The pre-generated ETP spans 5000 to 6000kyr.

## Details

Column 1: time (kyr)

Column 2: ETP

## Author(s)

Generated using the [etp](#) function of the [astrochron-package](#).

## References

Stephen R. Meyers, Cyclostratigraphy and the problem of astrochronologic testing, Earth-Science Reviews, Volume 190, 2019, Pages 190-223, ISSN 0012-8252 <doi:10.1016/j.earscirev.2018.11.015>

J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: Astron. Astrophys., Volume 428, 261-285. <doi:10.1051/0004-6361:20041335>

---

astro\_anchor

*Anchor proxy record to an astronomical solution*

---

## Description

Anchor the extracted signal to an astronomical solution using a GUI. The [astro\\_anchor](#) function allows one to tie minima or maxima in the proxy record to minima or maxima in an astronomical solution. By tying the proxy record to an astronomical solution one will generate tie-points which can be used to generate an astrochronological age-model. As minima or maxima in the proxy record are tied to minima or maxima in an astronomical solution it is important to provide input which has clearly definable minima and maxima. As such input should be of a "sinusoidal" nature otherwise the `extract_astrosolution=TRUE` and/or `extract_proxy_signal=TRUE` options need to be set to `TRUE` to create sinusoidal signals.

Astronomical solutions option are:

- La2004 Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2004 Obliquity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2004 Precession solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Obliquity solution downloadable via the <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>

- La2010b Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010b Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010b Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2011 Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- ZB17a Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17a Obliquity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17b Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17b Obliquity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17c Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17c Obliquity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17d Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17d Obliquity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17e Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17e Obliquity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)
- ZB17f Eccentricity solution downloadable via [https://www.soest.hawaii.edu/oceanography/faculty/zeebe\\_files/Astro.html](https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html)



- 405kyr eccentricity 405 metronome can be generated using the formula:  
 $e_{405} = 0.027558 - 0.010739 \cdot \cos(0.0118 + 2(\pi) \cdot (t/405000))$  (laskar et al., 2004 & laskar 2020)
- 173kyr obliquity metronome can be generated using using the formula:  
 $es3-s6(t) = 0.144 \cdot \cos(1.961 + 2(\pi) \cdot (t/172800))$  (laskar et al., 2004 & laskar 2020)
- An etp model using the `etp` function of the 'astrochron' R package

## Usage

```
astro_anchor(
  astro_solution = NULL,
  proxy_signal = NULL,
  proxy_min_or_max = "max",
  clip_astrosolution = FALSE,
  astrosolution_min_or_max = "max",
  clip_high = NULL,
  clip_low = NULL,
  extract_astrosolution = FALSE,
  astro_period_up = 1.2,
  astro_period_down = 0.8,
  astro_period_cycle = NULL,
  extract_proxy_signal = FALSE,
  proxy_period_up = 1.2,
  proxy_period_down = 0.8,
  proxy_period_cycle = NULL,
  pts = 3,
  verbose = FALSE,
  time_dir = TRUE,
  genplot = FALSE
)
```

## Arguments

- `astro_solution` Input is an astronomical solution which the proxy record will be anchored to, the input should be a matrix or data frame with the first column being age and the second column should be a insolation/angle/value
- `proxy_signal` Input is the proxy data set which will be anchored to an astronomical solution, the input should be a matrix or data frame with the first column being depth/time and the second column should be a proxy value. For the best results either the astronomical components need to be pre-extracted before anchoring. This means that a filtering/cycle extracting need to be applied to the input data or the `extract_proxy_signal` option needs to be set to TRUE.
- `proxy_min_or_max` Tune proxy maxima or minima to the astronomical solution Default="max".
- `clip_astrosolution` Clip the astronomical solution Default=FALSE.
- `astrosolution_min_or_max` Tune to maximum or minimum values of the astronomical solution Default="max"

clip_high	Upper value to clip to.
clip_low	Lower value to clip to.
extract_astrosolution	Extract a certain astronomical cycle/component from a astronomical solution prior to anchoring Default=FALSE.
astro_period_up	Specifies the upper period of the astronomical cycle which is extracted from an astronomical solution. The astro_period_up is a factor with which the astronomical component is multiplied by. Default=1.2
astro_period_down	Specified the lower period of the astronomical cycle which is extracted from an astronomical solution. The astro_period_down value is a factor with which the astronomical component is multiplied by. Default=0.8
astro_period_cycle	Period (in kyr) of the to be extracted astronomical component from the astronomical solution.
extract_proxy_signal	Extract a certain astronomical cycle/component from a proxy signal Default=FALSE.
proxy_period_up	Specifies the upper period of the astronomical cycle to be extracted from the proxy record. The upper bound value is a factor with which the (proxy_period_cycle) value is multiplied by. Default=1.2.
proxy_period_down	Specifies the upper period of the astronomical cycle to be extracted from the proxy record. The lower bound value is a factor with which the astronomical component (proxy_period_cycle) value is multiplied by. Default=0.8.
proxy_period_cycle	Period in kyr of the astronomical cycle/component which is to be extracted from the proxy record.
pts	The pts parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the pts parameter can be changed which can aid in peak detection. Usually increasing the pts parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=3
verbose	print text Default=FALSE set verbose to TRUE to allow for anchoring using text feedback commands
time_dir	The direction of the proxy record which is assumed for tuning if time increases with increasing depth/time values (e.g. bore hole data which gets older with increasing depth ) then time_dir should be set to TRUE if time decreases with depth/time values (eg stratigraphic logs where 0m is the bottom of the section) then time_dir should be set to FALSE time_dir=TRUE
genplot	Generate plot Default="FALSE"

**Value**

The output is a matrix with the 4 columns. The first column is the depth/time of the proxy tie-point. The second column is the time value of the astronomical solution tie-point. The third column is the proxy value of the proxy tie-point. The fourth column is the proxy/insolation value of the astronomical solution tie-point. If `genplot` is set to true then a plot of the anchored points will be plotted

**References**

J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: *Astron. Astrophys.*, Volume 428, 261-285. <doi:10.1051/0004-6361:20041335>

Laskar, J., Fienga, A., Gastineau, M., Manche, H., 2011a, La2010: A new orbital solution for the long-term motion of the Earth: *Astron. Astrophys.*, Volume 532, A89 <doi:10.1051/0004-6361/201116836>

Laskar, J., Gastineau, M., Delisle, J.-B., Farres, A., Fienga, A.: 2011b, Strong chaos induced by close encounters with Ceres and Vesta, *Astron: Astrophys.*, Volume 532, L4. <doi:10.1051/0004-6361/201117504>

J. Laskar, Chapter 4 - Astrochronology, Editor(s): Felix M. Gradstein, James G. Ogg, Mark D. Schmitz, Gabi M. Ogg, *Geologic Time Scale 2020*, Elsevier, 2020, Pages 139-158, ISBN 9780128243602, <doi:10.1016/B978-0-12-824360-2.00004-8> or <https://www.sciencedirect.com/science/article/pii/B978012824360200048>

Zeebe, R. E. and Lourens, L. J. Geologically constrained astronomical solutions for the Cenozoic era, *Earth and Planetary Science Letters*, 2022 <doi:10.1016/j.epsl.2022.117595>

Richard E. Zeebe Lucas J. Lourens ,Solar System chaos and the Paleocene–Eocene boundary age constrained by geology and astronomy. *Science* 365, 926-929 (2019) <doi:10.1126/science.aax0612>

Zeebe, Richard E. "Numerical solutions for the orbital motion of the Solar System over the past 100 Myr: limits and new results." *The Astronomical Journal* 154, no. 5 (2017): 193. <doi:10.3847/1538-3881/aa8cce>

Stephen R. Meyers, Cyclostratigraphy and the problem of astrochronologic testing, *Earth-Science Reviews*, Volume 190, 2019, Pages 190-223, ISSN 0012-8252 <doi:10.1016/j.earscirev.2018.11.015>

**Examples**

```
# Use the grey_track example tracking points to anchor the grey scale data set
# of Zeeden et al., (2013) to the p-0.5t la2004 solution

grey_wt <-
  analyze_wavelet(
    data = grey,
```



```
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )
#Use the pre-tracked grey_track curve which traced the precession cycle
grey_track <- completed_series(
  wavelet = grey_wt,
  tracked_curve = grey_track,
  period_up = 1.25,
  period_down = 0.75,
  extrapolate = TRUE,
  genplot = FALSE
)
# Extract precession, obliquity and eccentricity to create a synthetic insolation curve

grey_prec <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 22,
  tune = FALSE,
  plot_residual = FALSE
)

grey_obl <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 110,
  tune = FALSE,
  plot_residual = FALSE
)

grey_ecc <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.25,
  period_down = 0.75,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 40.8,
  tune = FALSE,
  plot_residual = FALSE
)
```

```

insolation_extract <- cbind(grey_ecc[,1],grey_prec[,2]+grey_obl[,2]+grey_ecc[,2]+mean(grey[,2]))
insolation_extract <- as.data.frame(insolation_extract)
insolation_extract_mins <- min_detect(insolation_extract,pts=3)

#use the astrosignal_example to tune to which is an \cr
# ETP solution (p-0.5t la2004 solution)
astrosignal_example <- na.omit(astrosignal_example)
astrosignal_example[,2] <- -1*astrosignal_example[,2]
astrosignal <- as.data.frame(astrosignal_example)

#anchor the synthetic insolation curve extracted from the grey scale record to the insolation curve.

anchor_pts <- astro_anchor(
  astro_solution = astrosignal,
  proxy_signal = insolation_extract,
  proxy_min_or_max = "min",
  clip_astrosolution = FALSE,
  astrosolution_min_or_max = "min",
  clip_high = NULL,
  clip_low = NULL,
  extract_astrosolution = FALSE,
  astro_period_up = NULL,
  astro_period_down = NULL,
  astro_period_cycle = NULL,
  extract_proxy_signal = FALSE,
  proxy_period_up = NULL,
  proxy_period_down = NULL,
  proxy_period_cycle = NULL,
  pts=3,
  verbose=FALSE, #set verbose to TRUE to allow for anchoring using text feedback commands
  genplot=FALSE
)

```

---

Bisciaro\_al\_wt\_track *Period of the short kyr ecc cycle in the Al record of the Bisciaro Fm*

---

### Description

Data points which give the period (in meters) of the short kyr eccentricity cycle tracked in the wavelet scalogram of the aluminium (XRF) record of the Bisciaro Formation  
 The period was tracked using the [track\\_period\\_wavelet](#) function  
 The tracking is based on a reinterpretation of Arts (2014)

### Details

Column 1: depth proxy record  
 Column 2: period tracked in the wavelet scalogram of the Aluminium (XRF) record

**References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

---

Bisciaro\_ca\_wt\_track *Period of the short kyr ecc cycle in the Ca record of the Bisciaro Fm*

---

**Description**

Data points which give the period (in meters) of the short kyr eccentricity cycle tracked in the wavelet scalogram of the calcium (XRF) record of the Bisciaro Formation  
The period was tracked using the [track\\_period\\_wavelet](#) function  
The tracking is based on a reinterpretation of Arts (2014)

**Details**

Column 1: depth proxy record  
Column 2: period tracked in the wavelet scalogram of the calcium (XRF) record

**References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

---

Bisciaro\_Mg\_wt\_track *Period of the short kyr ecc cycle in the Mg record of the Bisciaro Fm*

---

**Description**

Data points which give the period (in meters) of the short kyr eccentricity cycle tracked in the wavelet scalogram of the magnesium (XRF) record of the Bisciaro Formation  
The period was tracked using the [track\\_period\\_wavelet](#) function  
The tracking is based on a reinterpretation of Arts (2014)

**Details**

Column 1: depth proxy record  
Column 2: period tracked in the wavelet scalogram of the Magnesium (XRF) record

**References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

---

Bisciaro\_Mn\_wt\_track    *Period of the short kyr ecc cycle in the Mn record of the Bisciaro Fm*

---

### **Description**

Data points which give the period (in meters) of the short kyr eccentricity cycle tracked in the wavelet scalogram of the manganese (XRF) record of the Bisciaro Formation  
The period was tracked using the [track\\_period\\_wavelet](#) function  
The tracking is based on a reinterpretation of Arts (2014)

### **Details**

Column 1: depth proxy record  
Column 2: period tracked in the wavelet scalogram of the manganese (XRF) record

### **References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

---

Bisciaro\_sial\_wt\_track  
*Period of the short kyr ecc cycle in the si/Al record of the Bisciaro Fm*

---

### **Description**

Data points which give the period (in meters) of the short kyr eccentricity cycle tracked in the wavelet scalogram of the silicon/aluminium (XRF) record of the Bisciaro Formation  
The period was tracked using the [track\\_period\\_wavelet](#) function  
The tracking is based on a reinterpretation of Arts (2014)

### **Details**

Column 1: depth proxy record  
Column 2: period tracked in the wavelet scalogram of the silicon/aluminium (XRF) record

### **References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

Bisciaro\_XRF

*XRF records of the Bisciaro Fm***Description**

XRF proxy records from the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy)

**Details**

Column 1: depth proxy record  
 Column 2-71: XRF proxy records

**References**

M.C.M. Arts, 2014, Magnetostratigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy). Unpublished Bsc. thesis

completed\_series

*Complete the tracking of cycle in a wavelet spectra***Description**

Use the traced series and the existing wavelet spectra to complete the tracking of a cycle of the wavelet spectra. The selected points using the [track\\_period\\_wavelet](#) function form an incomplete line unless every point is tracked. However clicking every individual point along a wavelet ridge is time intensive and error prone. To avoid errors and save time the [completed\\_series](#) function can be used to complete the tracing of a cycle in a wavelet spectra. The [completed\\_series](#) function interpolates the data points selected using the [track\\_period\\_wavelet](#). A search algorithm then looks up and replaces the interpolated curve values with the values of the nearest spectral peak in the wavelet spectra.

**Usage**

```
completed_series(  
  wavelet = NULL,  
  tracked_curve = NULL,  
  period_up = 1.2,  
  period_down = 0.8,  
  extrapolate = TRUE,  
  genplot = FALSE,  
  keep_editable = FALSE  
)
```

**Arguments**

wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
tracked_curve	Traced period result from the <code>track_period_wavelet</code> function.
period_up	The <code>period_up</code> parameter is the factor with which the linear interpolated <code>tracked_curve</code> curve is multiplied by. This linear interpolated <code>tracked_curve</code> multiplied by the <code>period_up</code> factor is the upper boundary which is used for detecting the spectral peak nearest to the linear interpolated <code>tracked_curve</code> curve. If no spectral peak is detected within the specified boundary the interpolated value is used instead. between spectral peaks Default=1.2,
period_down	The <code>period_down</code> parameter is the factor with which the linear interpolated <code>tracked_curve</code> curve is multiplied by. This linear interpolated <code>tracked_curve</code> multiplied by the <code>period_down</code> factor is the lower boundary which is used for detecting the spectral peak nearest to the linear interpolated <code>tracked_curve</code> curve. If no spectral peak is detected within the specified boundary the interpolated value is used instead. between spectral peaks Default=0.8,
extrapolate	Extrapolate the completed curve when through parts where no spectral peaks could be traced Default=TRUE.
genplot	Generate a plot Default=TRUE. The red curve is the completed curve, the black curve is the original curve.
keep_editable	Keep option to add extra features after plotting Default=FALSE

**Value**

Returns a matrix with 2 columns The first column is the depth axis The second column is the completed tracking of the period a cycle of the wavelet spectra

**Examples**

```
#Use the grey_track example points to complete the tracking of the
# precession cycle in the wavelet spectra of the grey scale data set
# of Zeeden et al., (2013).
```

```
grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )
```

```
#The ~22kyr precession cycle is between 0.25 and 1m The grey_track data
#set is a pre-loaded uncompleted tracking of the precession cycle
```

```
#grey_track <- track_period_wavelet(
```

```

#astro_cycle = 22,
#wavelet = NULL,
#n.levels = 100,
#periodlab = "Period (meters)",
#x_lab = "depth (meters)"
#)

grey_track <- completed_series(
  wavelet = grey_wt,
  tracked_curve = grey_track,
  period_up = 1.25,
  period_down = 0.75,
  extrapolate = TRUE,
  genplot = FALSE,
  keep_editable=FALSE
)

```

---

curve2sedrate

---

*Convert a tracked cycle to a sedimentation rate curve*


---

### Description

Converts the period of a tracked cycle to a sedimentation rate curve by assigning a duration (in kyr) to the period of a tracked cycle

### Usage

```
curve2sedrate(tracked_cycle_curve = NULL, tracked_cycle_period = NULL)
```

### Arguments

tracked\_cycle\_curve

A tracked cycle which is the result of using the [track\\_period\\_wavelet](#) function

Any input (matrix or data frame) in which the first column is depth in meters and the second column is period in meters

tracked\_cycle\_period

Period of the tracked cycle (in kyr).

### Value

The output is a matrix with 2 columns The first column is depth The second column sedimentation rate in cm/kyr

## Examples

```

#Conversion of the period (in meters) of a 405 kyr eccentricity cycle tracked
#in a wavelet spectra by assigning a duration of 405 kyr to the tracked cycle.
# the example uses the magnetic susceptibility data set of Pas et al., (2018)
# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE)

#convert period in meters to sedrate in cm/kyr
mag_track_sedrate <- curve2sedrate(tracked_cycle_curve=mag_track_complete,
  tracked_cycle_period=405)

```

---

curve2time

*Convert the tracked curve to a depth time space*

---

## Description

Converts the tracked curve to a depth time space.



**Usage**

```
curve2time(
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  genplot = FALSE,
  keep_editable = FALSE
)
```

**Arguments**

`tracked_cycle_curve` Curve of the cycle tracked using the [track\\_period\\_wavelet](#) function  
Any input (matrix or data frame) in which the first column is depth in meters and the second column is period in meters can be used.

`tracked_cycle_period` Period of the tracked curve in kyr.

`genplot` Generates a plot with depth vs time Default=FALSE.

`keep_editable` Keep option to add extra features after plotting Default=FALSE

**Value**

The output is a matrix with 2 columns. The first column is depth. The second column sedimentation rate in cm/kyr. If `genplot=TRUE` then a depth vs time plot will be plotted.

**Author(s)**

Based on the [sedrate2time](#) function of the 'astrochron' R package

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

**Examples**

```
#Convert a tracked curve to a depth time space. The examples uses the
#magnetic susceptibility data set of Pas et al., (2018).

## perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
```

```

#                               n.levels = 100,
#                               periodlab = "Period (metres)",
#                               x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set mag_track_solution is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE)

#convert period in meters to sedrate depth vs time
mag_track_time<- curve2time(tracked_cycle_curve=mag_track_complete,
  tracked_cycle_period=405,
  genplot=FALSE,
  keep_editable=FALSE)

```

---

curve2time_unc	<i>Convert the re-tracked curve results to a depth time space with uncertainty</i>
----------------	--

---

## Description

Converts the re-tracked curve results from [retrack\\_wt\\_MC](#) function to a depth time space while also taking into account the uncertainty of the tracked astronomical cycle

## Usage

```

curve2time_unc(
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  tracked_cycle_period_unc = NULL,
  tracked_cycle_period_unc_dist = "n",
  n_simulations = NULL,
  output = 1
)

```

**Arguments**

tracked_cycle_curve	Curve of the cycle tracked using the <a href="#">retrack_wt_MC</a> function Any input (matrix or data frame) with 3 columns in which column 1 is the x-axis, column 2 is the mean tracked frequency (in cycles/metres) column 3 1 standard deviation
tracked_cycle_period	Period of the tracked curve in kyr.
tracked_cycle_period_unc	uncertainty in the period of the tracked cycle
tracked_cycle_period_unc_dist	distribution of the uncertainty of the tracked cycle value need to be either "u" for uniform distribution or "n" for normal distribution Default="n"
n_simulations	number of time series to be modeled
output	If output = 1 a matrix with the predicted ages given the input for each run is given. If output = 2 a matrix with 6 columns is generated, the first column is depth/height, the other columns are the quantile (0.025,0.373,0.5,0.6827,0.975) age values of the runs if output = 3 a matrix with 4 columns is generated with the first column being depth/height, column 2 is the mean tracked duration (in kyrs) column 3 is mean duration + 1 standard deviation and column 4 is mean duration - 1 standard deviation

**Value**

If output = 1 a matrix with the predicted ages given the input for each run is given If output = 2 a matrix with 6 columns is generated, the first column is depth/height, the other columns are the quantile (0.02275, 0.373, 0.5, 0.6827, 0.97725) age values of the runs if output = 3 a matrix with 4 columns is generated with the first column being depth/height, column 2 is the mean tracked duration (in kyrs) column 3 is mean duration + 1 standard deviation and column 4 is mean duration - 1 standard deviation

**Author(s)**

Based on the [sedrate2time](#) function of the 'astrochron' R package

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

**Examples**

```
# Re-track the 110kyr eccentricity cycle in the wavelet scalogram
# from the XRF record of the Bisciaro data set of Arts (2014) and then
# add generate and age model including uncertainty

Bisciaro_al <- Bisciaro_XRF[, c(1, 61)]
Bisciaro_al <- astrochron::sortNave(Bisciaro_al, verbose=FALSE, genplot=FALSE)
```

```
Bisciaro_al <- astrochron::linterp(Bisciaro_al, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_al <- Bisciaro_al[Bisciaro_al[, 1] > 2, ]
```

```
Bisciaro_al_wt <-
  analyze_wavelet(
    data = Bisciaro_al,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )
```

```
# Bisciaro_al_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_al_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
# Bisciaro_al_wt_track <- completed_series(
#   wavelet = Bisciaro_al_wt,
#   tracked_curve = Bisciaro_al_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_al_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_al_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )
```

```
Bisciaro_ca <- Bisciaro_XRF[, c(1, 55)]
Bisciaro_ca <- astrochron::sortNave(Bisciaro_ca,verbose=FALSE,genplot=FALSE)
Bisciaro_ca <- astrochron::linterp(Bisciaro_ca, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_ca <- Bisciaro_ca[Bisciaro_ca[, 1] > 2, ]
```

```
Bisciaro_ca_wt <-
  analyze_wavelet(
    data = Bisciaro_ca,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )
```

```

)

# Bisciaro_ca_wt_track <-
# track_period_wavelet(
#   astro_cycle = 110,
#   wavelet = Bisciaro_ca_wt,
#   n.levels = 100,
#   periodlab = "Period (metres)",
#   x_lab = "depth (metres)"
# )
#
# Bisciaro_ca_wt_track <- completed_series(
#   wavelet = Bisciaro_ca_wt,
#   tracked_curve = Bisciaro_ca_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_ca_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_ca_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE)

Bisciaro_sial <- Bisciaro_XRF[,c(1,64)]
Bisciaro_sial <- astrochron::sortNave(Bisciaro_sial,verbose=FALSE,genplot=FALSE)
Bisciaro_sial <- astrochron::linterp(Bisciaro_sial, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_sial <- Bisciaro_sial[Bisciaro_sial[, 1] > 2, ]

Bisciaro_sial_wt <-
  analyze_wavelet(
    data = Bisciaro_sial,
    dj = 1 /200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_sial_wt_track <-
# track_period_wavelet(
#   astro_cycle = 110,
#   wavelet = Bisciaro_sial_wt,
#   n.levels = 100,
#   periodlab = "Period (metres)",
#   x_lab = "depth (metres)"
# )
#
#
#

```

```

# Bisciario_sial_wt_track <- completed_series(
#   wavelet = Bisciario_sial_wt,
#   tracked_curve = Bisciario_sial_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciario_sial_wt_track <-
#   loess_auto(
#     time_series = Bisciario_sial_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciario_Mn <- Bisciario_XRF[,c(1,46)]
Bisciario_Mn <- astrochron::sortNave(Bisciario_Mn, verbose=FALSE, genplot=FALSE)
Bisciario_Mn <- astrochron::linterp(Bisciario_Mn, dt = 0.01, verbose=FALSE, genplot=FALSE)
Bisciario_Mn <- Bisciario_Mn[Bisciario_Mn[, 1] > 2, ]

Bisciario_Mn_wt <-
  analyze_wavelet(
    data = Bisciario_Mn,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciario_Mn_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciario_Mn_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciario_Mn_wt_track <- completed_series(
#   wavelet = Bisciario_Mn_wt,
#   tracked_curve = Bisciario_Mn_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )

```

```

# Bisciario_Mn_wt_track <-
#   loess_auto(
#     time_series = Bisciario_Mn_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciario_Mg <- Bisciario_XRF[,c(1,71)]
Bisciario_Mg <- astrochron::sortNave(Bisciario_Mg, verbose=FALSE, genplot=FALSE)
Bisciario_Mg <- astrochron::linterp(Bisciario_Mg, dt = 0.01, verbose=FALSE, genplot=FALSE)
Bisciario_Mg <- Bisciario_Mg[Bisciario_Mg[, 1] > 2, ]

Bisciario_Mg_wt <-
  analyze_wavelet(
    data = Bisciario_Mg,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciario_Mg_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciario_Mg_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciario_Mg_wt_track <- completed_series(
#   wavelet = Bisciario_Mg_wt,
#   tracked_curve = Bisciario_Mg_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciario_Mg_wt_track <-
#   loess_auto(
#     time_series = Bisciario_Mg_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE)

```





```
output = 1)
```

---

curve2time\_unc\_anchor *Anchor an age model including its uncertainty to a single radiometric data*

---

### Description

Anchor an age model including its uncertainty to a single radiometric which has a known uncertainty and a known uncertainty in bed location. the model also allows for the addition of gap(s) in the record with a known durations. if no single radiometric date is specified then the gap(s) will be added to the original age-model

### Usage

```
curve2time_unc_anchor(
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  tracked_cycle_period_unc = NULL,
  tracked_cycle_period_unc_dist = "n",
  achor_age = NULL,
  achor_SD = NULL,
  achor_depth = NULL,
  achor_depth_unc = NULL,
  achor_depth_unc_dist = "u",
  gap_depth = NULL,
  gap_dur = NULL,
  gap_unc = NULL,
  gap_unc_dist = "n",
  n_simulations = NULL,
  output = 1
)
```

### Arguments

tracked\_cycle\_curve  
Curve of the cycle tracked using the [retrack\\_wt\\_MC](#) function  
Any input (matrix or data frame) with 3 columns in which column 1 is the x-axis, column 2 is the mean tracked frequency (in cycles/metres) column 3 1 standard deviation

tracked\_cycle\_period  
Period of the tracked curve in kyr.

tracked\_cycle\_period\_unc  
uncertainty in the period of the tracked cycle

tracked_cycle_period_unc_dist	distribution of the uncertainty of the tracked cycle value need to be either "u" for uniform distribution or "n" for normal distribution Default="n"
achor_age	age (in kyr) of the anchor
achor_SD	uncertainty given as 1 sd (in kyr) of the anchor
achor_depth	depth in (m) of the anchor
achor_depth_unc	uncertainty in (m) of the anchor
achor_depth_unc_dist	distribution of the uncertainty of the anchor age, value need to be either "u" for uniform distribution or "n" for normal distribution Default="n"
gap_depth	depth(s) at which a gap is present
gap_dur	duration in (kyr) of the gap
gap_unc	uncertainty in the duration (kyr) of the gap
gap_unc_dist	distribution of the uncertainty of the duration of the value need to be either "u" for uniform distribution or "n" for normal distribution Default="n"
n_simulations	number of time series to be modeled
output	if output = 1 a matrix with the predicted ages given the input for each run is given If output = 2 a matrix with 6 columns is generated, the first column is depth/height, the other columns are the quantile (0.025,0.373,0.5,0.6827,0.975) age values of the runs if output = 3 a matrix with 4 columns is generated with the first column being depth/height, column 2 is the mean tracked duration (in kyrs) column 3 is mean duration + 1 standard deviation and column 4 is mean duration - 1 standard deviation

### Value

If output = 1 a matrix with the predicted ages given the input for each run is given If output = 2 a matrix with 6 columns is generated, the first column is depth/height, the other columns are the quantile (0.025,0.373,0.5,0.6827,0.975) age values of the runs if output = 3 a matrix with 4 columns is generated with the first column being depth/height, column 2 is the mean tracked duration (in kyrs) column 3 is mean duration + 1 standard deviation and column 4 is mean duration - 1 standard deviation

### Author(s)

Part of the code is based on the [sedrate2time](#) function of the 'astrochron' R package

### References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

**Examples**

```

# Re-track the 110kyr eccentricity cycle in the wavelet scalogram
# from the XRF record of the Bisciaro data set of Arts (2014) and then
# add anchor it a U/Pb date of an ash bed and generate an anchored age model including uncertainty

Bisciaro_al <- Bisciaro_XRF[, c(1, 61)]
Bisciaro_al <- astrochron::sortNave(Bisciaro_al,verbose=FALSE,genplot=FALSE)
Bisciaro_al <- astrochron::linterp(Bisciaro_al, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_al <- Bisciaro_al[Bisciaro_al[, 1] > 2, ]

Bisciaro_al_wt <-
  analyze_wavelet(
    data = Bisciaro_al,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_al_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_al_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
# Bisciaro_al_wt_track <- completed_series(
#   wavelet = Bisciaro_al_wt,
#   tracked_curve = Bisciaro_al_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_al_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_al_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciaro_ca <- Bisciaro_XRF[, c(1, 55)]
Bisciaro_ca <- astrochron::sortNave(Bisciaro_ca,verbose=FALSE,genplot=FALSE)
Bisciaro_ca <- astrochron::linterp(Bisciaro_ca, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_ca <- Bisciaro_ca[Bisciaro_ca[, 1] > 2, ]

```

```

Bisciaro_ca_wt <-
  analyze_wavelet(
    data = Bisciaro_ca,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_ca_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_ca_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
# Bisciaro_ca_wt_track <- completed_series(
#   wavelet = Bisciaro_ca_wt,
#   tracked_curve = Bisciaro_ca_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_ca_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_ca_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE)

Bisciaro_sial <- Bisciaro_XRF[,c(1,64)]
Bisciaro_sial <- astrochron::sortNave(Bisciaro_sial, verbose=FALSE, genplot=FALSE)
Bisciaro_sial <- astrochron::linterp(Bisciaro_sial, dt = 0.01, verbose=FALSE, genplot=FALSE)
Bisciaro_sial <- Bisciaro_sial[Bisciaro_sial[, 1] > 2, ]

Bisciaro_sial_wt <-
  analyze_wavelet(
    data = Bisciaro_sial,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_sial_wt_track <-
#   track_period_wavelet(

```

```

#   astro_cycle = 110,
#   wavelet = Bisciaro_sial_wt,
#   n.levels = 100,
#   periodlab = "Period (metres)",
#   x_lab = "depth (metres)"
# )
#
#
# Bisciaro_sial_wt_track <- completed_series(
#   wavelet = Bisciaro_sial_wt,
#   tracked_curve = Bisciaro_sial_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_sial_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_sial_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciaro_Mn <- Bisciaro_XRF[,c(1,46)]
Bisciaro_Mn <- astrochron::sortNave(Bisciaro_Mn,verbose=FALSE,genplot=FALSE)
Bisciaro_Mn <- astrochron::linterp(Bisciaro_Mn, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_Mn <- Bisciaro_Mn[Bisciaro_Mn[, 1] > 2, ]

Bisciaro_Mn_wt <-
  analyze_wavelet(
    data = Bisciaro_Mn,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_Mn_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_Mn_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciaro_Mn_wt_track <- completed_series(

```

```

# wavelet = Bisciaro_Mn_wt,
# tracked_curve = Bisciaro_Mn_wt_track,
# period_up = 1.2,
# period_down = 0.8,
# extrapolate = TRUE,
# genplot = FALSE,
# keep_editable = FALSE
# )
# Bisciaro_Mn_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_Mn_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciaro_Mg <- Bisciaro_XRF[,c(1,71)]
Bisciaro_Mg <- astrochron::sortNave(Bisciaro_Mg,verbose=FALSE,genplot=FALSE)
Bisciaro_Mg <- astrochron::linterp(Bisciaro_Mg, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_Mg <- Bisciaro_Mg[Bisciaro_Mg[, 1] > 2, ]

Bisciaro_Mg_wt <-
  analyze_wavelet(
    data = Bisciaro_Mg,
    dj = 1 /200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_Mg_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_Mg_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciaro_Mg_wt_track <- completed_series(
#   wavelet = Bisciaro_Mg_wt,
#   tracked_curve = Bisciaro_Mg_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_Mg_wt_track <-
#   loess_auto(

```

```
# time_series = Bisciaro_Mg_wt_track,
# genplot = FALSE,
# print_span = FALSE,
# keep_editable = FALSE)

wt_list_bisc <- list(Bisciaro_al_wt,
                   Bisciaro_ca_wt,
                   Bisciaro_sial_wt,
                   Bisciaro_Mn_wt,
                   Bisciaro_Mg_wt)

#Instead of tracking, the tracked solution data sets Bisciaro_al_wt_track,
#Bisciaro_ca_wt_track, Bisciaro_sial_wt_track, Bisciaro_Mn_wt_track,
# Bisciaro_Mn_wt_track and Bisciaro_Mg_wt_track are used

data_track_bisc <- cbind(Bisciaro_al_wt_track[,2],
                        Bisciaro_ca_wt_track[,2],
                        Bisciaro_sial_wt_track[,2],
                        Bisciaro_Mn_wt_track[,2],
                        Bisciaro_Mg_wt_track[,2])

x_axis_bisc <- Bisciaro_al_wt_track[,1]

bisc_retrack <- retrack_wt_MC(wt_list = wt_list_bisc,
                             data_track = data_track_bisc,
                             x_axis = x_axis_bisc,
                             nr_simulations = 20,
                             seed_nr = 1337,
                             verbose = FALSE,
                             genplot = FALSE,
                             keep_editable = FALSE,
                             create_GIF = FALSE,
                             plot_GIF = FALSE,
                             width_plt = 600,
                             height_plt = 450,
                             period_up = 1.5,
                             period_down = 0.5,
                             plot.COI = TRUE,
                             n.levels = 100,
                             palette_name = "rainbow",
                             color_brewer = "grDevices",
                             periodlab = "Period (metres)",
                             x_lab = "depth (metres)",
                             add_avg = FALSE,
                             time_dir = TRUE,
                             file_name = NULL,
                             run_multicore = FALSE,
                             output = 5,
                             n_imgs = 50,
```

```

        plot_horizontal = TRUE,
        empty_folder = FALSE)

bisc_retrack_age_incl_unc <- curve2time_unc_anchor(tracked_cycle_curve = bisc_retrack,
tracked_cycle_period = 110,
tracked_cycle_period_unc = ((135-110)+(110-95))/2,
tracked_cycle_period_unc_dist = "n",
achor_age = 20609,
achor_SD = 40,
achor_depth = 7.25,
achor_depth_unc = 0.25,
achor_depth_unc_dist = "n",
gap_depth = NULL,
gap_dur = NULL,
gap_unc = NULL,
gap_unc_dist = "n",
n_simulations = 20,
output = 1)

```

---

curve2tune

*Convert data from the depth to the time domain*


---

## Description

Converts a data set from the depth to the time domain using a tracked curve/cycle to depth domain an assigning a duration (in kyr) set tracked curve/cycle.

## Usage

```

curve2tune(
  data = NULL,
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  genplot = FALSE,
  keep_editable = FALSE
)

```

## Arguments

**data** Data set (matrix with 2 columns 1st column depth 2nd column proxy value) which was used as input for the [analyze\\_wavelet](#) function. That result was then used to tracked a cycle using the [track\\_period\\_wavelet](#) function

**tracked\_cycle\_curve** Tracking result of a cycle tracked using the [track\\_period\\_wavelet](#) function Any input (matrix or data frame) in which the first column is depth in meters and the second column is period in meters can be used.



tracked_cycle_period	Period of the tracked curve (in kyr).
genplot	If genplot=TRUE 3 plots stacked on top of each other will be plotted. Plot 1: the original data set. Plot 2: the depth time plot. Plot 3: the data set in the time domain.
keep_editable	Keep option to add extra features after plotting Default=FALSE

### Value

The output is a matrix with 2 columns. The first column is time. The second column sedimentation proxy value.

If genplot=TRUE then 3 plots stacked on top of each other will be plotted. Plot 1: the original data set. Plot 2: the depth time plot. Plot 3: the data set in the time domain.

### Author(s)

Part of the code is based on the [sedrate2time](#) function of the 'astrochron' R package

### References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

### Examples

```
#The example uses the magnetic susceptibility data set of Pas et al., (2018).
# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (meters)",
#                                x_lab = "depth (meters)")

#Instead of tracking, the tracked solution data set mag_track_solution is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
```

```

    genplot = FALSE
  )

  # smooth the tracking of the 405 kyr eccentricity cycle
  mag_track_complete <- loess_auto(time_series = mag_track_complete,
    genplot = FALSE, print_span = FALSE)

  mag_track_time<- curve2tune(data=mag,
    tracked_cycle_curve=mag_track_complete,
    tracked_cycle_period=405,
    genplot = FALSE,
    keep_editable=FALSE)

```

---

delpts\_tracked\_period\_wt

*Remove tracking points which were tracked in a wavelet spectra*

---

### Description

Interactively select points for deletion With the [track\\_period\\_wavelet](#) function it is possible to track points in a wavelet spectra, however errors can be made and as such it is possible to delete these points with the [delpts\\_tracked\\_period\\_wt](#) function. This function allows one to select points for deletion. #'

### Usage

```

delpts_tracked_period_wt(
  tracking_pts = NULL,
  wavelet = NULL,
  n.levels = 100,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)",
  palette_name = "rainbow",
  color_brewer = "grDevices"
)

```

### Arguments

tracking_pts	Points tracked using the <a href="#">track_period_wavelet</a> function.
wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
n.levels	Number of color levels Default=100.
periodlab	label for the y-axis Default="Period (metres)".
x_lab	label for the x-axis Default="depth (metres)".

palette_name	Name of the color palette which is used for plotting. The color palettes that can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R package 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R package 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices

### Value

The results of the deletion of the tracking points is a matrix with 3 columns. The first column is depth/time The second column is the period of the tracked cycle The third column is the sedimentation rate based on the duration (in time) of the tracked cycle

### Examples

```
#Track the 405kyr eccentricity cycle in the magnetic susceptibility record
# of the Sullivan core of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)",
#                                palette_name ="rainbow",
#                                color_brewer ="grDevices)

#load the mag_track_solution data set to get an example data set from which
#data points can be deleted

mag_track_corr <- delpts_tracked_period_wt(tracking_pts = mag_track_solution,
```

```

wavelet = mag_wt,
n.levels = 100,
periodlab = "Period (metres)",
x_lab = "depth (metres)",
palette_name = "rainbow",
color_brewer = "grDevices")

```

---

depth\_rank\_example      *An example depth rank series*

---

### Description

The [depth\\_rank\\_example](#) example data set is a depth rank series which can be used as input for the [lithlog\\_disc](#) function which creates a discretized record which can then be used as input in the [analyze\\_wavelet](#) function

### Details

Column 1: depth (meters)  
Column 2: depth rank

---

dur\_gaps      *calculate the duration of stratigraphic gaps using astronomical cycles*

---

### Description

calculate the duration of stratigraphic gaps using the duration of stable astronomical cycles

### Usage

```

dur_gaps(
  proxies = NULL,
  retracked_period_1 = NULL,
  retracked_period_2 = NULL,
  min_max = NULL,
  n_simulations = 10,
  tracked_cycle_period = NULL,
  tracked_cycle_period_unc = NULL,
  tracked_cycle_period_unc_dist = "u",
  pts = 5,
  dj = 1/200,
  lowerPeriod = 1,

```

```

    upperPeriod = 3200,
    period_max = NULL,
    period_min = NULL,
    missing_cycle_dur = NULL,
    n_cycles_missing = 1,
    missing_cycle_unc = NULL,
    missing_cycle_unc_dist = "u",
    run_multicore = FALSE
)

```

## Arguments

proxies	list of proxies which were used to create a astrochronological age model and which are used to calculate the duration of the gap
retracked_period_1	A matrix of 3 columns in which the first column is depth/height. The second column is the period of the tracked cycle. The third column is uncertainty given as 1 standard deviation for the period of the tracked cycle. The gap to be modeled should be located in between retracked_period_1 and retracked_period_2
retracked_period_2	A matrix of 3 columns in which the first column is depth/height. The second column is the period of the tracked cycle. The third column is uncertainty given as 1 standard deviation for the period of the tracked cycle. The gap to be modeled should be located in between retracked_period_1 and retracked_period_2
min_max	list of "min" or "max" indicating whether time should be estimated between minima or maxima for each proxy
n_simulations	number of gap duration to calculate
tracked_cycle_period	period in time of the tracked cycle
tracked_cycle_period_unc	uncertainty in the period of the tracked cycle
tracked_cycle_period_unc_dist	distribution of the uncertainty of the tracked cycle value need to be either "u" for uniform distribution or "n" for normal distribution Default="u"
pts	the pts parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the pts parameter can be changed which can aid in peak detection. Usually increasing the pts parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=5#
dj	Spacing between successive scales. The CWT analyses analyses the signal using successive periods which increase by the power of 2 (e.g. $2^0=1, 2^1=2, 2^2=4, 2^3=8, 2^4=16$ ). To have more resolution in-between these steps the dj parameter exists, the dj parameter specifies how many extra steps/spacing in-between the power of 2 scaled CWT is added. The amount of steps is $1/x$ with a higher x indicating a

	smaller spacing. Increasing the increases the computational time of the CWT Default=1/200.
lowerPeriod	Lowest period to be analyzed Default=2. The CWT analyses the signal starting from the lowerPeriod to the upperPeriod so the proper selection these parameters allows to analyze the signal for a specific range of cycles. scaling is done using power 2 so for the best plotting results select a value to the power or 2.
upperPeriod	Upper period to be analyzed Default=1024. The CWT analyses the signal starting from the lowerPeriod to the upperPeriod so the proper selection these parameters allows to analyze the signal for a specific range of cycles. scaling is done using power 2 so for the best plotting results select a value to the power or 2.
period_max	Maximum period (upper boundary) to be used to extract a cycle.
period_min	Minimum period (lower boundary) to be used to extract a cycle.
missing_cycle_dur	duration of the missing cycles
n_cycles_missing	number of missing cycles Default=1
missing_cycle_unc	duration uncertainty of the missing cycle
missing_cycle_unc_dist	distribution of the uncertainty of the tracked cycle value need to be either "u" for uniform distribution or "n" for normal distribution Default="u"
run_multicore	Run function using multiple cores Default="FALSE"

**Value**

a vector with all the calculated gap durations

---

extract\_amplitude      *Extract amplitude from a signal*

---

**Description**

Extracts the amplitude from a signal using the continuous wavelet transform using a Morlet wavelet. The extraction of the amplitude is useful for cyclostratigraphic studies because the amplitude of an astronomical cycle is modulated by higher order astronomical cycles.

**Usage**

```
extract_amplitude(
  signal = NULL,
  pts = 3,
  genplot = FALSE,
  remean = TRUE,
  ver_results = FALSE,
  keep_editable = FALSE
)
```

**Arguments**

signal	Input signal from which the amplitude is extracted any signal in which the first column is depth/time and the second column is the proxy record from which the amplitude is extracted
pts	The pts parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the pts parameter can be changed which can aid in peak detection. Usually increasing the pts parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=3
genplot	If set to TRUE a plot with extracted amplitude will be displayed Default=FALSE.
remean	Prior to analysis the mean is subtracted from the data set to re-mean set Default=TRUE.
ver_results	To verify the amplitude extraction is representative of the amplitude extracted using the <code>extract_amplitude</code> function the results can be compared to the amplitude extracted using the <code>Hilbert_transform</code> if the mean difference is more then 5 whether the input contains a reliable enough signal with high a enough amplitude modulation to actually extract an amplitude from. Default=FALSE.
keep_editable	Keep option to add extra features after plotting Default=FALSE

**Value**

Returns a matrix with 2 columns. The first column is depth/time. The second column is the extracted amplitude

**Author(s)**

Code based on the `reconstruct` function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gibert P. Compo. The assignment of the standard deviation of the uncertainty of the wavelet is based on the work of Gabor (1946) and Russell et al., (2016)

**References**

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
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J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. *Geophysics* 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

## Examples

```
#Extract amplitude of the 405 kyr eccentricity cycle from the the magnetic
# susceptibility data set of De pas et al., (2018)
#Perform the CWT on the magnetic susceptibility data set of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set mag_track_solution
#is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE
)

#Smooth the completed tracking of the 405 kyr eccentricity cycle in the wavelet spectra

mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE)

mag_405_ecc <- extract_signal(
  tracked_cycle_curve = mag_track_complete,
  wavelet = mag_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  tracked_cycle_period = 405,
```



```

extract_cycle = 405,
tune = FALSE,
plot_residual = FALSE
)

#extract the amplitude of the 405 kyr eccentricity cycle
mag_ampl <- extract_amplitude(
signal = mag_405_ecc,
pts=3,
genplot = FALSE,
ver_results = FALSE,
keep_editable=FALSE)

```

---

extract_power	<i>Extract power from a wavelet spectra</i>
---------------	---

---

## Description

Extracts the spectral power from a wavelet spectra in the depth domain using a traced period and boundaries surround the traced period. The extraction of spectral is useful for cyclostratigraphic studies because the spectral power of an astronomical cycle is modulated by higher order astronomical cycles. The spectral power record from an astronomical cycle can thus be used as a proxy for amplitude modulating cycles. The traced period result from the [track\\_period\\_wavelet](#) function with boundaries is used to extract spectral power in the depth domain from a wavelet spectra.

## Usage

```

extract_power(
  completed_series = NULL,
  wavelet = NULL,
  period_up = 1.2,
  period_down = 0.8,
  tracked_cycle_period = NULL,
  extract_cycle_power = NULL
)

```

## Arguments

completed_series	Traced period result from the <a href="#">track_period_wavelet</a> function completed using the <a href="#">completed_series</a> . The input can be pre-smoothed using the the <a href="#">loess_auto</a> function.
wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
period_up	Upper period as a factor of the to be extracted power Default=1.2.
period_down	Lower period as a factor of the to be extracted power Default=0.8.

tracked\_cycle\_period

Period of the tracked cycle (make sure that tracked\_cycle\_period) and extract\_cycle\_power) are of the same unit (either depth or time domain).

extract\_cycle\_power

Period of the cycle for which the power will be extracted (make sure that extract\_cycle\_power) and tracked\_cycle\_period) are of the same unit (either depth or time domain).

### Value

Returns a matrix with 3 columns. The first column is depth/time. The second column is extracted power. The third column is extracted power/total power.

### Author(s)

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gilbert P. Compo. The assignment of the standard deviation of the uncertainty of the wavelet is based on the work of Gabor (1946) and Russell et al., (2016) The functionality of this function is inspired by the [integratePower](#) function of the 'astrochron' R package.

### References

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis <doi:10.1016/j.earscirev.2018.11.015>

### Examples

```
#Extract the power of the 405 kyr eccentricity cycle from the the magnetic
# susceptibility data set of De pas et al., (2018)
#Perform the CWT on the magnetic susceptibility data set of Pas et al., (2018)
```

```
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)
```

```
#Track the 405 kyr eccentricity cycle in a wavelet spectra
```

```
#mag_track <- track_period_wavelet(astro_cycle = 405,
#                               wavelet=mag_wt,
#                               n.levels = 100,
```

```

#                               periodlab = "Period (metres)",
#                               x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set mag_track_solution
#is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE
)

#Smooth the completed tracking of the 405 kyr eccentricity cycle in the wavelet spectra

mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE)

#extract the spectral power of the 405 kyr eccentricity cycle
mag_power <- extract_power(
  completed_series = mag_track_complete,
  wavelet = mag_wt,
  period_up = 1.2,
  period_down = 0.8,
  tracked_cycle_period = 405,
  extract_cycle_power = 405
)

```

---

extract\_power\_stable *Extract power from a wavelet spectra by using a constant period/duration*

---

### Description

Extract spectral power from the wavelet using a constant period/duration and boundaries as selection criteria. The extraction of spectral is useful for cyclostratigraphic studies because the spectral power of an astronomical cycle is modulated by higher order astronomical cycles. The spectral power record from an astronomical cycle can thus be used as a proxy for amplitude modulating cycles. The spectral power is extracted from a wavelet spectra which was created using the [analyze\\_wavelet](#) function for a given, cycle, period\_up and period\_down

### Usage

```

extract_power_stable(
  wavelet = NULL,
  cycle = NULL,

```

```

    period_up = 1.2,
    period_down = 0.8
  )

```

### Arguments

wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
cycle	Period of cycle for which the power will be extracted from the record.
period_up	Specifies the upper period of the to be extracted power Default=1 . 2.
period_down	specifies the lower period of the to be extracted power Default=0 . 8.

### Value

Returns a matrix with 3 columns. The first column is depth/time. The second column is extracted power. The third column is extracted power/total power.

### Author(s)

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gilbert P. Compo (1998). The functionality of this function is inspired by the [integratePower](#) function of the 'astrochron' R package

### References

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis <doi:10.1016/j.earscirev.2018.11.015>

### Examples

```

#Extract the spectral power of the 210 yr de Vries cycle from the Total Solar
#Irradiance data set of Steinhilber et al., (2012).

TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = FALSE,
    omega_nr = 6
  )
TSI_wt_pwr_de_Vries_cycle <- extract_power_stable(

```

```

    wavelet = TSI_wt,
    cycle = 210,
    period_up = 1.2,
    period_down = 0.8
)

```

---

extract\_signal

*Extract signal from a wavelet spectra using a traced period curve*


---

### Description

Extract signal power from the wavelet in the depth domain using the traced period.

### Usage

```

extract_signal(
  tracked_cycle_curve = NULL,
  wavelet = NULL,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  tracked_cycle_period = NULL,
  extract_cycle = NULL,
  tune = FALSE,
  plot_residual = FALSE
)

```

### Arguments

tracked_cycle_curve	Traced period result from the track_period_wavelet function completed using the completed_series. The input can be pre-smoothed using the the loess_auto function.
wavelet	wavelet object created using the <a href="#">analyze_wavelet</a> function.
period_up	Upper period as a factor of the to be extracted cycle Default=1.2.
period_down	Lower period as a factor of the to be extracted cycle Default=0.8.
add_mean	Add mean to the extracted cycle Default=TRUE.
tracked_cycle_period	Period in time of the traced cycle.
extract_cycle	Period of the to be extracted cycle.
tune	Convert record from the depth to the time domain using the traced period Default=FALSE.
plot_residual	Plot the residual signal after extraction of set cycle Default=FALSE.

**Value**

Returns a matrix with 2 columns The first column is depth/time The second column is extracted signal

**Author(s)**

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gibert P. Compo (1998).

**References**

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

**Examples**

```
#Extract the 405 kyr eccentricity cycle from the the magnetic susceptibility \cr
#record of the Sullivan core and use the Gabor uncertainty principle to define \cr
#the mathematical uncertainty of the analysis and use a factor of that standard \cr
#deviation to define boundaries.

#Perform the CWT
mag_wt <- analyze_wavelet(data = mag,
dj = 1/100,
lowerPeriod = 0.1,
upperPeriod = 254,
verbose = FALSE,
omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \code{\link{mag_track_solution}} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
```

```

    period_down = 0.8,
    extrapolate = TRUE,
    genplot = FALSE
  )

  # smooth the tracking of the 405 kyr eccentricity cycle
  mag_track_complete <- loess_auto(time_series = mag_track_complete,
    genplot = FALSE, print_span = FALSE)

  # extract the 405 kyr eccentricity cycle from the wavelet spectrum and use the \cr
  # tracked cycle curve and set factors of the extracted cycle as boundaries

  mag_405_ecc <- extract_signal(
    tracked_cycle_curve = mag_track_complete,
    wavelet = mag_wt,
    period_up = 1.2,
    period_down = 0.8,
    add_mean = TRUE,
    tracked_cycle_period = 405,
    extract_cycle = 405,
    tune = FALSE,
    plot_residual = FALSE
  )

```

---

extract\_signal\_stable *Extract a signal/cycle from a wavelet spectra using a set period and boundaries*

---

### Description

Extracts a cycle from the wavelet object created using the [analyze\\_wavelet](#) function using a fixed period and fixed period boundaries defined as factors of the original cycle

### Usage

```

extract_signal_stable(
  wavelet = NULL,
  cycle = NULL,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  plot_residual = FALSE,
  keep_editable = FALSE
)

```

### Arguments

wavelet            Wavelet object created using the [analyze\\_wavelet](#) function.

cycle	Period of the cycle which needs to be extracted.
period_up	Specifies the upper period as a factor of the to be extracted cycle Default=1.2.
period_down	Specifies the lower period as a factor of the to be extracted cycle Default=0.8.
add_mean	Add mean to the extracted cycle Default=TRUE.
plot_residual	plot the residual signal after extraction of set cycle Default=FALSE.
keep_editable	Keep option to add extra features after plotting Default=FALSE

### Value

#Returns a matrix with 2 columns. The first column is time/depth. The second column is the extracted signal/cycle.

### Author(s)

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gibert P. Compo (1998).

### References

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

### Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar
#Irradiance data set of Steinhilber et al., (2012)
```

```
#Perform the CWT
TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = FALSE,
  omega_nr = 6
)
```

```
#Extract the 210 yr de Vries cycle from the wavelet spectra
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
  cycle=210,
  period_up =1.25,
  period_down = 0.75,
  add_mean=TRUE,
```



```
plot_residual=FALSE,  
keep_editable=FALSE)
```

---

extract\_signal\_stable\_V2

*Extract signal from a wavelet spectrum using a upper and lower period boundary*

---

### Description

Extract a signal from the wavelet using a upper and lower period boundary

### Usage

```
extract_signal_stable_V2(  
  wavelet = NULL,  
  period_max = NULL,  
  period_min = NULL,  
  add_mean = TRUE,  
  plot_residual = FALSE,  
  keep_editable = FALSE  
)
```

### Arguments

wavelet	wavelet object created using the <a href="#">analyze_wavelet</a> function.
period_max	Maximum period (upper boundary) to be used to extract a cycle.
period_min	Minimum period (lower boundary) to be used to extract a cycle.
add_mean	Add mean to the extracted cycle Default=TRUE.
plot_residual	Plot the signal from which the extracted cycle is subtracted Default=FALSE.
keep_editable	Keep option to add extra features after plotting Default=FALSE

### Value

Signal extracted from the wavelet spectra. Output is a matrix with the first column being depth/time and the second column is the cycle extracted from the proxy record.

### Author(s)

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gibert P. Compo (1998).

## References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

## Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar  
# Irradiance data set of Steinhilber et al., (2012)
```

```
TSI_wt <-  
analyze_wavelet(  
  data = TSI,  
  dj = 1/200,  
  lowerPeriod = 16,  
  upperPeriod = 8192,  
  verbose = FALSE,  
  omega_nr = 6  
)
```

```
de_Vries_cycle <- extract_signal_stable_V2(wavelet=TSI_wt,  
  period_max = 240,  
  period_min = 180,  
  add_mean=TRUE,  
  plot_residual=FALSE,  
  keep_editable=FALSE)
```

---

extract\_signal\_standard\_deviation

*Extract a signal using standard deviation*

---

## Description

Extract signal from a wavelet spectra in the depth domain using a the standard deviation of the omega (number of cycles) as boundaries. The uncertainty is based on the Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet. The calculated uncertainty is the underlying analytical uncertainty which is the result of applying the Gabor uncertainty principle to the continuous wavelet transform using a Morlet wavelet.

**Usage**

```
extract_signal_standard_deviation(
  wavelet = NULL,
  tracked_cycle_curve = NULL,
  multi = 1,
  extract_cycle = NULL,
  tracked_cycle_period = NULL,
  add_mean = TRUE,
  tune = FALSE,
  genplot_uncertainty_wt = FALSE,
  genplot_extracted = FALSE,
  keep_editable = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices"
)
```

**Arguments**

wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
tracked_cycle_curve	Curve of the cycle tracked using the <a href="#">track_period_wavelet</a> function. Any input (matrix or data frame) in which the first column is depth or time and the second column is period should work.
multi	multiple of the standard deviation to be used as boundaries for the cycle extraction Default=1.
extract_cycle	Period of the cycle to be extracted.
tracked_cycle_period	Period of the tracked cycle.
add_mean	Add mean to the extracted cycle Default=TRUE.
tune	Tune data set using the Default=tracked_cycle_curve curve Default=FALSE.
genplot_uncertainty_wt	Generate a wavelet spectra plot with the tracked curve and its analytical uncertainty based the Gabor uncertainty principle applied continuous wavelet transform using a Morlet wavelet on superimposed on top of it. In the plot the red curve and blue curves are the upper and lower bounds based on the multi parameter which x-times the standard deviation of uncertainty. The black curve is the Default=FALSE curve.
genplot_extracted	Generates a plot with the data set and the extracted cycle on top Default=FALSE of it.
keep_editable	Keep option to add extra features after plotting Default=FALSE
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of

these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R package 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R package 'grDevices' run the grDevices::hcl.pals() function

color\_brewer Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices

### Value

Signal extracted from the wavelet spectra. Output is a matrix with the first column being depth/time and the second column is the astronomical cycle extracted from the proxy record

If genplot\_uncertainty\_wt=TRUE then a wavelet spectra will be plotted with the uncertainty superimposed on top of it. In the plot the red curve and blue curves are the upper and lower bounds based on the multi parameter.The black curve is the Default=tracked\_cycle\_curve curve. If genplot\_extracted=TRUE plot with the data set and the extracted cycle on top of it will be plotted.

### Author(s)

Code based on the [reconstruct](#) function of the 'WaveletComp' R package which is based on the wavelet 'MATLAB' code written by Christopher Torrence and Gibert P. Compo (1998). The assignment of the standard deviation of the uncertainty of the wavelet is based on the work of Gabor (1946) and Russell et al., (2016)

### References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)
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J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. *Geophysics* 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

## Examples

```
#Extract the 405 kyr eccentricity cycle from the magnetic susceptibility
#record of the Sullivan core of Pas et al., (2018) and use the Gabor
# uncertainty principle to define the mathematical uncertainty of the
# analysis and use a factor of that standard deviation to define
# boundaries

# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)",
#                                palette_name="rainbow",
#                                color_brewer="grDevices")

#Instead of tracking, the tracked solution data set mag_track_solution is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE)

# extract the 405 kyr eccentricity cycle from the wavelet spectrum and use
# the Gabor uncertainty principle to define the mathematical uncertainty of
```

```

# the analysis and use a multiple of the derived standard deviation to define boundaries

mag_405_ecc <- extract_signal_standard_deviation(
  wavelet = mag_wt,
  tracked_cycle_curve = mag_track_complete,
  multi = 1,
  extract_cycle = 405,
  tracked_cycle_period = 405,
  add_mean = TRUE,
  tune = FALSE,
  genplot_uncertainty_wt = FALSE,
  genplot_extracted = FALSE,
  keep_editable=FALSE,
  palette_name="rainbow",
  color_brewer="grDevices"
)

```

---

flmw

*Fit linear models to spectral peaks extracted from the wavelet spectra to astronomical cycles multiplied by sedimentation rate  $x$*

---

## Description

The `flmw` function is used calculate the linear correlation for a list of astronomical cycles transformed using a range of sedimentation rates and then compared to spectral peaks of a wavelet spectra

## Usage

```

flmw(
  wavelet = NULL,
  sedrate_low = NULL,
  sedrate_high = NULL,
  spacing = NULL,
  cycles = c(NULL),
  x_lab = "depth",
  y_lab = "sedrate",
  run_random = FALSE,
  rand_simulations = 1000,
  run_multicore = FALSE,
  genplot = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices",
  plot_res = 2,
  keep_editable = FALSE,
  verbose = FALSE
)

```

**Arguments**

wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function
sedrate_low	Minimum sedimentation rate (cm/kyr) for which the sum of maximum spectral power is calculated for.
sedrate_high	Maximum sedimentation rate (cm/kyr) for which the sum of maximum spectral power is calculated for.
spacing	Spacing (cm/kyr) between sedimentation rates
cycles	Astronomical cycles (in kyr) for which the combined sum of maximum spectral power is calculated for
x_lab	label for the x-axis Default="depth"
y_lab	label for the y-axis Default="sedrate"
run_random	run multiple simulation to calculate percentile against the 0 hypothesis
rand_simulations	nr of simulations to calculate percentile against the 0 hypothesis
run_multicore	run simulation using multiple cores Default=FALSE the simulation is run at x-2 cores to allow the 2 remaining processes to run background processes
genplot	Generate plot Default="FALSE"
palette_name	Name of the color palette which is used for plotting. The color palettes that can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R package 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R package 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices
plot_res	options 1-8 option 1: slope coefficient, option 2: r squared, option 3: nr of components, option 4: difference to the origin , option 5: slope coefficient percentile option 6: r squared percentile, option 7: nr of components percentile, option 8: difference to the origin percentile Default=2
keep_editable	Keep option to add extra features after plotting Default=FALSE
verbose	Print text Default=FALSE.

**Value**

Returns a list which contains 10 elements element 1: slope coefficient element 2: r squared element 3: nr of components element 4: difference to the origin element 5: slope coefficient percentile element 6: r squared percentile element 7: nr of components percentile, element 8: difference to the origin percentile element 9: y-axis values of the matrices which is sedimentation rate element 10: x-axis values of the matrices which is depth

**Author(s)**

Based on the [eAsm](#) function of the 'astrochron' R package and the 'eCOCO' and 'COCO' function of the 'Acycle' software

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis <doi:10.1016/j.earscirev.2018.11.015>

Acycle: Time-series analysis software for paleoclimate research and education, Mingsong Li, Linda Hinnov, Lee Kump, Computers & Geosciences, Volume 127, 2019, Pages 12-22, ISSN 0098-3004, <doi:10.1016/j.cageo.2019.02.011>

Tracking variable sedimentation rates and astronomical forcing in Phanerozoic paleoclimate proxy series with evolutionary correlation coefficients and hypothesis testing, Mingsong Li, Lee R. Kump, Linda A. Hinnov, Michael E. Mann, Earth and Planetary Science Letters, Volume 501, T2018, Pages 165-179, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.08.041>

**Examples**

```
#estimate sedimentation rate for the magnetic susceptibility record
# of the Sullivan core of Pas et al., (2018).

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

sedrates <- flmw(wavelet = mag_wt,
  sedrate_low = 0.5,
  sedrate_high = 4,
  spacing = 0.05,
  cycles = c(2376, 1600, 1180, 696, 406, 110),
  x_lab = "depth",
  y_lab = "sedrate",
  run_random = FALSE,
  rand_simulations = 50, # increase to get better constrained results
  run_multicore = FALSE,
  genplot = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices",
  plot_res = 2,
```



```
keep_editable=FALSE,
verbose=FALSE)
```

---

```
geo_col          Generate standard color codes for the Geological Time Scale
```

---

### Description

Generates the R color code which corresponds its respective geological subdivision

### Usage

```
geo_col(name = NULL)
```

### Arguments

name                    Name of the geologchronological subdivision

### Value

Returns the color code of the geological subdivision

### References

Ogg, Gabi & Ogg, James & Gradstein, Felix. (2021). Recommended color coding of stages - Appendix 1 from Geologic Time Scale 2020.

### Examples

```
#generate the Silurian part of the GTS
plot.new()
plot(
  x = c(0, 1),
  y = c(419.2, 443.8),
  col = "white",
  xlab = "",
  ylab = "Time (Ma)",
  xaxt = "n",
  xaxs = "i",
  yaxs = "i",
  ylim = rev(c(419, 444))
) # Draw empty plot

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Rhuddanian"),
  col =geo_col("Rhuddanian")
)
```

```
text(
  0.85,geo_mid("Rhuddanian"),
  "Rhuddanian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Aeronian"),
  col =geo_col("Aeronian")
)

text(
  0.85,geo_mid("Aeronian"),
  "Aeronian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Telychian"),
  col =geo_col("Telychian")
)

text(
  0.85,geo_mid("Telychian"),
  "Telychian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Sheinwoodian"),
  col =geo_col("Sheinwoodian")
)

text(
  0.85,geo_mid("Sheinwoodian"),
  "Sheinwoodian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
```

```
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Homerian"),
col =geo_col("Homerian")
)

text(
  0.85,geo_mid("Homerian"),
  "Homerian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Gorstian"),
  col =geo_col("Gorstian")
)

text(
  0.85,geo_mid("Gorstian"),
  "Gorstian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Ludfordian"),
  col =geo_col("Ludfordian")
)

text(
  0.85,geo_mid("Ludfordian"),
  "Ludfordian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Pridoli_Age"),
  col =geo_col("Pridoli_Age")
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Pridoli"),
```

```
col =geo_col("Pridoli")
)

text(
  0.5,geo_mid("Pridoli"),
  "Pridoli",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Ludlow"),
  col =geo_col("Ludlow")
)

text(
  0.5,geo_mid("Ludlow"),
  "Ludlow",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Wenlock"),
  col =geo_col("Wenlock")
)

text(
  0.5,geo_mid("Wenlock"),
  "Wenlock",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Llandovery"),
  col =geo_col("Llandovery")
)

text(
  0.5,geo_mid("Llandovery"),
  "Llandovery",
  cex = 1,
  col = "black",
  srt = 0
)
```

```
polygon(  
  x = c(0, 0.33, 0.33, 0),  
  y = geo_loc("Silurian"),  
  col = geo_col("Silurian")  
)  
  
text(  
  0.165, geo_mid("Silurian"),  
  "Silurian",  
  cex = 1,  
  col = "black",  
  srt = 0  
)
```

---

geo\_loc

*Generates ages for the boundaries of a geochronological subdivision*

---

### **Description**

Generates ages for the boundaries of a geochronological subdivision which is based on the Geological Time Scale

### **Usage**

```
geo_loc(name = NULL)
```

### **Arguments**

name                    Name of the geologchronological subdivision

### **Value**

Returns the ages of the boundary of a geochronological subdivision which can then be added to a polygon object

### **References**

Ogg, Gabi & Ogg, James & Gradstein, Felix. (2021). Recommended color coding of stages - Appendix 1 from Geologic Time Scale 2020.

### **Examples**

```
#generate the Silurian part of the GTS  
plot.new()  
plot(  
  x = c(0, 1),
```

```
y = c(419.2, 443.8),
col = "white",
xlab = "",
ylab = "Time (Ma)",
xaxt = "n",
xaxs = "i",
yaxs = "i",
ylim = rev(c(419, 444))
) # Draw empty plot

polygon(
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Rhuddanian"),
col =geo_col("Rhuddanian")
)

text(
0.85,geo_mid("Rhuddanian"),
"Rhuddanian",
cex = 1,
col = "black",
srt = 0
)

polygon(
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Aeronian"),
col =geo_col("Aeronian")
)

text(
0.85,geo_mid("Aeronian"),
"Aeronian",
cex = 1,
col = "black",
srt = 0
)

polygon(
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Telychian"),
col =geo_col("Telychian")
)

text(
0.85,geo_mid("Telychian"),
"Telychian",
cex = 1,
col = "black",
srt = 0
)

polygon(
```

```
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Sheinwoodian"),
col =geo_col("Sheinwoodian")
)

text(
  0.85,geo_mid("Sheinwoodian"),
  "Sheinwoodian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Homerian"),
  col =geo_col("Homerian")
)

text(
  0.85,geo_mid("Homerian"),
  "Homerian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Gorstian"),
  col =geo_col("Gorstian")
)

text(
  0.85,geo_mid("Gorstian"),
  "Gorstian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Ludfordian"),
  col =geo_col("Ludfordian")
)

text(
  0.85,geo_mid("Ludfordian"),
  "Ludfordian",
  cex = 1,
```

```
col = "black",
srt = 0
)

polygon(
x = c(0.66, 1, 1, 0.66),
y = geo_loc("Pridoli_Age"),
col =geo_col("Pridoli_Age")
)

polygon(
x = c(0.33, 0.66, 0.66, 0.33),
y = geo_loc("Pridoli"),
col =geo_col("Pridoli")
)

text(
0.5,geo_mid("Pridoli"),
"Pridoli",
cex = 1,
col = "black",
srt = 0
)

polygon(
x = c(0.33, 0.66, 0.66, 0.33),
y = geo_loc("Ludlow"),
col =geo_col("Ludlow")
)

text(
0.5,geo_mid("Ludlow"),
"Ludlow",
cex = 1,
col = "black",
srt = 0
)

polygon(
x = c(0.33, 0.66, 0.66, 0.33),
y = geo_loc("Wenlock"),
col =geo_col("Wenlock")
)

text(
0.5,geo_mid("Wenlock"),
"Wenlock",
cex = 1,
col = "black",
srt = 0
)
```



```
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Llandovery"),
  col = geo_col("Llandovery")
)

text(
  0.5, geo_mid("Llandovery"),
  "Llandovery",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0, 0.33, 0.33, 0),
  y = geo_loc("Silurian"),
  col = geo_col("Silurian")
)

text(
  0.165, geo_mid("Silurian"),
  "Silurian",
  cex = 1,
  col = "black",
  srt = 0
)
```

---

geo\_mid

*Generate the mean age of a geological subdivision*

---

### **Description**

Generates the mean age of a geological subdivision which is based on the Geological Time Scale

### **Usage**

```
geo_mid(name = NULL)
```

### **Arguments**

name                    Name of the geologchronological subdivision

### **Value**

Returns the mean age of the geochronological subdivision

## References

Ogg, Gabi & Ogg, James & Gradstein, Felix. (2021). Recommended color coding of stages - Appendix 1 from Geologic Time Scale 2020.

## Examples

```
#generate the Silurian part of the GTS
plot.new()
plot(
  x = c(0, 1),
  y = c(419.2, 443.8),
  col = "white",
  xlab = "",
  ylab = "Time (Ma)",
  xaxt = "n",
  xaxs = "i",
  yaxs = "i",
  ylim = rev(c(419, 444))
) # Draw empty plot

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Rhuddanian"),
  col =geo_col("Rhuddanian")
)

text(
  0.85,geo_mid("Rhuddanian"),
  "Rhuddanian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Aeronian"),
  col =geo_col("Aeronian")
)

text(
  0.85,geo_mid("Aeronian"),
  "Aeronian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Telychian"),
  col =geo_col("Telychian")
)
```

```
)

text(
  0.85,geo_mid("Telychian"),
  "Telychian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Sheinwoodian"),
  col =geo_col("Sheinwoodian")
)

text(
  0.85,geo_mid("Sheinwoodian"),
  "Sheinwoodian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Homerian"),
  col =geo_col("Homerian")
)

text(
  0.85,geo_mid("Homerian"),
  "Homerian",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.66, 1, 1, 0.66),
  y = geo_loc("Gorstian"),
  col =geo_col("Gorstian")
)

text(
  0.85,geo_mid("Gorstian"),
  "Gorstian",
  cex = 1,
  col = "black",
  srt = 0
)
```

```
polygon(  
  x = c(0.66, 1, 1, 0.66),  
  y = geo_loc("Ludfordian"),  
  col =geo_col("Ludfordian")  
)  
  
text(  
  0.85,geo_mid("Ludfordian"),  
  "Ludfordian",  
  cex = 1,  
  col = "black",  
  srt = 0  
)  
  
polygon(  
  x = c(0.66, 1, 1, 0.66),  
  y = geo_loc("Pridoli_Age"),  
  col =geo_col("Pridoli_Age")  
)  
  
polygon(  
  x = c(0.33, 0.66, 0.66, 0.33),  
  y = geo_loc("Pridoli"),  
  col =geo_col("Pridoli")  
)  
  
text(  
  0.5,geo_mid("Pridoli"),  
  "Pridoli",  
  cex = 1,  
  col = "black",  
  srt = 0  
)  
  
polygon(  
  x = c(0.33, 0.66, 0.66, 0.33),  
  y = geo_loc("Ludlow"),  
  col =geo_col("Ludlow")  
)  
  
text(  
  0.5,geo_mid("Ludlow"),  
  "Ludlow",  
  cex = 1,  
  col = "black",  
  srt = 0  
)  
  
polygon(  
  x = c(0.33, 0.66, 0.66, 0.33),  
  y = geo_loc("Ludlow"),  
  col =geo_col("Ludlow")  
)
```

```
x = c(0.33, 0.66, 0.66, 0.33),
y = geo_loc("Wenlock"),
col =geo_col("Wenlock")
)

text(
  0.5,geo_mid("Wenlock"),
  "Wenlock",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0.33, 0.66, 0.66, 0.33),
  y = geo_loc("Llandovery"),
  col =geo_col("Llandovery")
)

text(
  0.5,geo_mid("Llandovery"),
  "Llandovery",
  cex = 1,
  col = "black",
  srt = 0
)

polygon(
  x = c(0, 0.33, 0.33, 0),
  y = geo_loc("Silurian"),
  col =geo_col("Silurian")
)

text(
  0.165,geo_mid("Silurian"),
  "Silurian",
  cex = 1,
  col = "black",
  srt = 0
)
```

---

grey

*Grey scale record IODP 926 of Zeeden et al., (2013)*

---

### **Description**

IODP 926 grey scale record of Zeeden et al., (2013) for the (154-174m) interval. The (154-174m) interval spans the Miocene.

**Details**

Column 1: depth (meters)  
 Column 2: greyscale value

**References**

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369, 2013, Pages 430-451, ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

---

grey_track	<i>Tracking points of the precession (22 kyr cycle) IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)</i>
------------	--

---

**Description**

Example data which consists of tracking points of the precession (22 kyr cycle) in the wavelet scalogram of the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

**Details**

Column 1: Depth (meters)  
 Column 2: period (meters)

**References**

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369, 2013, Pages 430-451, ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

---

GTS_info	<i>Information of the Geological timescale 2020</i>
----------	---

---

**Description**

GTS\_info data set consists the information of the Geological timescale 2020 including the color data of Ogg et al., (2021) The ages, durations, uncertainties and colors of the Geological timescale 2020 are included in the data set

**Details**

Column 1: name  
Column 2: type  
Column 1: top age  
Column 1: top error  
Column 1: bottom age  
Column 1: bottom error  
Column 1: Cyan value  
Column 1: Magenta value  
Column 1: Yellow value  
Column 1: Key value  
Column 1: Red Value  
Column 1: Green value  
Column 1: Blue value  
Column 1: font style  
Column 1: font color

**References**

Ogg, Gabi & Ogg, James & Gradstein, Felix. (2021). Recommended color coding of stages - Appendix 1 from Geologic Time Scale 2020.

---

Hilbert_transform	<i>Perform a Hilbert transform on a signal</i>
-------------------	--

---

**Description**

Extract the amplitude modulation using the Hilbert transform.

**Usage**

```
Hilbert_transform(data = NULL, demean = TRUE, nr_pad = 100)
```

**Arguments**

data	Input is a time series with the first column being depth or time and the second column being a proxy.
demean	Remove the mean from the time series.
nr_pad	nr of points added tot the top and bottom of the data set to mitigate the edging effect of the Hilbert transform.

**Value**

Returns a matrix with 2 columns. The first column is depth/time. The second column is the Hilbert transform of the signal.

**Author(s)**

Based on the the [inst.pulse](#) function of the 'DecomposeR' R package.

**References**

Wouters, S., Crucifix, M., Sinnesael, M., Da Silva, A.C., Zeeden, C., Zivanovic, M., Boulvain, F., Devleeschouwer, X., 2022, "A decomposition approach to cyclostratigraphic signal processing". *Earth-Science Reviews* 225 (103894). <doi:10.1016/j.earscirev.2021.103894>

Huang, Norden E., Zhaohua Wu, Steven R. Long, Kenneth C. Arnold, Xianyao Chen, and Karin Blank. 2009. "On Instantaneous Frequency". *Advances in Adaptive Data Analysis* 01 (02): 177–229. <doi:10.1142/S1793536909000096>

**Examples**

```
#Example in which the Hilbert transform (eg. amplitude modulation) of the ~210yr
#de Vries cycle is extracted from the Total Solar Irradiance data set of
#Steinhilber et al., (2012)
```

```
#Perform the CWT
TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = FALSE,
  omega_nr = 6
)
```

```
#Extract the 210 yr de Vries cycle from the wavelet spectra
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
  cycle=210,
  period_up =1.25,
  period_down = 0.75,
  add_mean=TRUE,
  plot_residual=FALSE)
```

```
#Perform the Hilbert transform on the amplitude record of the 210 yr de Vries
# cycle which was extracted from the wavelet spectra
```

```
de_Vries_cycle_hilbert <- Hilbert_transform(data=de_Vries_cycle,demean=TRUE)
```



## Description

Discretizes lithologs to allow further time-series analysis first the Greatest common divisor/highest common factor is calculated which is then used to discretize the litholog to an evenly sampled data series. The function is designed to place the boundary at the original depth level of the bed boundaries. The Greatest common divisor/highest common factor can be a very small number as such the discretized data set can be large which impacts computational performance later on therefore a linear interpolation option is added to downscale the data to allow for computational efficiency later on. This is made to discretize lithologs created using the 'Stratigrapher' package. as such the same data format for input is used. eg. column 1 is bottom of the bed, column 2 is top of bed, column 3 is depth rank/proxy value

## Usage

```
lithlog_disc(
  litholog = NULL,
  subset_fact = 10,
  lin_interp = FALSE,
  dt = NULL,
  genplot = FALSE,
  x_lab = "rank",
  y_lab = "depth (m)",
  keep_editable = FALSE
)
```

## Arguments

<code>litholog</code>	litholog input matrix with 3 columns column 1 is bottom of the bed, column 2 is top of bed, column 3 is depth rank/proxy value
<code>subset_fact</code>	subset factor which is x times the greatest common divider Default=10.
<code>lin_interp</code>	Linear interpolation of the data set Default=FALSE
<code>dt</code>	step size Default=NULL.
<code>genplot</code>	generate plot Default=FALSE
<code>x_lab</code>	label for the x-axis Default="rank"
<code>y_lab</code>	label for the y-axis Default="depth (m)"
<code>keep_editable</code>	Keep option to add extra features after plotting Default=FALSE

## Value

Returns a matrix with 2 columns, the first column is depth the second column is the depth/rank proxy If `genplot` is Default=TRUE then a plot of the discretized time series is plotted

## References

Wouters, S., Da Silva, A.-C., Boulvain, F., and Devleeschouwer, X.. 2021. Stratigrapher: Concepts for Litholog Generation in R. The R Journal. <doi:10.32614/RJ-2021-039>

**Examples**

```
# Convert depth rank record to a discrete proxy record to allow for further
# analysis in which discrete time series are needed
depth_rank_example_disc <- lithlog_disc(litholog = depth_rank_example,
  subset_fact = 10,
  genplot = FALSE,
  x_lab = "rank",
  y_lab = "depth (m)",
  keep_editable=FALSE)
```

---

loess\_auto

*Perform an automatically loess based smoothing of a time series*


---

**Description**

Perform an automatically loess based smoothing of a time series. The local polynomial regression with automatic smoothing parameter selection is based on an optimization using the 'aicc' bias-corrected 'AIC' criterion and the 'gcv' generalized cross-validation criterion.

**Usage**

```
loess_auto(
  time_series = NULL,
  genplot = FALSE,
  print_span = FALSE,
  keep_editable = FALSE
)
```

**Arguments**

time_series	Input is a time series with the first column being depth or time and the second column being a proxy
genplot	Option to generate plot Default=TRUE. The plot will consist of the original signal in blue, the smoothed plot is displayed in black and the + and - 1 sd bounds of the smoothing are displayed in red.
print_span	Print span length as a fraction of the total length of the record.
keep_editable	Keep option to add extra features after plotting Default=FALSE

**Value**

A matrix with 3 columns. The first column is depth/time. The second column is the smoothed curve. The third column is difference between the original curve and the smoothed curve.

**Author(s)**

Based on the the [loess.as](#) function of the 'fANCOVA' R package.

## References

Cleveland, W. S. (1979) Robust locally weighted regression and smoothing scatter plots. *Journal of the American Statistical Association*. 74, 829–836. <doi:10.1080/01621459.1979.10481038> Hurvich, C.M., Simonoff, J.S., and Tsai, C.L. (1998), Smoothing Parameter Selection in Nonparametric Regression Using an Improved Akaike Information Criterion. *Journal of the Royal Statistical Society B*. 60, 271–293 <doi:10.1111/1467-9868.00125> Golub, G., Heath, M. and Wahba, G. (1979). Generalized cross validation as a method for choosing a good ridge parameter. *Technometrics*. 21, 215–224. <doi:10.2307/1268518>

## Examples

```
#'smooth the period curve of the 405 kyr eccentricity cycle extracted from
# the magnetic susceptibility data set of Pas et al., (2018)
#perform the CWT on the magnetic susceptibility data set of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set mag_track_solution is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = FALSE,
  keep_editable=FALSE
)

#Smooth the completed tracking of the 405 kyr eccentricity cycle as tracked in the wavelet spectra
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE,keep_editable=FALSE)
```

---

mag	<i>Magnetic susceptibility data of the Sullivan core of Pas et al., (2018)</i>
-----	--

---

### Description

The magnetic susceptibility data set consists of the magnetic susceptibility measurements of Pas et al., (2018), which measured the magnetic susceptibility on the Sullivan core which is of Famennian age.

### Details

Column 1: depth value (meters depth)  
 Column 2: magnetic susceptibility value

### References

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488, 2018, Pages 102-114, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>

---

mag_track_solution	<i>Period of the 405 kyr ecc cycle in the magnetic susceptibility record of the Sullivan core</i>
--------------------	---

---

### Description

Data points which give the period (in meters) of the 405 kyr eccentricity cycle tracked in the wavelet scalogram of the magnetic susceptibility record of the Sullivan core  
 The period was tracked using the [track\\_period\\_wavelet](#) function  
 The tracking is based on the original age model of Pas et al., (2018)

### Details

Column 1: Depth (meters)  
 Column 2: tracked period of 405 kyr eccentricity cycle (meters)

### References

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488, 2018, Pages 102-114, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>

---

max_detect	<i>Detect and filter out all maxima in a signal</i>
------------	---

---

### Description

The `max_detect` function is used to detect and filter out local maxima in a sinusoidal signal.

### Usage

```
max_detect(data = NULL, pts)
```

### Arguments

data	Matrix or data frame with the first column being depth or time and the second column being a proxy
pts	The pts parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the pts parameter can be changed which can aid in peak detection. Usually increasing the pts parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=3

### Value

#Returns a matrix with 2 columns first column is depth/time the second column are local maxima values

### Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar  
#Irradiance data set of Steinhilber et al., (2012)  
#after which all maxima are extracted
```

```
TSI_wt <-  
analyze_wavelet(  
  data = TSI,  
  dj = 1/200,  
  lowerPeriod = 16,  
  upperPeriod = 8192,  
  verbose = FALSE,  
  omega_nr = 6  
)
```

```
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,  
  cycle=210,  
  period_up = 1.25,  
  period_down = 0.75,  
  add_mean=TRUE,
```

```

plot_residual=FALSE)

min_de_Vries_cycle <- min_detect(de_Vries_cycle)

```

---

minimal_tuning	<i>Create an age model using minimal tuning</i>
----------------	---

---

### Description

Create an age model using the minimal tuning technique. This means that the distance between 2 peaks of an extracted cycle are set to duration of the interpreted astronomical cycle

### Usage

```

minimal_tuning(
  data = NULL,
  pts = 5,
  cycle = 405,
  tune_opt = "max",
  output = 0,
  genplot = FALSE,
  keep_editable = FALSE
)

```

### Arguments

data	Input is an cycle extracted filtered in the depth domain
pts	The pts parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the pts parameter can be changed which can aid in peak detection. Usually increasing the pts parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=5
cycle	duration in kyr of the filtered/extracted cycle
tune_opt	tuning options "min", "max" and "minmax" use minima, maxima or both of the cyclic signal to create the age model Default="max"
output	#The output depends on the output setting If output = 0 output is a matrix of with 4 columns being; depth,proxy,sedimentation rate and time If output = 1 output is a matrix of with 2 columns being; depth and sedimentation rate #If output = 2 output is a matrix of with 2 columns being; depth and time
genplot	Keep option to add extra features after plotting Default=FALSE
keep_editable	Keep option to add extra features after plotting Default=FALSE

**Value**

The output depends on the output setting. If `output = 0` output is a matrix of with 4 columns being (depth, proxy, sedimentation rate and time). If `genplot = TRUE` 4 plots are generated; depth vs proxy, depth vs sedimentation rate, depth vs time and time vs proxy. If `output = 1` output is a matrix of with 2 columns being (depth and sedimentation rate). If `genplot = TRUE` a plot of depth vs sedimentation rate is generated. If `output = 2` output is a matrix of with 2 columns being (depth and time). If `genplot = TRUE` a plot of depth vs time is generated.

**Author(s)**

Part of the code is based on the [sedrate2time](#) function of the 'astrochron' R package

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

**Examples**

```
# Extract the 405kyr eccentricity cycle from the wavelet scalogram
# from the magnetic susceptibility record f the Sullivan core
# of Pas et al., (2018) and then create a age model using minimal tuning
# (e.g.) set the distance between peaks to 405 kyr
```

```
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)
```

```
mag_405 <- extract_signal_stable_V2(
  wavelet = mag_wt,
  period_max = 4,
  period_min = 2,
  add_mean = FALSE,
  plot_residual = FALSE,
  keep_editable = FALSE
)
```

```
mag_405_min_tuning <- minimal_tuning(data = mag_405,
  pts = 5,
  cycle = 405,
  tune_opt = "max",
  output = 0,
  genplot = FALSE,
  keep_editable = FALSE)
```

---

min_detect	<i>Detect and filter out all minima in a signal</i>
------------	---

---

### Description

The `min_detect` function is used to detect and filter out local minima in a sinusoidal signal

### Usage

```
min_detect(data = NULL, pts = 3)
```

### Arguments

<code>data</code>	Matrix or data frame with first column being depth or time and the second column being a proxy
<code>pts</code>	the <code>pts</code> parameter specifies how many points to the left/right up/down the peak detect algorithm goes in detecting a peak. The peak detecting algorithm works by comparing the values left/right up/down of it, if the values are both higher or lower then the value a peak. To deal with error produced by this algorithm the <code>pts</code> parameter can be changed which can aid in peak detection. Usually increasing the <code>pts</code> parameter means more peak certainty, however it also means that minor peaks might not be picked up by the algorithm Default=3

### Value

#Returns a matrix with 2 columns first column is depth/time the second column are local minima values

### Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar
#Irradiance data set of Steinhilber et al., (2012)
#after which all minima are extracted
```

```
TSI_wt <-
analyze_wavelet(
data = TSI,
dj = 1/200,
lowerPeriod = 16,
upperPeriod = 8192,
  verbose = FALSE,
  omega_nr = 6
)
```

```
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
cycle=210,
period_up =1.25,
```



```
period_down = 0.75,  
add_mean=TRUE,  
plot_residual=FALSE)  
  
min_de_Vries_cycle <- min_detect(de_Vries_cycle)
```

---

model\_red\_noise\_wt     *Models average spectral power based curves based on a red-noise signal generated using the characteristics of an input signal.*

---

### Description

The `model_red_noise_wt` function is used to generate average spectral power curves based on and input signal and set wavelet settings.

### Usage

```
model_red_noise_wt(  
  wavelet = NULL,  
  n_simulations = NULL,  
  run_multicore = FALSE,  
  verbose = FALSE  
)
```

### Arguments

<code>wavelet</code>	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
<code>n_simulations</code>	Number of red noise simulations.
<code>run_multicore</code>	run simulation using multiple cores Default=FALSE the simulation is run at x-2 cores to allow the 2 remaining processes to run background processes.
<code>verbose</code>	Print text Default=FALSE.

### Value

Returns a matrix in which each column represents the average spectral power resulting from a red-noise run.

### Author(s)

Code based on the [analyze\\_wavelet](#) function of the 'WaveletComp' R package and `wt` function of the 'biwavelet' R package which are based on the wavelet 'MATLAB' code written by Christopher Torrence and Gilbert P. Compo (1998).

## References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
- Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)
- Morlet, Jean, Georges Arens, Eliane Fourceau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " Geophysics 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>
- J. Morlet, G. Arens, E. Fourceau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. Geophysics 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

## Examples

```
##generate average spectral power curves based on red noise curves which are
# based on the magnetic susceptibility record of the Sullivan core of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
  n_simulations=10, # increase number for better constrained results
  run_multicore=FALSE,
  verbose=FALSE)
```

---

percentile\_from\_red\_noise

*Calculate average spectral power from red noise curves for a given percentile*

---

## Description

The `percentile_from_red_noise` function is used to generate and average spectral power curve based on a set percentile based. To generate the percentile curve the results of the `model_red_noise_wt` function are used.

**Usage**

```
percentile_from_red_noise(red_noise = NULL, wavelet = NULL, percentile = NULL)
```

**Arguments**

red_noise	Red noise curves generated using the <a href="#">model_red_noise_wt</a> function.
wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
percentile	Percentile value (0-1).

**Value**

Returns a matrix with 2 columns.  
The first column is the period (m).  
The second column is the spectral power at percentile x based on the red noise modelling runs.

**Examples**

```
##generate average spectral power curves based on red noise curves which are
# based on the magnetic susceptibility record of the Sullivan core of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
  n_simulations=10, # Increase number for a better constrained result
  run_multicore=FALSE,
  verbose=FALSE)

prob_curve <- percentile_from_red_noise(
  red_noise = mag_wt_red_noise,
  wavelet = mag_wt,
  percentile = 0.9)
```

---

plot\_astro\_anchor      *Plot proxy record anchored to an astronomical solution*

---

### Description

Plot the results of the anchoring the extracted signal to an astronomical solution using which was conducted using the [astro\\_anchor](#)

### Usage

```
plot_astro_anchor(
  astro_solution = NULL,
  proxy_signal = NULL,
  anchor_points = NULL,
  time_dir = TRUE,
  keep_editable = FALSE
)
```

### Arguments

astro_solution	Input is an astronomical solution with which the proxy record was anchored to, the input should be a matrix or data frame with the first column being age and the second column should be a insolation/angle/value
proxy_signal	Input is the proxy data set which was anchored to an astronomical solution, the input should be a matrix or data frame with the first column being depth/time and the second column should be a proxy value.
anchor_points	Anchor points generated using the <a href="#">astro_anchor</a> function
time_dir	The direction of the proxy record which was assumed during anchoring if time increases with increasing depth/time values (e.g. bore hole data which gets older with increasing depth ) then time_dir should be set to TRUE if time decreases with depth/time values (eg stratospheric logs where 0m is the bottom of the section) then time_dir should be set to FALSE time_dir=TRUE
keep_editable	Keep option to add extra features after plotting Default=FALSE

### Value

The output is a set of 2 plots connected by lines The top plot is the proxy record with anchor points on top of it The bottom plot is the astronomical solution The lines connect the anchor points

### Examples

```
# Use the grey_track example tracking points to anchor the grey scale data set
# of Zeeden et al., (2013) to the p-0.5t la2004 solution

grey_wt <-
  analyze_wavelet(
    data = grey,
```

```
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )

#Use the pretracked grey_track curve which traced the precession cycle
grey_track <- completed_series(
  wavelet = grey_wt,
  tracked_curve = grey_track,
  period_up = 1.25,
  period_down = 0.75,
  extrapolate = TRUE,
  genplot = FALSE
)
# Extract precession, obliquity and eccentricity to create a synthetic insolation curve

grey_prec <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 22,
  tune = FALSE,
  plot_residual = FALSE
)

grey_obl <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 110,
  tune = FALSE,
  plot_residual = FALSE
)

grey_ecc <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.25,
  period_down = 0.75,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 40.8,
  tune = FALSE,
  plot_residual = FALSE
)
```

```

insolation_extract <- cbind(grey_ecc[,1],grey_prec[,2]+grey_obl[,2]+grey_ecc[,2]+mean(grey[,2]))
insolation_extract <- as.data.frame(insolation_extract)
insolation_extract_mins <- min_detect(insolation_extract,pts=3)

#use the astrosignal_example to tune to which is an \cr
# ETP solution (p-0.5t la2004 solution).

astrosignal_example <- na.omit(astrosignal_example)
astrosignal_example[,2] <- -1*astrosignal_example[,2]
astrosignal <- as.data.frame(astrosignal_example)

#anchor the synthetic insolation curve extracted from the
# grey scale record to the insolation curve.
#use the anchor_points_grey data set to plot the
#result of using the astro_anchor function

#anchor_points_grey <- astro_anchor(
#astro_solution = astrosignal,
#proxy_signal = insolation_extract,
#proxy_min_or_max = "min",
#clip_astrosolution = FALSE,
#astrosolution_min_or_max = "min",
#clip_high = NULL,
#clip_low = NULL,
#extract_astrosolution = FALSE,
#astro_period_up = NULL,
#astro_period_down = NULL,
#astro_period_cycle = NULL,
#extract_proxy_signal = FALSE,
#proxy_period_up = NULL,
#proxy_period_down = NULL,
#proxy_period_cycle = NULL,
#pts=3,
#verbose=FALSE,
#genplot=FALSE # set verbose to TRUE to allow for anchoring using text feedback commands
#)

plot_astro_anchor(astro_solution = astrosignal,
proxy_signal = insolation_extract,
anchor_points = anchor_points_grey,
time_dir = FALSE,
keep_editable = FALSE)

```

**Description**

Plot the average spectral power of a wavelet spectra using the results of the [analyze\\_wavelet](#) function.

**Usage**

```
plot_avg_wavelet(  
  wavelet = NULL,  
  y_lab = "Power",  
  x_lab = "period (metres)",  
  keep_editable = FALSE  
)
```

**Arguments**

wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
y_lab	Label for the y-axis Default="Power".
x_lab	Label for the x-axis Default="depth (metres)".
keep_editable	Keep option to add extra features after plotting Default=FALSE

**Value**

The output is a plot of the average spectral power of a wavelet spectra

**Examples**

```
#Example 1. Plot the average spectral power of the wavelet spectra of  
# the Total Solar Irradiance data set of Steinhilber et al., (2012)  
TSI_wt <-  
  analyze_wavelet(  
    data = TSI,  
    dj = 1/200,  
    lowerPeriod = 16,  
    upperPeriod = 8192,  
    verbose = FALSE,  
    omega_nr = 6  
  )  
  
plot_avg_wavelet(wavelet=TSI_wt,  
  y_lab= "power",  
  x_lab="period (years)",  
  keep_editable=FALSE)  
  
#Example 2. Plot the average spectral power of the wavelet spectra of \cr  
# the magnetic susceptibility data set of Pas et al., (2018)  
mag_wt <-  
  analyze_wavelet(  
    data = mag,  
    dj = 1/100,
```

```

lowerPeriod = 0.1,
upperPeriod = 254,
verbose = FALSE,
omega_nr = 10
)
plot_avg_wavelet(wavelet=mag_wt,
                 y_lab= "power",
                 x_lab="period (metres)",
                 keep_editable=FALSE)

#Example 3. Plot the average spectral power of the wavelet spectra of
#the greyscale data set of Zeeden et al., (2013)
grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )

plot_avg_wavelet(wavelet=grey_wt,
                 y_lab= "power",
                 x_lab="period (metres)",
                 keep_editable=FALSE)

```

---

plot\_sed\_model

*Plot sedimentation modelling results*


---

### Description

The `plot_sed_model` function is used plot/re-plot the results from the `flmw` and `sum_power_sedrate` functions

### Usage

```

plot_sed_model(
  model_results = NULL,
  plot_res = 1,
  x_lab = "depth (m)",
  y_lab = "sed rate cm/kyr",
  keep_editable = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices"
)

```



**Arguments**

model_results	Wavelet object created using the <a href="#">analyze_wavelet</a> function
plot_res	Numbers to be used as input form the <a href="#">flmw</a> output options 1-8 option 1: slope coefficient, option 2: r squared, option 3: nr of components, option 4: difference to origin, option 5: slope coefficient percentile option 6: r squared percentile, option 7: nr of components percentile, option 8: difference to origin percentile. If the output of the <a href="#">sum_power_sedrate</a> function is used then input should be option 1: sum max power option 2: nr of components
x_lab	Label for x-axis Default="depth (m)"
y_lab	Label for y-axis Default="sed rate cm/kyr"
keep_editable	Keep option to add extra features after plotting Default=FALSE
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices

**Value**

Returns a plot of sedimentation rates vs depth and a value which was generated using the [flmw](#) or [sum\\_power\\_sedrate](#) functions

**Examples**

```
#estimate sedimentation rate for the the magnetic susceptibility record
# of the Sullivan core of Pas et al., (2018).
```

```
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)
```

```

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
n_simulations=10, # increase for a better constrained result
run_multicore=FALSE,
verbose=FALSE)

sedrates <- sum_power_sedrate(red_noise=mag_wt_red_noise,
wavelet=mag_wt,
percentile=0.75,
sedrate_low = 0.5,
sedrate_high = 4,
spacing = 0.05,
cycles = c(2376,1600,1180,696,406,110),
x_lab="depth",
y_lab="sedrate",
run_multicore=FALSE,
genplot = FALSE,
palette_name = "rainbow",
color_brewer= "grDevices",
verbose=FALSE)

plot_sed_model(model_results=sedrates,
plot_res=1,
x_lab = "depth (m)",
y_lab = "sed rate cm/kyr",
keep_editable=FALSE,
palette_name = "rainbow",
color_brewer= "grDevices")

```

---

plot\_wavelet

*Plots a wavelet power spectra*


---

### Description

Plot wavelet spectra using the outcome of the [analyze\\_wavelet](#) function.

### Usage

```

plot_wavelet(
  wavelet = NULL,
  lowerPeriod = NULL,
  upperPeriod = NULL,
  plot.COI = TRUE,
  n.levels = 100,
  palette_name = "rainbow",
  color_brewer = "grDevices",

```

```

useRaster = TRUE,
periodlab = "Period (metres)",
x_lab = "depth (metres)",
keep_editable = FALSE,
dev_new = TRUE,
plot_dir = TRUE,
add_lines = NULL,
add_points = NULL,
add_abline_h = NULL,
add_abline_v = NULL,
add_MTM_peaks = FALSE,
add_data = TRUE,
add_avg = FALSE,
add_MTM = FALSE,
siglvl = 0.95,
demean_mtm = TRUE,
detrend_mtm = TRUE,
padfac_mtm = 5,
tbw_mtm = 3,
plot_horizontal = TRUE
)

```

### Arguments

wavelet	wavelet object created using the <a href="#">analyze_wavelet</a> function.
lowerPeriod	Lowest period value which will be plotted
upperPeriod	Highest period value which will be plotted
plot.COI	Option to plot the cone of influence Default=TRUE.
n.levels	Number of color levels Default=100.
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices

useRaster	Plot as a raster or vector image Default=TRUE. WARNING plotting as a vector image is computationally intensive.
periodlab	Label for the y-axis Default="Period (metres)".
x_lab	Label for the x-axis Default="depth (metres)".
keep_editable	Keep option to add extra features after plotting Default=FALSE
dev_new	Opens a new plotting window to plot the plot, this guarantees a "nice" looking plot however when plotting in an R markdown document the plot might not plot Default=TRUE
plot_dir	The direction of the proxy record which is assumed for tuning if time increases with increasing depth/time values (e.g. bore hole data which gets older with increasing depth ) then plot_dir should be set to TRUE if time decreases with depth/time values (eg stratospheric logs where 0m is the bottom of the section) then plot_dir should be set to FALSE plot_dir=TRUE
add_lines	Add lines to the wavelet plot input should be matrix with first axis being depth/time the columns after that should be period values Default=NULL
add_points	Add points to the wavelet plot input should be matrix with first axis being depth/time and columns after that should be period values Default=NULL
add_abline_h	Add horizontal lines to the plot. Specify the lines as a vector e.g. c(2,3,5,6) Default=NULL
add_abline_v	Add vertical lines to the plot. Specify the lines as a vector e.g. c(2,3,5,6) Default=NULL
add_MTM_peaks	Add the MTM peak periods as horizontal lines Default=FALSE
add_data	Plot the data on top of the wavelet Default=TRUE
add_avg	Plot the average wavelet spectral power to the side of the wavelet Default=FALSE
add_MTM	Add the MTM plot next to the wavelet plot Default=FALSE
siglvl	Set the significance level for the MTM analysis (0-1) Default=0.95
demean_mtm	Remove mean from data before conducting the MTM analysis Default=TRUE
detrend_mtm	Remove mean from data before conducting the MTM analysis Default=TRUE
padfac_mtm	Pad factor for the MTM analysis Default=5
tbw_mtm	time bandwidth product of the MTM analysis Default=3
plot_horizontal	plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default=TRUE

### Value

The output is a plot of a wavelet spectra. if add\_MTM\_peaks = TRUE then the output of the MTM analysis will given as matrix

### Author(s)

Code based on the [analyze.wavelet](#) and [wt.image](#) functions of the 'WaveletComp' R package and [wt](#) function of the 'biwavelet' R package which are based on the wavelet MATLAB code written by Christopher Torrence and Gibert P. Compo (1998). The MTM analysis is from the astrochron R package of Meyers et al., (2012)

## References

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- J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. Geophysics 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>
- S.R. Meyers, 2012, Seeing Red in Cyclic Stratigraphy: Spectral Noise Estimation for Astrochronology: Paleocyanography, 27, PA3228, <doi:10.1029/2012PA002307>

## Examples

```
#Example 1. A plot of a wavelet spectra using the Total Solar Irradiance
# data set of Steinhilber et al., (2012)
```

```
TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = FALSE,
    omega_nr = 6
  )

plot_wavelet(
  wavelet = TSI_wt,
  lowerPeriod = NULL,
  upperPeriod = NULL,
  plot.COI = TRUE,
  n.levels = 100,
  palette_name = "rainbow",
  color_brewer= "grDevices",
  useRaster = TRUE,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)",
  keep_editable = FALSE,
  dev_new=TRUE,
  plot_dir = TRUE,
  add_lines = NULL,
  add_points= NULL,
```

```
add_abline_h = NULL,  
add_abline_v = NULL,  
add_MTM_peaks = FALSE,  
add_data = TRUE,  
add_avg = TRUE,  
add_MTM = FALSE,  
siglvl = 0.95,  
demean_mtm = TRUE,  
detrend_mtm = TRUE,  
padfac_mtm = 5,  
tbw_mtm = 3,  
plot_horizontal=TRUE)
```

```
#Example 2. A plot of a wavelet spectra using the magnetic susceptibility  
#data set of Pas et al., (2018)
```

```
mag_wt <-
```

```
analyze_wavelet(  
data = mag,  
dj = 1/100,  
lowerPeriod = 0.1,  
upperPeriod = 254,  
verbose = FALSE,  
omega_nr = 10  
)
```

```
plot_wavelet(  
wavelet = mag_wt,  
lowerPeriod = NULL,  
upperPeriod = NULL,  
plot.COI = TRUE,  
n.levels = 100,  
palette_name = "rainbow",  
color_brewer= "grDevices",  
useRaster = TRUE,  
periodlab = "Period (metres)",  
x_lab = "depth (metres)",  
keep_editable = FALSE,  
dev_new=TRUE,  
plot_dir = TRUE,  
add_lines= NULL,  
add_points= NULL,  
add_abline_h = NULL,  
add_abline_v = NULL,  
add_MTM_peaks = FALSE,  
add_data = TRUE,  
add_avg = TRUE,  
add_MTM = FALSE,  
siglvl = 0.95,  
demean_mtm = TRUE,  
detrend_mtm = TRUE,  
padfac_mtm = 5,  
tbw_mtm = 3,  
plot_horizontal=TRUE)
```

```
#Example 3. A plot of a wavelet spectra using the greyscale
# data set of Zeeden et al., (2013)
grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = FALSE,
    omega_nr = 8
  )

plot_wavelet(
  wavelet = grey_wt,
  lowerPeriod = NULL,
  upperPeriod = NULL,
  plot.COI = TRUE,
  n.levels = 100,
  palette_name = "rainbow",
  color_brewer= "grDevices",
  useRaster = TRUE,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)",
  keep_editable = FALSE,
  dev_new=TRUE,
  plot_dir = TRUE,
  add_lines = NULL,
  add_points= NULL,
  add_abline_h = NULL,
  add_abline_v = NULL,
  add_MTM_peaks = FALSE,
  add_data = TRUE,
  add_avg = TRUE,
  add_MTM = FALSE,
  siglvl = 0.95,
  demean_mtm = TRUE,
  detrend_mtm = TRUE,
  padfac_mtm = 5,
  tbw_mtm = 3,
  plot_horizontal=TRUE)

```

---

plot\_win\_fft

*Plot windowed fft based spectral analysis results*

---

### **Description**

The `plot_win_fft` function allows for the (re)plotting of the results of the `win_fft`

**Usage**

```
plot_win_fft(
  win_fft = NULL,
  x_lab = c("depth (m)"),
  y_lab = c("frequency cycle/metre"),
  plot_res = 1,
  perc_vis = 0,
  freq_max = NULL,
  freq_min = NULL,
  keep_editable = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices",
  plot_horizontal = TRUE,
  dev_new = TRUE
)
```

**Arguments**

win_fft	list which is the results of the <a href="#">win_fft</a>
x_lab	label for the x-axis Default="depth"
y_lab	label for the y-axis Default="sedrate"
plot_res	plot 1 of 8 options option 1: Amplitude matrix, option 2: Power matrix, option 3: Phase matrix, option 4: AR1_CL matrix, option 5: AR1_Fit matrix, option 6: AR1_90_power matrix, option 7: AR1_95_power matrix, option 8: AR1_99_power matrix, Default=1
perc_vis	Cutoff percentile when plotting Default=0
freq_max	Maximum frequency to plot
freq_min	Minimum frequency to plot
keep_editable	Keep option to add extra features after plotting Default=FALSE
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer,



grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices"

plot\_horizontal  
plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default=TRUE

dev\_new  
Opens a new plotting window to plot the plot, this guarantees a "nice" looking plot however when plotting in an R markdown document the plot might not plot Default=TRUE

### Value

Returns a plot of, which plot 1 of 8 options, option 1: Amplitude matrix option 2: Power matrix option 3: Phase matrix option 4: AR1\_CL matrix option 5: AR1\_Fit matrix option 6: AR1\_90\_power matrix option 7: AR1\_95\_power matrix option 8: AR1\_99\_power matrix

### Examples

```
#Conduct a windowed fft on the magnetic susceptibility record \cr
# of the Sullivan core of Pas et al., (2018).
```

```
mag_win_fft <- win_fft(data= mag,
  padfac = 5,
  window_size = 12.5,
  run_multicore = FALSE,
  genplot = FALSE,
  palette_name = "rainbow",
  color_brewer="grDevices",
  x_lab = c("depth (m)"),
  y_lab = c("frequency cycle/meter"),
  plot_res = 1,
  perc_vis = 0.5,
  freq_max = 5,
  freq_min = 0.001,
  keep_editable=FALSE,
  verbose=FALSE)
```

```
# Plot the amplitude spectra
plot_win_fft(win_fft= mag_win_fft,
  x_lab = c("depth (m)"),
  y_lab = c("frequency cycle/meter"),
  plot_res = 1,
  perc_vis = 0.5,
  freq_max = 5,
  freq_min = 0.001,
  keep_editable=FALSE,
  palette_name = "rainbow",
  color_brewer="grDevices",
  plot_horizontal=TRUE,
  dev_new=TRUE)
```

---

`retrack_wt_MC`*Re-track cycles using a Monte-Carlo simulation*

---

### Description

When analyzing multi-proxy records an age-model can be created for each proxy. These age-models can be in general agreement but might also indicate conflicting deposition rates. Picking one age-model out of the all multi-proxy age-models and stating that, that age-model is the best overlooks the information contained within the other proxies and hence a degree of error remains the age-model exists. To combine the multiple age-models all the age models can be averaged out and the uncertainty can be calculated by means of the standard deviation. The result is an age-model which takes into account all the age-models from the proxy records. The averaged out age-model does not take into account any small user errors during the creation of the individual age-models nor does the averaging take into account the differences between the age-models and how the initial age-model of a certain proxy might be off in certain intervals. The link[WaverideR]retrack\_wt\_MC mitigates these problems by re-tracking periods of astronomical cycles in the wavelet spectra. The re-tracking is based on the information provided by the age-models constructed from the different proxy records. First a synthetic tracked curve is created by adding up fractions (0-1) of the tracked periods of the different proxy records. This synthetic curve is then used to re-track the period/spectral peaks of an astronomical cycle in a randomly select wavelet scalogram. This process is repeated  $x$  times. The result  $x$  tracked curves which take into account all the original age-models. From the re-tracked curves one can calculate the mean period and the standard deviation. The resulting standard deviation is a good indicator of the quality of the imprint of of astronomical cycles in the proxy records. A small standard deviation indicates that given the input of the different tracked cycles similar periods keep on being tracked indicating the an astronomical is well recorded in the proxy records and as such the age-model is very reliable in set interval. A high standard deviation on the other hand means that the tracking results in vastly different periods of the tracked astronomical cycle, as such the quality of the imprint of the astronomical cycle proxy records is poor and hence the age-model is less-reliable in this interval.

### Usage

```
retrack_wt_MC(  
  wt_list = NULL,  
  data_track = NULL,  
  x_axis = NULL,  
  nr_simulations = 50,  
  seed_nr = 1337,  
  verbose = FALSE,  
  genplot = FALSE,  
  keep_editable = FALSE,  
  create_GIF = FALSE,  
  plot_GIF = FALSE,  
  width_plt = 600,  
  height_plt = 450,  
  period_up = 1.5,  
  period_down = 0.5,
```

```

plot.COI = TRUE,
n.levels = 100,
palette_name = "rainbow",
color_brewer = "grDevices",
periodlab = "Period (metres)",
x_lab = "depth (metres)",
add_avg = FALSE,
time_dir = TRUE,
file_name = NULL,
run_multicore = FALSE,
output = 1,
n_imgs = 50,
plot_horizontal = TRUE,
empty_folder = FALSE
)

```

### Arguments

wt_list	a list containing all the wavelet objects created using the link[WaverideR]analyze_wavelet wavelet function To create a list use the link[base]list function
data_track	a matrix containing all the tracked period values. To create the matrix use the link[base]cbind function and only add the tracked period values so do not add the depth axis. When combining the tracked period values make sure that all curves have a similar depth spacing.
x_axis	The x-axis of the tracked period values
nr_simulations	The number of Monte-Carlo simulations which are to be conducted Default=50
seed_nr	The seed number of the Monte-Carlo simulations. Default=1337
verbose	Print text when running the function Default=FALSE
genplot	Plot a plot with the mean period and + and - standard deviation Default=FALSE
keep_editable	Keep option to add extra features after plotting Default=FALSE
create_GIF	Create a GIF with the re-tracked lines in the wavelet scalograms Default=FALSE
plot_GIF	Plot a GIF with the re-tracked lines in the wavelet scalograms Default=FALSE
width_plt	width of the re-tracked plot Default=600
height_plt	width of the re-tracked plot Default=450
period_up	The period_up parameter is the factor with which the linear interpolated tracked_curve curve is multiplied by. This linear interpolated tracked_curve multiplied by the period_up factor is the upper boundary which is used for detecting the spectral peak nearest to the linear interpolated tracked_curve curve. If no spectral peak is detected within the specified boundary the interpolated value is used instead. between spectral peaks Default=1.5,
period_down	The period_down parameter is the factor with which the linear interpolated tracked_curve curve is multiplied by. This linear interpolated tracked_curve multiplied by the period_down factor is the lower boundary which is used for detecting the spectral peak nearest to the linear interpolated tracked_curve curve. If no spectral peak is detected within the specified boundary the interpolated value is used instead. between spectral peaks Default=0.5,

plot.COI	Option to plot the cone of influence Default=TRUE.
n.levels	Number of color levels Default=100.
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices
periodlab	Label for the y-axis Default="Period (metres)".
x_lab	Label for the x-axis Default="depth (metres)".
add_avg	Plot the average wavelet spectral power to the side of the wavelet Default=FALSE
time_dir	The direction of the proxy record which is assumed for tuning if time increases with increasing depth/time values (e.g. bore hole data which gets older with increasing depth ) then time_dir should be set to TRUE if time decreases with depth/time values (eg stratospheric logs where 0m is the bottom of the section) then time_dir should be set to FALSE time_dir=TRUE
file_name	Name of the images created using this function. Each file gets a number added to it which corresponds to which number of simulation it was the files are saved in a folder with a similar name created in the current directory
run_multicore	Run function using multiple cores Default="FALSE"
output	#'If output = 1, output is a list which contain 3 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. #'object 2 is a matrix with all the tracked periods. Object 3 is a GIF in which #'all the tracked periods are plotted. If output = 2, output is a list which contain 2 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. object 2 is a matrix with all the tracked periods. If output = 3, output is a list which contain 2 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. Object 2 is a GIF in which all the tracked periods are plotted. If output = 4, output is a list which contain 3 objects. Object 1 is a matrix with all the tracked periods. Object 2 is a GIF in which all the tracked periods are plotted. If output = 4 output is a list which contain 3 objects. Object 1 is a matrix with all the tracked periods. Object 2 is a GIF in which all the tracked periods are plotted. If output = 5 a matrix with

	the x-axis and the mean tracked frequency and standard deviation is returned. If output = 6, a matrix with all the tracked periods is returned. If output = 7, a GIF in which all the tracked periods are plotted is returned. Default=1
n_imgs	Number images used in creating the GIF a high number of images is computationally intensive and will create a large sized GIF Default=50
plot_horizontal	plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default=TRUE
empty_folder	Empty the folder in which the images created using this function are saved Default=FALSE

### Value

The output depends on the output setting If `genplot = TRUE` a plot will be generated in which the mean period and standard deviation is plotted if `plot_GIF = TRUE` a GIF with n number of `n_imgs` will be plotted in which the retraced curve is plotted in a wavelet scalogram If `output = 1`, output is a list which contain 3 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. object 2 is a matrix with all the tracked periods. Object 3 is a GIF in which all the tracked periods are plotted. If `output = 2`, output is a list which contain 2 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. object 2 is a matrix with all the tracked periods. If `output = 3`, output is a list which contain 2 objects. object 1 is a matrix with the x-axis and the mean tracked frequency and standard deviation. Object 2 is a GIF in which all the tracked periods are plotted. If `output = 4`, output is a list which contain 3 objects. Object 1 is a matrix with all the tracked periods. Object 2 is a GIF in which all the tracked periods are plotted. If `output = 4` output is a list which contain 3 objects. Object 1 is a matrix with all the tracked periods. Object 2 is a GIF in which all the tracked periods are plotted. If `output = 5` a matrix with the x-axis and the mean tracked period and standard deviation is returned. If `output = 6`, a matrix with all the tracked periods is returned. If `output = 7`, a GIF in which all the tracked periods are plotted is returned

### Examples

```
# Re-track the 110kyr eccentricity cycle in the wavelet scalogram
# from the XRF record of the Bisciaro data set of Arts (2014)

Bisciaro_al <- Bisciaro_XRF[, c(1, 61)]
Bisciaro_al <- astrochron::sortNave(Bisciaro_al, verbose=FALSE, genplot=FALSE)
Bisciaro_al <- astrochron::linterp(Bisciaro_al, dt = 0.01, verbose=FALSE, genplot=FALSE)
Bisciaro_al <- Bisciaro_al[Bisciaro_al[, 1] > 2, ]

Bisciaro_al_wt <-
  analyze_wavelet(
    data = Bisciaro_al,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_al_wt_track <-
```

```

# track_period_wavelet(
#   astro_cycle = 110,
#   wavelet = Bisciaro_al_wt,
#   n.levels = 100,
#   periodlab = "Period (metres)",
#   x_lab = "depth (metres)"
# )
#
# Bisciaro_al_wt_track <- completed_series(
#   wavelet = Bisciaro_al_wt,
#   tracked_curve = Bisciaro_al_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_al_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_al_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciaro_ca <- Bisciaro_XRF[, c(1, 55)]
Bisciaro_ca <- astrochron::sortNave(Bisciaro_ca, verbose=FALSE, genplot=FALSE)
Bisciaro_ca <- astrochron::linterp(Bisciaro_ca, dt = 0.01, verbose=FALSE, genplot=FALSE)
Bisciaro_ca <- Bisciaro_ca[Bisciaro_ca[, 1] > 2, ]

Bisciaro_ca_wt <-
  analyze_wavelet(
    data = Bisciaro_ca,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_ca_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_ca_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
# Bisciaro_ca_wt_track <- completed_series(
#   wavelet = Bisciaro_ca_wt,
#   tracked_curve = Bisciaro_ca_wt_track,

```

```

# period_up = 1.2,
# period_down = 0.8,
# extrapolate = TRUE,
# genplot = FALSE,
# keep_editable = FALSE
# )
#
# Bisciaro_ca_wt_track <-
# loess_auto(
#   time_series = Bisciaro_ca_wt_track,
#   genplot = FALSE,
#   print_span = FALSE,
#   keep_editable = FALSE)

Bisciaro_sial <- Bisciaro_XRF[,c(1,64)]
Bisciaro_sial <- astrochron::sortNave(Bisciaro_sial,verbose=FALSE,genplot=FALSE)
Bisciaro_sial <- astrochron::linterp(Bisciaro_sial, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_sial <- Bisciaro_sial[Bisciaro_sial[, 1] > 2, ]

Bisciaro_sial_wt <-
analyze_wavelet(
  data = Bisciaro_sial,
  dj = 1 /200 ,
  lowerPeriod = 0.01,
  upperPeriod = 50,
  verbose = FALSE,
  omega_nr = 8
)

# Bisciaro_sial_wt_track <-
# track_period_wavelet(
#   astro_cycle = 110,
#   wavelet = Bisciaro_sial_wt,
#   n.levels = 100,
#   periodlab = "Period (metres)",
#   x_lab = "depth (metres)"
# )
#
#
# Bisciaro_sial_wt_track <- completed_series(
#   wavelet = Bisciaro_sial_wt,
#   tracked_curve = Bisciaro_sial_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_sial_wt_track <-
# loess_auto(
#   time_series = Bisciaro_sial_wt_track,
#   genplot = FALSE,

```

```

#   print_span = FALSE,
#   keep_editable = FALSE
# )

Bisciaro_Mn <- Bisciaro_XRF[,c(1,46)]
Bisciaro_Mn <- astrochron::sortNave(Bisciaro_Mn,verbose=FALSE,genplot=FALSE)
Bisciaro_Mn <- astrochron::linterp(Bisciaro_Mn, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_Mn <- Bisciaro_Mn[Bisciaro_Mn[, 1] > 2, ]

Bisciaro_Mn_wt <-
  analyze_wavelet(
    data = Bisciaro_Mn,
    dj = 1 / 200 ,
    lowerPeriod = 0.01,
    upperPeriod = 50,
    verbose = FALSE,
    omega_nr = 8
  )

# Bisciaro_Mn_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_Mn_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciaro_Mn_wt_track <- completed_series(
#   wavelet = Bisciaro_Mn_wt,
#   tracked_curve = Bisciaro_Mn_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
# Bisciaro_Mn_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_Mn_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE
#   )

Bisciaro_Mg <- Bisciaro_XRF[,c(1,71)]
Bisciaro_Mg <- astrochron::sortNave(Bisciaro_Mg,verbose=FALSE,genplot=FALSE)
Bisciaro_Mg <- astrochron::linterp(Bisciaro_Mg, dt = 0.01,verbose=FALSE,genplot=FALSE)
Bisciaro_Mg <- Bisciaro_Mg[Bisciaro_Mg[, 1] > 2, ]

Bisciaro_Mg_wt <-

```



```

analyze_wavelet(
  data = Bisciaro_Mg,
  dj = 1 / 200 ,
  lowerPeriod = 0.01,
  upperPeriod = 50,
  verbose = FALSE,
  omega_nr = 8
)

# Bisciaro_Mg_wt_track <-
#   track_period_wavelet(
#     astro_cycle = 110,
#     wavelet = Bisciaro_Mg_wt,
#     n.levels = 100,
#     periodlab = "Period (metres)",
#     x_lab = "depth (metres)"
#   )
#
#
# Bisciaro_Mg_wt_track <- completed_series(
#   wavelet = Bisciaro_Mg_wt,
#   tracked_curve = Bisciaro_Mg_wt_track,
#   period_up = 1.2,
#   period_down = 0.8,
#   extrapolate = TRUE,
#   genplot = FALSE,
#   keep_editable = FALSE
# )
#
# Bisciaro_Mg_wt_track <-
#   loess_auto(
#     time_series = Bisciaro_Mg_wt_track,
#     genplot = FALSE,
#     print_span = FALSE,
#     keep_editable = FALSE)

wt_list_bisc <- list(Bisciaro_al_wt,
                    Bisciaro_ca_wt,
                    Bisciaro_sial_wt,
                    Bisciaro_Mn_wt,
                    Bisciaro_Mg_wt)

#Instead of tracking, the tracked solution data sets Bisciaro_al_wt_track,
#Bisciaro_ca_wt_track, Bisciaro_sial_wt_track, Bisciaro_Mn_wt_track,
# Bisciaro_Mn_wt_track and Bisciaro_Mg_wt_track are used

data_track_bisc <- cbind(Bisciaro_al_wt_track[,2],
                        Bisciaro_ca_wt_track[,2],
                        Bisciaro_sial_wt_track[,2],
                        Bisciaro_Mn_wt_track[,2],

```

```
Bisciaro_Mg_wt_track[,2])  
  
x_axis_bisc <- Bisciaro_al_wt_track[,1]  
  
bisc_retrack <- retrack_wt_MC(wt_list = wt_list_bisc,  
  data_track = data_track_bisc,  
  x_axis = x_axis_bisc,  
  nr_simulations = 20,  
  seed_nr = 1337,  
  verbose = FALSE,  
  genplot = FALSE,  
  keep_editable = FALSE,  
  create_GIF = FALSE,  
  plot_GIF = FALSE,  
  width_plt = 600,  
  height_plt = 450,  
  period_up = 1.5,  
  period_down = 0.5,  
  plot.COI = TRUE,  
  n.levels = 100,  
  palette_name = "rainbow",  
  color_brewer = "grDevices",  
  periodlab = "Period (metres)",  
  x_lab = "depth (metres)",  
  add_avg = FALSE,  
  time_dir = TRUE,  
  file_name = NULL,  
  run_multicore = FALSE,  
  output = 1,  
  n_imgs = 50,  
  plot_horizontal = TRUE,  
  empty_folder = FALSE)
```

---

sedrate2tune

*Use a sedimentation curve to convert data to the time domain*

---

### **Description**

Convert a proxy record from the depth to time domain using a sedimentation rate curve

### **Usage**

```
sedrate2tune(  
  data = NULL,  
  sed_curve = NULL,
```

```

    genplot = FALSE,
    keep_editable = FALSE
  )

```

### Arguments

data	Input should be a matrix of 2 columns with first column being depth and the second column is a proxy value
sed_curve	Input should be a matrix of 2 columns with first column being depth and the second column is the sedimentation rate is cm/kyr
genplot	Generates a plot of the proxy record in the time domain Default=FALSE.
keep_editable	Keep option to add extra features after plotting Default=FALSE

### Value

The output is a matrix with 2 columns. The first column is time The second column is the proxy value If genplot=TRUE then a time vs proxy value plot will be plotted.

### Author(s)

Part of the code is based on the [sedrate2time](#) function of the 'astrochron' R package

### References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

### Examples

```

# Extract the 405kyr eccentricity cycle from the wavelet scalogram
# from the magnetic susceptibility record of the Sullivan core
# of Pas et al., (2018) and then create a age model using minimal tuning
# (e.g.) set the distance between peaks to 405 kyr. The age model
# (sedimentation rate curve) is then used to convert the data
# from the depth to the time domain

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

mag_405 <- extract_signal_stable_V2(
  wavelet = mag_wt,
  period_max = 4,
  period_min = 2,
  add_mean = TRUE,
  plot_residual = FALSE,

```

```

    keep_editable = FALSE
  )

  mag_405_min_tuning <- minimal_tuning(data = mag_405,
    pts = 5,
    cycle = 405,
    tune_opt = "max",
    output = 1,
    genplot = FALSE,
    keep_editable = FALSE)

  mag_time <- sedrate2tune(
    data=mag,
    sed_curve=mag_405_min_tuning,
    genplot=FALSE,
    keep_editable=FALSE)

```

---

sum_power_sedrate	<i>Calculate sum of maximum spectral power for sedimentation rates for a wavelet spectra</i>
-------------------	--

---

### Description

The `sum_power_sedrate` function is used calculate the sum of maximum spectral power for a list of astronomical cycles from a wavelet spectra. The data is first normalized using the average spectral power curves for a given percentile based on results of the `model_red_noise_wt` function

### Usage

```

sum_power_sedrate(
  red_noise = NULL,
  wavelet = NULL,
  percentile = NULL,
  sedrate_low = NULL,
  sedrate_high = NULL,
  spacing = NULL,
  cycles = c(NULL),
  x_lab = "depth",
  y_lab = "sedrate",
  run_multicore = FALSE,
  genplot = FALSE,
  plot_res = 1,
  keep_editable = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices",
  verbose = FALSE
)

```

**Arguments**

red_noise	Red noise curves generated using the <code>model_red_noise_wt</code> function
wavelet	Wavelet object created using the <code>analyze_wavelet</code> function
percentile	Percentile value (0-1) of the rednoise runs which is used to normalize the data for. To account for the distribution/distortion of the spectral power distribution based on the analytical technique and random red-noise the data is normalized against a percentile based red-noise curve which is the results of the <code>'model_red_noise_wt'</code> modelling runs.
sedrate_low	Minimum sedimentation rate (cm/kyr)for which the sum of maximum spectral power is calculated for.
sedrate_high	Maximum sedimentation rate (cm/kyr) for which the sum of maximum spectral power is calculated for.
spacing	Spacing (cm/kyr) between sedimentation rates
cycles	Astronomical cycles (in kyr) for which the combined sum of maximum spectral power is calculated for
x_lab	label for the y-axis Default="depth"
y_lab	label for the y-axis Default="sedrate"
run_multicore	run simulation using multiple cores Default=FALSE the simulation is run at x-2 cores to allow the 2 remaining processes to run background processes
genplot	Generate plot Default="FALSE"
plot_res	plot options are 1: sum max power or 2: nr of components Default=2
keep_editable	Keep option to add extra features after plotting Default=FALSE
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the <code>color_brewer</code> parameter. The included R packages from which palettes can be chosen from are; the <code>'RColorBrewer'</code> , <code>'grDevices'</code> , <code>'ColorRamps'</code> and <code>'Viridis'</code> R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package <code>'viridis'</code> has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge <code>'RColorBrewer'</code> run the <code>RColorBrewer::brewer.pal.info()</code> function The R package <code>'colorRamps'</code> has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package <code>'grDevices'</code> has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge <code>'grDevices'</code> run the <code>grDevices::hcl.pals()</code> function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the <code>RColorBrewer</code> , <code>grDevices</code> , <code>ColorRamps</code> and <code>Viridis</code> R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices
verbose	Print text Default=FALSE.

**Value**

Returns a list which contains 4 elements element 1: sum of maximum spectral power element 2: number of cycles used in the sum of maximum spectral power element 3: y-axis values of the matrices which is sedimentation rate element 4: x-axis values of the matrices which is depth

If Default="TRUE" a plot is created with 3 subplots. Subplot 1 is plot in which the the sum of maximum spectral power for a given sedimentation rate or nr of cycles is plotted for each depth given depth. Subplot 2 is a plot in which the average sum of maximum spectral power is plotted from each sedimentation Subplot 3 is a color scale for subplot 1.

**Author(s)**

Based on the [asm](#) and [eAsm](#) functions of the 'astrochron' R package and the 'eCOCO' and 'COCO' functions of the 'Acycle' software

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis <doi:10.1016/j.earscirev.2018.11.015>

Acycle: Time-series analysis software for paleoclimate research and education, Mingsong Li, Linda Hinnov, Lee Kump, Computers & Geosciences, Volume 127, 2019, Pages 12-22, ISSN 0098-3004, <doi:10.1016/j.cageo.2019.02.011>

Tracking variable sedimentation rates and astronomical forcing in Phanerozoic paleoclimate proxy series with evolutionary correlation coefficients and hypothesis testing, Mingsong Li, Lee R. Kump, Linda A. Hinnov, Michael E. Mann, Earth and Planetary Science Letters, Volume 501, T2018, Pages 165-179, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.08.041>

**Examples**

```
#estimate sedimentation rate for the the magnetic susceptibility record
# of the Sullivan core of Pas et al., (2018).

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
  n_simulations=10,
  run_multicore=FALSE,
  verbose=FALSE)

sedrates <- sum_power_sedrate(red_noise=mag_wt_red_noise,
  wavelet=mag_wt,
  percentile=0.75,
  sedrate_low = 0.5,
  sedrate_high = 4,
```

```

spacing = 0.05,
cycles = c(2376,1600,1180,696,406,110),
x_lab="depth",
y_lab="sedrate",
run_multicore=FALSE,
genplot = FALSE,
plot_res=1,
keep_editable=FALSE,
palette_name = "rainbow",
color_brewer="grDevices",
verbose=FALSE)

```

---

track\_period\_wavelet *Track the period of a cycle in a wavelet spectra*

---

### Description

Interactively select points in a wavelet spectra to trace a period in a wavelet spectra. The [track\\_period\\_wavelet](#) function plots a wavelet spectra in which spectral peaks can be selected allowing one to track a ridge hence one can track the a cycle with a changing period. Tracking points can be selected in the Interactive interface and will be shown as white dots when one wants to deselect a point the white dots can be re-clicked/re-selected and will turn red which indicates that the previously selected point is deselected. Deselecting points can be quite tricky due to the close spacing of points and such the [delpts\\_tracked\\_period\\_wt](#) can be used to delete points were previously selected using the [track\\_period\\_wavelet](#) function.

### Usage

```

track_period_wavelet(
  astro_cycle = 405,
  wavelet = NULL,
  n.levels = 100,
  track_peaks = TRUE,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)",
  palette_name = "rainbow",
  color_brewer = "grDevices",
  plot_horizontal = TRUE
)

```

### Arguments

astro_cycle	Duration (in kyr) of the cycle which traced.
wavelet	Wavelet object created using the <a href="#">analyze_wavelet</a> function.
n.levels	Number of color levels Default=100.

<code>track_peaks</code>	Setting which indicates whether tracking is restricted to spectral peaks ( <code>track_peaks=TRUE</code> ) or whether any point within the wavelet spectra can be selected ( <code>track_peaks=FALSE</code> ) Default= <code>TRUE</code> .
<code>periodlab</code>	label for the y-axis Default="Period (metres)".
<code>x_lab</code>	label for the x-axis Default="depth (metres)".
<code>palette_name</code>	Name of the color palette which is used for plotting. The color palettes that can be chosen depends on which the R package is specified in the <code>color_brewer</code> parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default= <code>rainbow</code> . The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R package 'RColorBrewer' run the <code>RColorBrewer::brewer.pal.info()</code> function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors","topo.colors" and "cm.colors" To see even more color palette options of the The R package 'grDevices' run the <code>grDevices::hcl.pals()</code> function
<code>color_brewer</code>	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default= <code>grDevices</code>
<code>plot_horizontal</code>	plot the wavelet horizontal or vertical eg y axis is depth or y axis power Default= <code>TRUE</code>

**Value**

Results of the tracking of a cycle in the wavelet spectra is a matrix with 3 columns. The first column is depth/time The second column is the period of the tracked cycle The third column is the sedimentation rate based on the duration (in time) of the tracked cycle

**Author(s)**

The function is based/inspired on the [traceFreq](#) function of the 'astrochron' R package

**References**

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<[doi:10.1016/j.earscirev.2018.11.015](https://doi.org/10.1016/j.earscirev.2018.11.015)>

**Examples**

```
#Track the 405kyr eccentricity cycle in the magnetic susceptibility record
# of the Sullivan core of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
```



```

dj = 1/100,
lowerPeriod = 0.1,
upperPeriod = 254,
verbose = FALSE,
omega_nr = 10)

mag_track <- track_period_wavelet(astro_cycle = 405,
                                wavelet=mag_wt,
                                n.levels = 100,
                                track_peaks=TRUE,
                                periodlab = "Period (metres)",
                                x_lab = "depth (metres)",
                                palette_name = "rainbow",
                                color_brewer="grDevices",
                                plot_horizontal=TRUE)

```

---

TSI

*Total solar irradiation data (0-9400ka) of steinhilber et al., (2012)*


---

### Description

The Total solar irradiation data set consists of the TSI values of Steinhilber et al., (2012)

### Details

Column 1: Age (kyr)

Column 2: Total solar Irradiation (TSI)

### References

Steinhilber, Friedhelm & Abreu, Jacksiel & Beer, Juerg & Brunner, Irene & Christl, Marcus & Fischer, Hubertus & Heikkilä, U. & Kubik, Peter & Mann, Mathias & Mccracken, K. & Miller, Heinrich & Miyahara, Hiroko & Oerter, Hans & Wilhelms, Frank. (2012). 9,400 Years of cosmic radiation and solar activity from ice cores and tree rings. *Proceedings of the National Academy of Sciences of the United States of America*. 109. 5967-71. 10.1073/pnas.1118965109. <doi:10.1073/pnas.1118965109>

---

wavelet\_uncertainty

*Calculate the uncertainty associated with the wavelet analysis based on the Gabor uncertainty principle*


---

## Description

The `wavelet_uncertainty` function is used to calculate uncertainties associated with the wavelet analysis based on the Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet. The calculated uncertainty is the underlying analytical uncertainty which is the result of applying the Gabor uncertainty principle to the continuous wavelet transform using a Morlet wavelet.

## Usage

```
wavelet_uncertainty(
  tracked_cycle = NULL,
  period_of_tracked_cycle = NULL,
  wavelet = NULL,
  multi = 1,
  verbose = FALSE,
  genplot_time = FALSE,
  genplot_uncertainty = FALSE,
  genplot_uncertainty_wt = FALSE,
  keep_editable = FALSE,
  palette_name = "rainbow",
  color_brewer = "grDevices"
)
```

## Arguments

<code>tracked_cycle</code>	Curve of the cycle tracked using the <code>track_period_wavelet</code> function Any input (matrix or data frame) in which the first column is depth or time and the second column is period should work
<code>period_of_tracked_cycle</code>	period of the tracked curve (in kyr).
<code>wavelet</code>	wavelet object created using the <code>analyze_wavelet</code> function.
<code>multi</code>	multiple of the standard deviation to be used for defining uncertainty Default=1.
<code>verbose</code>	Print text Default=FALSE.
<code>genplot_time</code>	plot time curves with a upper and lower uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet, which uses which uses the omega number (number of cycles in the wavelet) at one standard deviation to define the analytical uncertainty Default=TRUE
<code>genplot_uncertainty</code>	Plot period curves with upper and lower uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet, which uses which uses the omega number (number of cycles in the wavelet) to define uncertainty at one standard deviation Default=TRUE
<code>genplot_uncertainty_wt</code>	generate a wavelet plot with the uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet superimposed on top of original wavelet plot. The red curve is period of the tracked curve plus the analytical uncertainty. The blue curve is period of the tracked

	curve min the analytical uncertainty. The black curve is the curve tracked using the 'Default=tracked_cycle_curve function Default=TRUE
keep_editable	Keep option to add extra features after plotting Default=FALSE
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer' run the RColorBrewer::brewer.pal.info() function The R package 'colorRamps' has the color palette options:"blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options:"rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R pacakge 'grDevices' run the grDevices::hcl.pals() function
color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices

## Value

Results pertaining to the uncertainty calculated based on the Gabor uncertainty principle.

If the genplot\_time is TRUE then a depth time plot will be plotted with 3 lines, the mean age, age plus x times the standard deviation and age minus x times the standard deviation .

If the genplot\_uncertainty is TRUE then a curve will be plotted with the mean period, the tracked period plus x times the standard deviation and the tracked period minus x times the standard deviation.

If the genplot\_uncertainty\_wt is TRUE a wavelet spectra will be plotted with the tracked period, the tracked period plus x times the standard deviation, the tracked period minus x times the standard deviation and the area in between will be shaded in grey.

Returns a matrix with 8 columns.

The first column is called "depth" eg. depth

The second column is "period" of the originally tracked period.

The third column is "frequency" of the originally tracked period.

The fourth column "uncertainty in frequency FWHM" is the uncertainty in frequency based on the Gabor uncertainty principle defined as (FWHM) full width at half maximum.

The fifth column "uncertainty in frequency x\_times SD" is the uncertainty in frequency based on the Gabor uncertainty principle defined as times x standard deviations.

The sixth column "time mean" is the mean time based on the tracked period.

The seventh column "time plus x\_times sd" is the time based on the tracked period plus x times the standard deviation.

The eight column "time min x\_times sd" is the time based on the tracked period min x times the

standard deviation.

### Author(s)

Code based on the [analyze.wavelet](#) function of the 'WaveletComp' R package and [wt](#) function of the 'biwavelet' R package which are based on the wavelet 'MATLAB' code written by Christopher Torrence and Gilbert P. Compo (1998). The assignment of the standard deviation of the uncertainty of the wavelet is based on the work of Gabor (1946) and Russell et al., (2016)

### References

- Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>
- Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>
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- Gabor, Dennis. "Theory of communication. Part 1: The analysis of information." Journal of the Institution of Electrical Engineers-part III: radio and communication engineering 93, no. 26 (1946): 429-441. <http://genesis.eecg.toronto.edu/gabor1946.pdf>
- Russell, Brian, and Jiajun Han. "Jean Morlet and the continuous wavelet transform. " CREWES Res. Rep 28 (2016): 115. <https://www.crewes.org/Documents/ResearchReports/2016/CRR201668.pdf>
- Morlet, Jean, Georges Arens, Eliane Fourgeau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " Geophysics 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>
- J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. Geophysics 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

### Examples

```
#calculate the Gabor uncertainty derived mathematical uncertainty of the
#magnetic susceptibility record of the Sullivan core of Pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
```

```

#           wavelet=mag_wt,
#           n.levels = 100,
#           periodlab = "Period (metres)",
#           x_lab = "depth (metres)",
#           palette_name="rainbow",
#           color_brewer= "grDevices")

#Instead of tracking, the tracked solution data set mag_track_solution is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = FALSE,
  genplot = FALSE,
  keep_editable=FALSE
)

mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = FALSE, print_span = FALSE,keep_editable=FALSE)

uncertainty <- wavelet_uncertainty(
  tracked_cycle = mag_track_complete,
  period_of_tracked_cycle = 405,
  wavelet = mag_wt,
  multi=1,
  verbose = FALSE,
  genplot_time = FALSE,
  genplot_uncertainty = FALSE,
  genplot_uncertainty_wt = FALSE,
  keep_editable=FALSE,
  palette_name="rainbow",
  color_brewer= "grDevices"
)

```

## Description

The continuous wavelet transform enables the observation of transient/non-stationary cyclicity in time-series. The goal of cyclostratigraphic studies is to define frequency/period in the depth/time domain. By conducting the continuous wavelet transform on cyclostratigraphic data series one can observe and extract cyclic signals/signatures from signals. These results can then be visualized and interpreted enabling one to identify/interpret cyclicity in the geological record, which can be used to construct astrochronological age-models and identify and interpret cyclicity in past and present climate systems.

## Details

Package: 'WaverideR'  
 Type: R package  
 Version: 0.3.2 (begin of 2023)  
 License: GPL (= 2)

## Note

If you want to use this package for publication or research purposes, please cite:

Arts, M.C.M (2023). WaverideR: Extracting Signals from Wavelet Spectra. <https://CRAN.R-project.org/package=WaverideR>

## Author(s)

Michiel Arts  
 Maintainer: Michiel Arts <[michiel.arts@stratigraphy.eu](mailto:michiel.arts@stratigraphy.eu)>

## References

The 'WaverideR' package builds upon existing literature and existing codebase. The following list of articles is relevant for the 'WaverideR' R package and its functions. Individual articles are also cited in the descriptions of function when relative for set function. The articles in the list below can be grouped in four subjects: (1) Cyclostratigraphic data analysis, (2) example data sets, (3) the (continuous) wavelet transform and (4) astronomical solutions). For each of these categories the relevance of set articles will be explained in the framework of the 'WaverideR' R package.

### # 1. Cyclostratigraphic data analysis

Stephen R. Meyers, Cyclostratigraphy and the problem of astrochronologic testing, Earth-Science Reviews, Volume 190, 2019, Pages 190-223, ISSN 0012-8252 [doi:10.1016/j.earscirev.2018.11.015](https://doi.org/10.1016/j.earscirev.2018.11.015)

The 'astrochron' R package is the most extensive R package with regards to cyclostratigraphic analysis. As such many of the functionalities of the 'WaverideR' R package are # inspired/based on the 'astrochron' R package. The major difference between # the 'astrochron' R package and the 'WaverideR' package is that the # 'astrochron' R package relies on the Fast Fourier Transform whereas

S.R. Meyers, 2012, Seeing Red in Cyclic Stratigraphy: Spectral Noise Estimation for Astrochronology: Paleoclimatology, 27, PA3228, [doi:10.1029/2012PA002307](https://doi.org/10.1029/2012PA002307)

The article of Meyers (2012) explains how the (Multitaper method) MTM technique implemented into The 'astrochron' R package The MTM method can be used to assign confidence levels to spectral peaks and distinguish spectral peaks from harmonic spectral peaks.

Acycle: Time-series analysis software for paleoclimate research and education, Mingsong Li, Linda Hinnov, Lee Kump, Computers & Geosciences, Volume 127, 2019, Pages 12-22, ISSN 0098-3004, [doi:10.1016/j.cageo.2019.02.011](https://doi.org/10.1016/j.cageo.2019.02.011)

The 'Acycle' software package is a 'Matlab' based program, which is used for cyclostratigraphic studies. Acycle relies mostly on the Fast Fourier Transform. The 'Coco' and 'eCoco' functions from Acycle formed the inspiration for the [flmw\\_sum\\_power\\_sedrate](#) functions of the 'WaverideR' R package.

Tracking variable sedimentation rates and astronomical forcing in Phanerozoic paleoclimate proxy series with evolutionary correlation coefficients and hypothesis testing, Mingsong Li, Lee R. Kump, Linda A. Hinnov, Michael E. Mann, Earth and Planetary Science Letters, Volume 501, 2018, Pages 165-179, ISSN 0012-821X, doi:10.1016/j.epsl.2018.08.041

Li et al., (2019) introduces the Coco and eCoco functions of the Acycle software package. the 'Coco' and 'eCoco' function of the 'Acycle' software are able to estimate the sedimentation rate based on spectral characteristics of astronomical cycles. The 'Coco' and 'eCoco' function and form the inspiration for the `flmw` and `sum_power_sedrate` functions of the 'WaverideR' Package.

Wouters, S., Crucifix, M., Sinnesael, M., Da Silva, A.C., Zeeden, C., Zivanovic, M., Boulvain, F., Devleeschouwer, X., 2022, "A decomposition approach to cyclostratigraphic signal processing". Earth-Science Reviews 225 (103894).doi:10.1016/j.earscirev.2021.103894

Wouters et al., (2022) introduces the Empirical Mode Decomposition (EMD) as part of the 'DecomposeR' R package. EMD is a non-Fast Fourier Transform based spectral analysis technique. The Hilbert transform function `inst.pulse` of this package is used in WaverideR functions `extract_amplitude` and `Hilbert_transform`.

Wouters, S., Da Silva, A.-C., Boulvain, F., and Devleeschouwer, X.. 2021. Stratigrapher: Concepts for Litholog Generation in R. The R Journal. doi:10.32614/RJ2021039

Wouters et al., (2021) introduces the `Stratigrapher` R package. This package contains functions which format, process, and plot lithologs. The litholog format of Wouters et al., (2021) is used as the standardized input format to convert lithologs to a time series format using the `lithlog_disc` function. The time series can then be analysed for the imprint of cycles.

#Huang, Norden E., Zhaohua Wu, Steven R. Long, Kenneth C. Arnold, Xianyao Chen, and Karin Blank. 2009. "On Instantaneous Frequency". Advances in Adaptive Data Analysis 01 (02): 177–229. doi:10.1142/S1793536909000096

The Hilbert transform function `inst.pulse` of the 'DecomposeR' R package is based on the work of Huang et al., (2009).

Cleveland, W. S. (1979) Robust locally weighted regression and smoothing scatter plots. Journal of the American Statistical Association. 74, 829–836. doi:10.1080/01621459.1979.10481038

Cleveland (1979) explains how the robust locally weighted regression works and how it can be used to smooth data sets. This theory is applied in the `loess_auto` function of the 'WaverideR' package.

#Hurvich, C.M., Simonoff, J.S., and Tsai, C.L. (1998), Smoothing Parameter Selection in Non-parametric Regression Using an Improved Akaike Information Criterion. Journal of the Royal Statistical Society B. 60, 271–293 doi:10.1111/14679868.00125

Hurvich et al., (1998) explains how the Improved Akaike Information Criterion can be used to optimally smooth data sets This theory is applied in the `loess_auto` function of the 'WaverideR' package.

#Golub, G., Heath, M. and Wahba, G. (1979). Generalized cross validation as a method for choosing a good ridge parameter. Technometrics. 21, 215–224. doi:10.2307/1268518

Golub et al., (1979) explains how the Generalized cross validation can be used to optimally smooth data sets. This theory is applied in the `loess_auto` function of the 'WaverideR' package.

## # 2. Example data sets

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488,2018,Pages 102-114,ISSN 0012-821X, doi:10.1016/j.epsl.2018.02.010

The data set of Pas et al, (2018) is a magnetic susceptibility data measured on the Fammennian

aged shales of the from the Illinois basin in the USA. The data set contains the imprint of astronomical cycles in the a Paleozoic succession making it a good example for times (250Ma) when no astronomical solutions are available.

Steinhilber, Friedhelm & Abreu, Jacksiel & Beer, Juerg & Brunner, Irene & Christl, Marcus & Fischer, Hubertus & Heikkilä, U. & Kubik, Peter & Mann, Mathias & Mcracken, K. & Miller, Heinrich & Miyahara, Hiroko & Oerter, Hans & Wilhelms, Frank. (2012). 9,400 Years of cosmic radiation and solar activity from ice cores and tree rings. *Proceedings of the National Academy of Sciences of the United States of America*. 109. 5967-71. 10.1073/pnas.1118965109. doi:10.1073/pnas.1118965109

The Total Solar Irradiance record of Steinhilber et al., (2012) is a Holocene record of normalized Total Solar Irradiance in the time domain. The data set is a good example for studying/extracting sub-Milankovitch 5000yr from a relatively (geologically) speaking young record.

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369,2013,Pages 430-451,ISSN 0031-0182, 10.1016/j.palaeo.2012.11.009

The record of Zeeden et al., (2013) consists of a grey scale record from Miocene sediment cores from offshore Brazil. The record contains a clear imprint of astronomical cycles as such it is a good Neogene example data set to demonstrate the functionalities of the 'WaverideR' R package

### # 3. The (continuous) wavelet transform

Morlet, Jean, Georges Arens, Eliane Fourgeau, and Dominique Glard. "Wave propagation and sampling theory—Part I: Complex signal and scattering in multilayered media. " *Geophysics* 47, no. 2 (1982): 203-221. <https://pubs.geoscienceworld.org/geophysics/article/47/2/203/68601/Wave-propagation-and-sampling-theory-Part-I>

Morlet et al., (1982a) together with Morlet et al., (1982b) are the original publications which explain the use of the wavelet to analyse signal.

J. Morlet, G. Arens, E. Fourgeau, D. Giard; Wave propagation and sampling theory; Part II, Sampling theory and complex waves. *Geophysics* 1982 47 (2): 222–236. <https://pubs.geoscienceworld.org/geophysics/article/47/2/222/68604/Wave-propagation-and-sampling-theory-Part-II>

Morlet et al., (1982a) together with Morlet et al., (1982b) are the original publications which explain the use of the wavelet to analyse signal.

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. *Bulletin of the American Meteorological Society* 79:61-78. [https://paos.colorado.edu/research/wavelets/bams\\_79\\_01\\_0061.pdf](https://paos.colorado.edu/research/wavelets/bams_79_01_0061.pdf)

'Torrence and Compo (1998) shows how the continuous wavelet transform can be used to analyse cyclicity in paleo-climatic data-sets. The equations in this publication forms the basis for many wavelet based packages/software applications.

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Gouhier et al., (2021) is the implementation of equations of Torrence and Compo (1998) in the form of the 'biwavelet' R package

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Roesch and Schmidbauer et al., (2018) is the article of the 'WaveletComp' R package which is a built upon the functionalities of the 'biwavelet' R package



Russell, Brian, and Jiajun Han. "Jean Morlet and the continuous wavelet transform. " CREWES Res. Rep 28 (2016): 115. <https://www.crewes.org/Documents/ResearchReports/2016/CRR201668.pdf>

Russell and Han (2016) gives a concise summary of the work of Morlet et al., (1982a) and Morlet et al., (1982b) and the developments since then. The publication also describes how the Gabor uncertainty principle (Gabor 1946) affects the frequency uncertainty of the wavelet which can be used to calculate the analytical uncertainty of a given wavelet spectra.

Gabor, Dennis. "Theory of communication. Part 1: The analysis of information." Journal of the Institution of Electrical Engineers-part III: radio and communication engineering 93, no. 26 (1946): 429-441. <http://genesis.eecg.toronto.edu/gabor1946.pdf>

Gabor (1946) describes the Gabor uncertainty principle which states how the uncertainty in time and frequency are related in time series analysis.

#### # 4. Astronomical solutions

J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: *Astron. Astrophys.*, Volume 428, 261-285. doi:10.1051/00046361:20041335

Laskar et al., (2004) is an astronomical solution which can be used to anchor geological data to absolute ages.

Laskar, J., Fienga, A., Gastineau, M., Manche, H., 2011a, La2010: A new orbital solution for the long-term motion of the Earth: *Astron. Astrophys.*, Volume 532, A89 doi:10.1051/00046361/201116836

Laskar et al., (2011a) is an astronomical solution which can be used to anchor geological data to absolute ages.

Laskar, J., Gastineau, M., Delisle, J.-B., Farres, A., Fienga, A.: 2011b, Strong chaos induced by close encounters with Ceres and Vesta, *Astron: Astrophys.*, Volume 532, L4. doi:10.1051/0004-6361/201117504

Laskar et al., (2011b) is an astronomical solution which can be used to anchor geological data to absolute ages.

J. Laskar, Chapter 4 - Astrochronology, Editor(s): Felix M. Gradstein, James G. Ogg, Mark D. Schmitz, Gabi M. Ogg, *Geologic Time Scale 2020*, Elsevier, 2020, Pages 139-158, ISBN 9780128243602, doi:10.1016/B9780128243602.000048

Laskar et al., (2019) explains how astronomical solutions are created and how they should/can be used

Zeebe, Richard E. "Numerical solutions for the orbital motion of the Solar System over the past 100 Myr: limits and new results." *The Astronomical Journal* 154, no. 5 (2017): 193. doi:10.3847/1538-3881/aa8cce

Zeebe (2017) is an astronomical solution which can be used to anchor geological data to absolute ages.

Richard E. Zeebe Lucas J. Lourens ,Solar System chaos and the Paleocene–Eocene boundary age constrained by geology and astronomy. *Science* 365,926-929(2019) doi:10.1126/science.aax0612

Zeebe and Lourens (2019) is an astronomical solution which can be used to anchor geological data to absolute ages.

Zeebe, R. E. and Lourens, L. J. Geologically constrained astronomical solutions for the Cenozoic era, *Earth and Planetary Science Letters*, 2022 doi:10.1016/j.epsl.2022.117595

Zeebe and Lourens (2022) is an astronomical solution which can be used to anchor geological data to absolute ages.

### Description

Data sets for testing the 'WaverideR' R package:

The `age_model_zeeden` data set is an age model (anchor points) for the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

The `astrosignal_example` data set consists of pre-generated ETP (eccentricity-tilt-precession) data set based on the p-0.5t la2004 solution and was generated using the `etp` function of the 'astrochron' R package

The `depth_rank_example` data set is a synthetic succession of sedimentary  
The grey data set is the grey scale record of IODP 926 for the interval (154-174m) which originates from Zeeden et al., (2013)

The `grey_track` data set consists of tracking points of the precession (22 kyr cycle) in the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

The `mag` data set is the magnetic susceptibility record of Pas et al., (2018)

The `mag_track_solution` is the period of the 405 kyr eccentricity cycle in the magnetic susceptibility record of Pas et al., (2018)

The `TSI` data set is the Total Solar Irradiance record of Steinhilber et al., (2012)

The `Bisciaro_Mg_wt_track` data set is the 110-kyr (short eccentricity) cycle tracked in the wavelet scalogram of the Magnesium (XRF) record of Arts (2014)

The `Bisciaro_Mn_wt_track` data set is the 110-kyr (short eccentricity) cycle tracked in the wavelet scalogram of the Manganese (XRF) record of Arts (2014)

The `Bisciaro_al_wt_track` data set is the 110-kyr (short eccentricity) cycle tracked in the wavelet scalogram of the Aluminum (XRF) record of Arts (2014)

The `Bisciaro_ca_wt_track` data set is the 110-kyr (short eccentricity) cycle tracked in the wavelet scalogram of the Calcium (XRF) record of Arts (2014)

The `Bisciaro_sial_wt_track` data set is the 110-kyr (short eccentricity) cycle tracked in the wavelet scalogram of the Silicon/Aluminum (XRF) record of Arts (2014)

The `Bisciaro_XRF` is the XRF data set of Arts (2014)

The `anchor_points_Bisciaro_al` data set consists of the tie points between the `Bisciaro_al` record of Arts (2014) and the la2011 solution of Laskar et al., (2011)

The GTS\_info data set contains the color coding and ages and uncertainties of Geologic Time Scale 2020 of Ogg (et al., 2021)

## References

- Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), *Earth and Planetary Science Letters*, Volume 488,2018,Pages 102-114,ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>
- Steinhilber, Friedhelm & Abreu, Jacksiel & Beer, Juerg & Brunner, Irene & Christl, Marcus & Fischer, Hubertus & Heikkilä, U. & Kubik, Peter & Mann, Mathias & Mccracken, K. & Miller, Heinrich & Miyahara, Hiroko & Oerter, Hans & Wilhelms, Frank. (2012). 9,400 Years of cosmic radiation and solar activity from ice cores and tree rings. *Proceedings of the National Academy of Sciences of the United States of America*. 109. 5967-71. 10.1073/pnas.1118965109. <doi:10.1073/pnas.1118965109>
- Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369,2013,Pages 430-451,ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>
- Stephen R. Meyers,Cyclostratigraphy and the problem of astrochronologic testing, *Earth-Science Reviews*,Volume 190,2019,Pages 190-223,ISSN 0012-8252 <doi:10.1016/j.earscirev.2018.11.015>
- J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: *Astron. Astrophys.*, Volume 428, 261-285. <doi:10.1051/0004-6361:20041335>
- Laskar, J., M. Gastineau, J. B. Delisle, A. Farrés, and A. Fienga (2011b), Strong chaos induced by close encounters with Ceres and Vesta, *Astron. Astrophys.*, 532, L4,<doi:10.1051/0004-6361/201117504>
- M.C.M. Arts, 2014, *Magnetostatigraphy and geochemical analysis of the early Miocene Bisciaro Formation in the Contessa Valley (Northern Italy)*. Unpublished Bsc. thesis
- Ogg, Gabi & Ogg, James & Gradstein, Felix. (2021). Recommended color coding of stages - Appendix 1 from Geologic Time Scale 2020.

---

win\_fft

*Windowed fft based spectral analysis*

---

## Description

The `win_fft` function for conducts a windowed spectral analysis based on the `fft`

**Usage**

```
win_fft(
  data = NULL,
  padfac = 5,
  window_size = NULL,
  run_multicore = FALSE,
  genplot = FALSE,
  x_lab = c("depth (m)"),
  y_lab = c("frequency cycle/metre"),
  plot_res = 1,
  perc_vis = 0,
  freq_max = NULL,
  freq_min = NULL,
  palette_name = "rainbow",
  color_brewer = "grDevices",
  keep_editable = FALSE,
  verbose = FALSE,
  dev_new = FALSE
)
```

**Arguments**

data	Input data set should consist of a matrix with 2 columns with first column being depth and the second column being a proxy
padfac	Pad record with zero, zero padding smooths out the spectra
window_size	size of the running window
run_multicore	Run function using multiple cores Default="FALSE"
genplot	Generate plot Default="FALSE"
x_lab	label for the y-axis Default="depth"
y_lab	label for the y-axis Default="sedrate"
plot_res	plot 1 of 8 options option 1: Amplitude matrix, option 2: Power matrix, option 3: Phase matrix, option 4: AR1_CL matrix, option 5: AR1_Fit matrix , option 6: AR1_90_power matrix, option 7: AR1_95_power matrix, option 8: AR1_99_power matrix, Default=1
perc_vis	Cutoff percentile when plotting Default=0
freq_max	Maximum frequency to plot
freq_min	Minimum frequency to plot
palette_name	Name of the color palette which is used for plotting. The color palettes than can be chosen depends on which the R package is specified in the color_brewer parameter. The included R packages from which palettes can be chosen from are; the 'RColorBrewer', 'grDevices', 'ColorRamps' and 'Viridis' R packages. There are many options to choose from so please read the documentation of these packages Default=rainbow. The R package 'viridis' has the color palette options: "magma", "plasma", "inferno", "viridis", "mako", and "rocket" and "turbo" To see the color palette options of the The R pacakge 'RColorBrewer'

run the `RColorBrewer::brewer.pal.info()` function The R package 'colorRamps' has the color palette options: "blue2green", "blue2green2red", "blue2red", "blue2yellow", "colorRamps", "cyan2yellow", "green2red", "magenta2green", "matlab.like", "matlab.like2" and "ygobb" The R package 'grDevices' has the built in palette options: "rainbow", "heat.colors", "terrain.colors", "topo.colors" and "cm.colors" To see even more color palette options of the The R package 'grDevices' run the `grDevices::hcl.pals()` function

color_brewer	Name of the R package from which the color palette is chosen from. The included R packages from which palettes can be chosen are; the RColorBrewer, grDevices, ColorRamps and Viridis R packages. There are many options to choose from so please read the documentation of these packages. "Default=grDevices"
keep_editable	Keep option to add extra features after plotting Default=FALSE
verbose	Print text Default=FALSE.
dev_new	Opens a new plotting window to plot the plot, this guarantees a "nice" looking plot however when plotting in an R markdown document the plot might not plot Default=FALSE

### Value

Returns a list which contains 10 elements element 1: Amplitude matrix element 2: Power matrix element 3: Phase matrix element 4: AR1\_CL matrix element 5: AR1\_Fit matrix element 6: AR1\_90\_power matrix element 7: AR1\_95\_power matrix element 8: AR1\_99\_power matrix element 9: depth element 10: y\_axis If `genplot` is `Default=TRUE` then a plot of one of the elements 1:8 is plotted

### Author(s)

Based on the [periodogram](#) function of the 'astrochron' R package.

### References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis  
<doi:10.1016/j.earscirev.2018.11.015>

### Examples

```
#Conduct a windowed fft on the magnetic susceptibility record
#of the Sullivan core of Pas et al., (2018).
```

```
mag_win_fft <- win_fft(data= mag,
  padfac = 5,
  window_size = 12.5,
  run_multicore = FALSE,
  genplot = FALSE,
  x_lab = c("depth (m)"),
  y_lab = c("frequency cycle/metre"),
  plot_res = 1,
  perc_vis = 0.5,
  freq_max = 5,
```

```
freq_min = 0.001,  
palette_name = "rainbow",  
color_brewer = "grDevices",  
keep_editable = FALSE,  
verbose = FALSE,  
dev_new = FALSE)
```

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