## Package 'causaloptim'

October 17, 2024

**Encoding** UTF-8

Type Package

Title An Interface to Specify Causal Graphs and Compute Bounds on Causal Effects

Version 1.0.0

Date 2024-10-16

Maintainer Michael C Sachs <sachsmc@gmail.com>

**Description** When causal quantities are not identifiable from the observed data, it still may be possible to bound these quantities using the observed data. We outline a class of problems for which the derivation of tight bounds is always a linear programming problem and can therefore, at least theoretically, be solved using a symbolic linear optimizer. We extend and generalize the approach of Balke and Pearl (1994) <doi:10.1016/B978-1-55860-332-5.50011-0> and we provide a user friendly graphical interface for setting up such problems via directed acyclic graphs (DAG), which only allow for problems within this class to be depicted. The user can then define linear constraints to further refine their assumptions to meet their specific problem, and then specify a causal query using a text interface. The program converts this user defined DAG, query, and constraints, and returns tight bounds. The bounds can be converted to R functions to evaluate them for specific datasets, and to latex code for publication. The methods and proofs of tightness and validity of the bounds are described in a paper by Sachs, Jonzon, Gabriel, and Sjölander (2022) <doi:10.1080/10618600.2022.2071905>.

License MIT + file LICENSE

Imports shiny, rcdd

**Depends** R (>= 3.5.0), igraph

RoxygenNote 7.3.2

**Suggests** testthat (>= 3.0.0), knitr, rmarkdown

VignetteBuilder knitr

URL https://sachsmc.github.io/causaloptim/

BugReports https://github.com/sachsmc/causaloptim/issues/

**Config/testthat/edition** 3

Contents

## NeedsCompilation no

Author Michael C Sachs [aut, cre], Erin E Gabriel [aut], Arvid Sjölander [aut], Gustav Jonzon [aut], Alexander A Balke [ctb] ((C++ code)), Colorado Reed [ctb] ((graph-creator.js))

**Repository** CRAN

Date/Publication 2024-10-17 09:00:02 UTC

## Contents

| causaloptim-package        | 3  |
|----------------------------|----|
| analyze_graph              | 3  |
| btm_var                    | 5  |
| causalproblemcheck         | 6  |
| check_constraints_violated | 7  |
| check_linear_objective     | 8  |
| check_parents              | 9  |
| constraintscheck           | 10 |
| create_causalmodel         | 10 |
| create_effect_vector       | 12 |
|                            | 13 |
| _1                         | 14 |
| create_response_function   | 15 |
|                            | 16 |
| B                          | 16 |
| graphrescheck              | 17 |
| initialize_graph           | 18 |
|                            | 18 |
|                            | 19 |
| list_to_path               | 20 |
| optimize_effect_2          | 20 |
| opt_effect                 | 21 |
| parse_constraints          | 22 |
| parse_effect               |    |
| plot.linearcausalproblem   | 23 |
| plot_graphres              | 24 |
| print.causalmodel          | 25 |
| print.linearcausalproblem  | 25 |
| querycheck                 | 26 |
| rdirichlet                 | 26 |
| sample_distribution        | 27 |
| simulate_bounds            | 28 |
| specify_graph              | 29 |
| update_effect              | 29 |

## Index

causaloptim-package An Interface to Specify Causal Graphs and Compute Bounds on Causal Effects

#### Description

Specify causal graphs using a visual interactive interface and then analyze them and compute symbolic bounds for the causal effects in terms of the observable parameters.

#### Details

Run the shiny app by results <- specify\_graph(). See detailed instructions in the vignette browseVignettes("causaloptim").

## Author(s)

Michael C Sachs, Arvid Sjölander, Gustav Jonzon, Alexander Balke, Colorado Reed, and Erin Gabriel Maintainer: Michael C Sachs <sachsmc at gmail.com>

#### References

Sachs, M. C., Jonzon, G., Sjölander, A., & Gabriel, E. E. (2023). A general method for deriving tight symbolic bounds on causal effects. Journal of Computational and Graphical Statistics, 32(2), 567-576. https://www.tandfonline.com/doi/full/10.1080/10618600.2022.2071905.

## See Also

browseVignettes('causaloptim') specify\_graph

| analyze_graph | Analyze the causal graph and effect to determine constraints and ob- |
|---------------|--|
|               | jective  |

#### Description

The graph must contain certain edge and vertex attributes which are documented in the Details below. The shiny app run by specify\_graph will return a graph in this format.

#### Usage

analyze\_graph(graph, constraints, effectt)

31

#### Arguments

| graph       | An igraph-package object that represents a directed acyclic graph with certain attributes. See Details. |
|-------------|---|
| constraints | A vector of character strings that represent the constraints on counterfactual quantities               |
| effectt     | A character string that represents the causal effect of interest  |

#### Details

The graph object must contain the following named vertex attributes:

- **name** The name of each vertex must be a valid R object name starting with a letter and no special characters. Good candidate names are for example, Z1, Z2, W2, X3, etc.
- leftside An indicator of whether the vertex is on the left side of the graph, 1 if yes, 0 if no.
- **latent** An indicator of whether the variable is latent (unobserved). There should always be a variable Ul on the left side that is latent and a parent of all variables on the left side, and another latent variable Ur on the right side that is a parent of all variables on the right side.
- **nvals** The number of possible values that the variable can take on, the default and minimum is 2 for 2 categories (0,1). In general, a variable with nvals of K can take on values 0, 1, ..., (K-1).

In addition, there must be the following edge attributes:

- **rlconnect** An indicator of whether the edge goes from the right side to the left side. Should be 0 for all edges.
- **edge.monotone** An indicator of whether the effect of the edge is monotone, meaning that if V1 -> V2 and the edge is monotone, then a > b implies V2(V1 = a) >= V2(V1 = b). Only available for binary variables (nvals = 2).

The effect parameter describes your causal effect of interest. The effect parameter must be of the form

p{V11(X=a)=a; V12(X=a)=b;...} op1 p{V21(X=b)=a; V22(X=c)=b;...} op2 ...

where Vij are names of variables in the graph, a, b are numeric values from 0:(nvals - 1), and op are either - or +. You can specify a single probability statement (i.e., no operator). Note that the probability statements begin with little p, and use curly braces, and items inside the probability statements are separated by ;. The variables may be potential outcomes which are denoted by parentheses. Variables may also be nested inside potential outcomes. Pure observations such as  $p{Y = 1}$  are not allowed if the left side contains any variables. There are 2 important rules to follow: 1) Only variables on the right side can be in the probability events, and if the left side is not empty: 2) none of the variables in the left side that are intervened upon can have any children in the left side, and all paths from the left to the right must be blocked by the intervention set. Here the intervention set is anything that is inside the smooth brackets (i.e., variable set to values).

All of the following are valid effect statements:

 $p\{Y(X = 1) = 1\} - p\{Y(X = 0) = 1\}$   $p\{X(Z = 1) = 1; X(Z = 0) = 0\}$  $p\{Y(M(X = 0), X = 1) = 1\} - p\{Y(M(X = 0), X = 0) = 1\}$ 

#### btm\_var

The constraints are specified in terms of potential outcomes to constrain by writing the potential outcomes, values of their parents, and operators that determine the constraint (equalities or inequalities). For example, X(Z = 1) >= X(Z = 0)

#### Value

A an object of class "linearcausalproblem", which is a list with the following components. This list can be passed to optimize\_effect\_2 which interfaces with the symbolic optimization program. Print and plot methods are also available.

- variables Character vector of variable names of potential outcomes, these start with 'q' to match Balke's notation
- **parameters** Character vector of parameter names of observed probabilities, these start with 'p' to match Balke's notation
- constraints Character vector of parsed constraints
- objective Character string defining the objective to be optimized in terms of the variables
- **p.vals** Matrix of all possible values of the observed data vector, corresponding to the list of parameters.
- **q.vals** Matrix of all possible values of the response function form of the potential outcomes, corresponding to the list of variables.
- parsed.query A nested list containing information on the parsed causal query.
- **objective.nonreduced** The objective in terms of the original variables, before algebraic variable reduction. The nonreduced variables can be obtained by concatenating the columns of q.vals.
- response.functions List of response functions.

graph The graph as passed to the function.

- **R** A matrix with coefficients relating the p.vals to the q.vals p = R \* q
- **c0** A vector of coefficients relating the q vals to the objective function theta = c0 \* q
- iqR A matrix with coefficients to represent the inequality constraints

#### Examples

### confounded exposure and outcome

```
b <- initialize_graph(igraph::graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y))
analyze_graph(b, constraints = NULL, effectt = "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}")
```

btm\_var

```
Recursive function to get the last name in a list
```

#### Description

Recursive function to get the last name in a list

#### Usage

btm\_var(x, name = NULL)

#### Arguments

| х    | a list                              |
|------|-------------------------------------|
| name | name of the top element of the list |

## Value

The name of the deepest nested list element

## Examples

btm\_var(list(X = list(Y = list(K = 1))))

causalproblemcheck Check conditions on causal problem

## Description

Check that a given causal problem (a causal DAG together with a causal query) satisfies conditions that guarantee that the optimization problem is linear.

## Usage

```
causalproblemcheck(digraph, query)
```

#### Arguments

| digraph | An igraph object representing a digraph.                |
|---------|---|
|         | Expected vertex attributes: leftside, latent and nvals. |
|         | Optional vertex attributes: exposure and outcome.       |
|         | Expected edge attributes: rlconnect and edge.monotone.  |
| query   | A string representing a causal query / effect.          |

## Value

TRUE if conditions are met; FALSE otherwise.

```
b <- graph_from_literal(X - +Y, Ur - +X, Ur - +Y)
V(b)$leftside <- c(0, 0, 0)
V(b)$latent <- c(0, 0, 1)
V(b)$nvals <- c(2, 2, 2)
V(b)$exposure <- c(1, 0, 0)
V(b)$outcome <- c(0, 1, 0)
E(b)$rlconnect <- c(0, 0, 0)
E(b)$edge.monotone <- c(0, 0, 0)</pre>
```

```
effectt <- "p{Y(X=1)=1}-p{Y(X=0)=1}"
causalproblemcheck(digraph = b, query = effectt)</pre>
```

check\_constraints\_violated

```
Check whether any of the observable constraints implied by the causal model are violated for a given distribution of observables
```

## Description

Check whether any of the observable constraints implied by the causal model are violated for a given distribution of observables

#### Usage

```
check_constraints_violated(obj, probs, tol = 1e-12)
```

## Arguments

| obj   | An object of class "causalmodel"   |
|-------|--|
| probs | A named vector of observable probabilities, in the same order as obj $data$ parameters |
| tol   | Tolerance for checking (in)equalities  |

## Value

Either TRUE (violated) or FALSE (not violated) with messages indicating what constraints are violated if any.

```
graph <- initialize_graph(graph_from_literal(Z -+ X, X -+ Y, Ur -+ X, Ur -+ Y))</pre>
```

```
iv_model <- create_causalmodel(graph, prob.form = list(out = c("X", "Y"), cond = "Z"))
check_constraints_violated(iv_model, probs = sample_distribution(iv_model))</pre>
```

check\_linear\_objective

*Check linearity of objective function implied by a causal model and effect* 

#### Description

Check linearity of objective function implied by a causal model and effect

#### Usage

```
check_linear_objective(causal_model, effectt)
```

## Arguments

| causal_model | An object of class "causalmodel" as produce by create_causalmodel |
|--------------|---|
| effectt      | A character string that represents the causal effect of interest  |

#### Details

The effect parameter describes your causal effect of interest. The effect parameter must be of the form

p{V11(X=a)=a; V12(X=a)=b;...} op1 p{V21(X=b)=a; V22(X=c)=b;...} op2 ...

where Vij are names of variables in the graph, a, b are numeric values from 0:(nvals - 1), and op are either - or +. You can specify a single probability statement (i.e., no operator). Note that the probability statements begin with little p, and use curly braces, and items inside the probability statements are separated by ;. The variables may be potential outcomes which are denoted by parentheses. Variables may also be nested inside potential outcomes.

All of the following are valid effect statements:

$$p{Y(X = 1) = 1} - p{Y(X = 0) = 1}$$

- $p{X(Z = 1) = 1; X(Z = 0) = 0}$
- $p{Y(M(X = 0), X = 1) = 1} p{Y(M(X = 0), X = 0) = 1}$

The effect must be fully specified, that is, all parents of a variable that is intervened upon need to be specified. The function cannot infer missing values or marginalize over some parents but not others.

## Value

A logical value that is TRUE if the objective function is linear

#### check\_parents

#### Examples

## regular IV case

check\_parents Check for paths from from to to

#### Description

Check for paths from from to to

#### Usage

```
check_parents(parent_lookup, from, to, prev = NULL)
```

## Arguments

| parent_lookup | A list of vectors                       |
|---------------|---|
| from          | character                               |
| to            | character                               |
| prev          | Should always be null when first called |

## Value

A list of paths or null if no path is found

```
parent_lookup <- list(M = "Am", Y = c("M", "Ay"), A = NULL, Am = "A", Ay = "A")
check_parents(parent_lookup, "A", "Y")</pre>
```

constraintscheck Check constraints

#### Description

Check that a user-provided constraint is parsable, has valid variables and relations.

## Usage

constraintscheck(constrainttext, graphres)

#### Arguments

| constrainttext | A string representing a constraint.  |
|----------------|--------------------------------------|
| graphres       | An igraph object representing a DAG. |

## Value

TRUE if all check pass; else FALSE.

#### Examples

```
graphres <- graph_from_literal(Z -+ X, X -+ Y, Ul -+ Z, Ur -+ X, Ur -+ Y)
V(graphres)$leftside <- c(1, 0, 0, 1, 0)
V(graphres)$latent <- c(0, 0, 0, 1, 1)
V(graphres)$nvals <- c(3, 2, 2, 2, 2)
V(graphres)$exposure <- c(0, 1, 0, 0, 0)
V(graphres)$outcome <- c(0, 0, 1, 0, 0)
E(graphres)$rlconnect <- c(0, 0, 0, 0, 0)
E(graphres)$edge.monotone <- c(0, 0, 0, 0, 0)
constrainttext <- "X(Z = 1) >= X(Z = 0)"
constraintscheck(constrainttext = constrainttext, graphres = graphres) # TRUE
```

| create_causalmodel | Create a structural causal model from a graph or a set of response |
|--------------------|--|
|                    | functions  |

## Description

Given either a graph or a set of response functions (i.e., either graph or respvars may be provided), and a specification of what conditional probabilities are observed, produce a causal model.

create\_causalmodel

#### Usage

```
create_causalmodel(
  graph = NULL,
  respvars = NULL,
  prob.form,
  p.vals,
  constraints = NULL,
  right.vars = NULL
)
```

#### Arguments

| graph       | A graph with special edge and vertex attributes, as produced by initialize_graph   |
|-------------|--|
| respvars    | List of response functions as produced by create_response_function   |
| prob.form   | A list with two named elements "out", "cond" where each element is a character vector of variable names that appear in p.vals  |
| p.vals      | Data frame defining which probabilities are observable. The variable names of p.vals must all appear in prob.form. If missing, will assume that all combinations of the variables values are observed. |
| constraints | A vector of character strings that represent the constraints on counterfactual quantities  |
| right.vars  | A vector of character strings indicating which variables are on the right side of the graph. Only required when graph is NULL. See examples.   |

## Details

It is assumed that probabilities of the form p(out | cond) are observed, for each combination of values in p.vals. cond may be NULL in which case nothing is conditioned on.

The constraints are specified in terms of potential outcomes to constrain by writing the potential outcomes, values of their parents, and operators that determine the constraint (equalities or inequalities). For example, X(Z = 1) >= X(Z = 0)

## Value

An object of class "causalmodel"

#### Examples

```
## regular IV case
```

#showing the use of right.vars

create\_effect\_vector Translate target effect to vector of response variables

#### Description

Translate target effect to vector of response variables

## Usage

```
create_effect_vector(causal_model, effect)
```

#### Arguments

| causal_model | An object of class "causalmodel" as produced by create_causalmodel |
|--------------|--|
| effect       | Effect list, as returned by parse_effect                           |

## Value

A list with the target effect in terms of qs

create\_linearcausalproblem

Create linear causal problem from causal model and effect

#### Description

A more flexible alternative to analyze\_graph that takes as inputs the causal model and effect.

#### Usage

create\_linearcausalproblem(causal\_model, effectt)

#### Arguments

| causal_model | An object of class "causalmodel" as produce by create_causalmodel |
|--------------|---|
| effectt      | A character string that represents the causal effect of interest  |

#### Details

The effect parameter describes your causal effect of interest. The effect parameter must be of the form

p{V11(X=a)=a; V12(X=a)=b;...} op1 p{V21(X=b)=a; V22(X=c)=b;...} op2 ...

where Vij are names of variables in the graph, a, b are numeric values from 0:(nvals - 1), and op are either - or +. You can specify a single probability statement (i.e., no operator). Note that the probability statements begin with little p, and use curly braces, and items inside the probability statements are separated by ;. The variables may be potential outcomes which are denoted by parentheses. Variables may also be nested inside potential outcomes. Pure observations such as  $p{Y = 1}$  are not allowed if the left side contains any variables. There are 2 important rules to follow: 1) Only variables on the right side can be in the probability events, and if the left side is not empty: 2) none of the variables in the left side that are intervened upon can have any children in the left side, and all paths from the left to the right must be blocked by the intervention set. Here the intervention set is anything that is inside the smooth brackets (i.e., variable set to values).

All of the following are valid effect statements:

$$p{Y(X = 1) = 1} - p{Y(X = 0) = 1}$$
  

$$p{X(Z = 1) = 1; X(Z = 0) = 0}$$
  

$$p{Y(M(X = 0), X = 1) = 1} - p{Y(M(X = 0), X = 0) = 1}$$

#### Value

A an object of class "linearcausalproblem", which is a list with the following components. This list can be passed to optimize\_effect\_2 which interfaces with the symbolic optimization program. Print and plot methods are also available.

variables Character vector of variable names of potential outcomes, these start with 'q' to match Balke's notation **parameters** Character vector of parameter names of observed probabilities, these start with 'p' to match Balke's notation

constraints Character vector of parsed constraints

- **objective** Character string defining the objective to be optimized in terms of the variables
- **p.vals** Matrix of all possible values of the observed data vector, corresponding to the list of parameters.
- **q.vals** Matrix of all possible values of the response function form of the potential outcomes, corresponding to the list of variables.
- parsed.query A nested list containing information on the parsed causal query.
- **objective.nonreduced** The objective in terms of the original variables, before algebraic variable reduction. The nonreduced variables can be obtained by concatenating the columns of q.vals.

response.functions List of response functions.

graph The graph as passed to the function.

- **R** A matrix with coefficients relating the p.vals to the q.vals p = R \* q
- **c0** A vector of coefficients relating the q vals to the objective function theta = c0 \* q
- iqR A matrix with coefficients to represent the inequality constraints

#### Examples

```
### confounded exposure and outcome
b <- initialize_graph(igraph::graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y))
confmod <- create_causalmodel(graph = b, prob.form = list(out = c("X", "Y"), cond = NULL))
create_linearcausalproblem(confmod, effectt = "p{Y(X = 1) = 1}")</pre>
```

create\_q\_matrix Translate response functions into matrix of counterfactuals

#### Description

Translate response functions into matrix of counterfactuals

#### Usage

```
create_q_matrix(respvars, right.vars, cond.vars, constraints)
```

#### Arguments

| respvars    | A list of functions as returned by create_response_function  |
|-------------|--|
| right.vars  | Vertices of graph on the right side                          |
| cond.vars   | Vertices of graph on the left side                           |
| constraints | A vector of character strings that represent the constraints |

#### Value

A list of 3 data frames of counterfactuals and their associated labels

## Examples

```
graphres <- initialize_graph(graph_from_literal(Z -+ X, X -+ Y, Ul -+ Z, Ur -+ X, Ur -+ Y))
constraints <- "X(Z = 1) >= X(Z = 0)"
cond.vars <- V(graphres)[V(graphres)$leftside == 1 & names(V(graphres)) != "Ul"]
right.vars <- V(graphres)[V(graphres)$leftside == 0 & names(V(graphres)) != "Ur"]
respvars <- create_response_function(graphres)
create_q_matrix(respvars, right.vars, cond.vars, constraints)</pre>
```

 ${\tt create\_response\_function}$ 

Translate regular DAG to response functions

## Description

Translate regular DAG to response functions

#### Usage

```
create_response_function(graph)
```

#### Arguments

graph An aaa-igraph-package object that represents a directed acyclic graph that contains certain edge attributes. The shiny app returns a graph in this format and initialize\_graph will add them to a regular igraph object with sensible defaults.

## Value

A list of functions representing the response functions

```
### confounded exposure and outcome
b <- initialize_graph(igraph::graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y))
create_response_function(b)</pre>
```

find\_all\_paths

#### Description

Given a set of response functions, find all directed paths from from to to

#### Usage

find\_all\_paths(respvars, from, to)

#### Arguments

| respvars | A set of response functions as created by create_response_function |
|----------|--|
| from     | A character string indicating the start of the path                |
| to       | A character string indicating the end of the path                  |

## Value

A list with all the paths or a list with NULL if there are none

## Examples

```
b <- initialize_graph(igraph::graph_from_literal(X -+ Z, Z -+ Y, X -+ Y, Ur -+ Z, Ur -+ Y))
medmod <- create_response_function(b)
find_all_paths(medmod, "X", "Y")
igraph::all_simple_paths(b, "X", "Y", mode = "out")</pre>
```

get\_default\_effect Define default effect for a given graph

## Description

Define default effect for a given graph

#### Usage

```
get_default_effect(graphres)
```

## Arguments

graphres The graph object, should have vertex attributes "outcome" and "exposure"

## Value

A string that can be passed to parse\_effect

#### graphrescheck

#### Examples

```
graphres <- graph_from_literal(Z -+ X, X -+ Y, Ul -+ Z, Ur -+ X, Ur -+ Y)
V(graphres)$leftside <- c(1, 0, 0, 1, 0)
V(graphres)$latent <- c(0, 0, 0, 1, 1)
V(graphres)$nvals <- c(3, 2, 2, 2, 2)
V(graphres)$exposure <- c(0, 1, 0, 0, 0)
V(graphres)$outcome <- c(0, 0, 1, 0, 0)
E(graphres)$rlconnect <- c(0, 0, 0, 0, 0)
E(graphres)$edge.monotone <- c(0, 0, 0, 0, 0)
get_default_effect(graphres = graphres) == "p{Y(X = 1)=1} - p{Y(X = 0)=1}" # TRUE</pre>
```

graphrescheck Check conditions on digraph

## Description

Check that a given digraph satisfies the conditions of 'no left to right edges', 'no cycles', 'valid number of categories' and 'valid variable names'. Optionally returns the digraph if all checks are passed.

## Usage

graphrescheck(graphres, ret = FALSE)

#### Arguments

| graphres | An igraph object representing a digraph.   |
|----------|--|
| ret      | A logical value. Default is FALSE. Set to TRUE to also return graphres if all checks are passed. |

## Value

If ret=FALSE (default): TRUE if all checks pass; else FALSE. If ret=TRUE: graphres if all checks pass; else FALSE.

```
graphres <- graph_from_literal(X -+ Y, X -+ M, M -+ Y, Ul -+ X, Ur -+ M, Ur -+ Y)
V(graphres)$leftside <- c(1, 0, 0, 1, 0)
V(graphres)$latent <- c(0, 0, 0, 1, 1)
V(graphres)$nvals <- c(2, 2, 2, 2, 2)
V(graphres)$exposure <- c(0, 0, 0, 0, 0)
V(graphres)$outcome <- c(0, 0, 0, 0, 0)
E(graphres)$rlconnect <- c(0, 0, 0, 0, 0, 0)
E(graphres)$edge.monotone <- c(0, 0, 0, 0, 0, 0)
graphrescheck(graphres = graphres) # TRUE</pre>
```

initialize\_graph

## Description

Checks for required attributes and adds defaults if missing

## Usage

```
initialize_graph(graph)
```

## Arguments

graph An object of class igraph

## Value

An igraph with the vertex attributes leftside, latent, and nvals, and edge attributes rlconnect and edge.monotone

## Examples

```
b <- igraph::graph_from_literal(X -+ Y)
b2 <- initialize_graph(b)
V(b2)$nvals
```

interpret\_bounds Convert bounds string to a function

## Description

Convert bounds string to a function

#### Usage

interpret\_bounds(bounds, parameters)

## Arguments

| bounds     | The bounds element as returned by optimize_effect                  |
|------------|--|
| parameters | Character vector defining parameters, as returned by analyze_graph |

#### Value

A function that takes arguments for the parameters, i.e., the observed probabilities and returns a vector of length 2: the lower bound and the upper bound.

## latex\_bounds

#### Examples

```
b <- graph_from_literal(X ++ Y, Ur ++ X, Ur ++ Y)
V(b)$leftside <- c(0,0,0)
V(b)$latent <- c(0,0,1)
V(b)$nvals <- c(2,2,2)
E(b)$rlconnect <- E(b)$edge.monotone <- c(0, 0, 0)
obj <- analyze_graph(b, constraints = NULL, effectt = "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}")
bounds <- optimize_effect_2(obj)
bounds_func <- interpret_bounds(bounds$bounds, obj$parameters)
bounds_func(.1, .1, .4, .3)
# vectorized
do.call(bounds_func, lapply(1:4, function(i) runif(5)))
```

latex\_bounds Latex bounds equations

## Description

Latex bounds equations

## Usage

```
latex_bounds(bounds, parameters, prob.sym = "P", brackets = c("(", ")"))
```

#### Arguments

| bounds     | Vector of bounds as returned by optimize_effect_2  |
|------------|--|
| parameters | The parameters object as returned by analyze_graph   |
| prob.sym   | Symbol to use for probability statements in latex, usually "P" or "pr"                                 |
| brackets   | Length 2 vector with opening and closing bracket, usually $c("(", ")")$ , or $c(" \setminus \{", "\})$ |

## Value

A character string with latex code for the bounds

```
b <- graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y)
V(b)$leftside <- c(0,0,0)
V(b)$latent <- c(0,0,1)
V(b)$nvals <- c(2,2,2)
E(b)$rlconnect <- E(b)$edge.monotone <- c(0, 0, 0)
obj <- analyze_graph(b, constraints = NULL, effectt = "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}")
bounds <- optimize_effect_2(obj)
latex_bounds(bounds$bounds, obj$parameters)
latex_bounds(bounds$bounds, obj$parameters, "Pr")
```

list\_to\_path

## Description

Recursive function to translate an effect list to a path sequence

## Usage

list\_to\_path(x, name = NULL)

#### Arguments

| х    | A list of vars as returned by parse_effect |
|------|--|
| name | The name of the outcome variable           |

#### Value

a list of characters describing the path sequence

## Examples

```
nofill <- "p{Y(X = 1, M1 = 1, M2(X = 1, M1 = 1)) = 1}"
eff2 <- parse_effect(nofill)$vars[[1]][[1]]
list_to_path(eff2, "Y")</pre>
```

optimize\_effect\_2 Run the optimizer to obtain symbolic bounds

## Description

Given an object with the linear programming problem set up, compute the bounds using rcdd. Bounds are returned as text but can be converted to R functions using interpret\_bounds, or latex code using latex\_bounds.

## Usage

optimize\_effect\_2(obj)

#### Arguments

```
obj
```

Object as returned by analyze\_graph or create\_linearcausalproblem

## opt\_effect

## Value

An object of class "balkebound" that is a list that contains the bounds and logs as character strings, and a function to compute the bounds

#### Examples

```
b <- initialize_graph(graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y))
obj <- analyze_graph(b, constraints = NULL, effectt = "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}")
optimize_effect_2(obj)</pre>
```

opt\_effect

```
Compute a bound on the average causal effect
```

## Description

This helper function does the heavy lifting for optimize\_effect\_2. For a given casual query, it computes either a lower or an upper bound on the corresponding causal effect.

#### Usage

opt\_effect(opt, obj)

## Arguments

| opt | A string. Either "min" or "max" for a lower or an upper bound, respectively.                    |
|-----|---|
| obj | An object as returned by the function analyze_graph. Contains the casual query to be estimated. |

## Value

An object of class optbound; a list with the following named components:

- expr is the main output; an expression of the bound as a print-friendly string,
- type is either "lower" or "upper" according to the type of the bound,
- dual\_vertices is a numeric matrix whose rows are the vertices of the convex polytope of the dual LP,
- dual\_vrep is a V-representation of the dual convex polytope, including some extra data.

parse\_constraints Parse text that defines a the constraints

## Description

Parse text that defines a the constraints

## Usage

parse\_constraints(constraints, obsnames)

## Arguments

| constraints | A list of character strings                            |
|-------------|--|
| obsnames    | Vector of names of the observed variables in the graph |

## Value

A data frame with columns indicating the variables being constrained, what the values of their parents are for the constraints, and the operator defining the constraint (equality or inequalities).

## Examples

```
constrainttext <- "X(Z = 1) >= X(Z = 0)"
obsnames <- c("Z", "X", "Y")
parse_constraints(constraints = constrainttext, obsnames = obsnames)</pre>
```

parse\_effect

Parse text that defines a causal effect

## Description

Parse text that defines a causal effect

#### Usage

```
parse_effect(text)
```

#### Arguments

text Character string

#### Value

A nested list that contains the following components:

- **vars** For each element of the causal query, this indicates potential outcomes as names of the list elements, the variables that they depend on, and the values that any variables are being fixed to.
- oper The vector of operators (addition or subtraction) that combine the terms of the causal query.

values The values that the potential outcomes are set to in the query.

**pcheck** List of logicals for each element of the query that are TRUE if the element is a potential outcome and FALSE if it is an observational quantity.

#### Examples

effectt <- "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}"
parse\_effect(text = effectt)</pre>

plot.linearcausalproblem

*Plot the graph from the causal problem with a legend describing attributes* 

#### Description

Plot the graph from the causal problem with a legend describing attributes

## Usage

## S3 method for class 'linearcausalproblem'
plot(x, ...)

## Arguments

| Х | object of class "linearcausalproblem" |
|---|---------------------------------------|
|   | Not used                              |

#### Value

Nothing

## See Also

plot\_graphres which plots the graph only

## Examples

```
b <- graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y)
V(b)$leftside <- c(0,0,0)
V(b)$latent <- c(0,0,1)
V(b)$nvals <- c(2,2,2)
V(b)$exposure <- c(1,0,0)
V(b)$outcome <- c(0,1,0)
E(b)$rlconnect <- c(0,0,0)
E(b)$edge.monotone <- c(0,0,0)
q <- "p{Y(X=1)=1}-p{Y(X=0)=1}"
obj <- analyze_graph(graph = b, constraints = NULL, effectt <- q)
plot(obj)
```

plot\_graphres Plot the analyzed graph object

## Description

Special plotting method for igraphs of this type

## Usage

plot\_graphres(graphres)

#### Arguments

graphres an igraph object

## Value

None

## See Also

plot.linearcausalproblem which plots a graph with attributes

## Examples

```
b <- graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y)
V(b)$leftside <- c(0,0,0)
V(b)$latent <- c(0,0,1)
V(b)$nvals <- c(2,2,2)
V(b)$exposure <- c(1,0,0)
V(b)$outcome <- c(0,1,0)
E(b)$rlconnect <- c(0,0,0)
E(b)$edge.monotone <- c(0,0,0)
plot(b)</pre>
```

24

print.causalmodel *Print relevant information about the causal model* 

## Description

Print relevant information about the causal model

## Usage

```
## S3 method for class 'causalmodel'
print(x, omit_cf_constraints = FALSE, omit_obs_constraints = FALSE, ...)
```

## Arguments

| Х                              | object of class "causalmodel"               |  |
|--------------------------------|---|--|
| <pre>omit_cf_constraints</pre> |   |  |
|                                | Do not print the counterfactual constraints |  |
| omit_obs_constraints           |   |  |
|                                | Do not print the observable constraints     |  |
|                                | Not used                                    |  |

## Value

x, invisibly

## Description

Print the causal problem

## Usage

```
## S3 method for class 'linearcausalproblem'
print(x, ...)
```

## Arguments

| Х | object of class "linearcausaloptim" |
|---|-------------------------------------|
|   | Not used                            |

## Value

x, invisibly

querycheck

#### Description

Given an admissible causal DAG, check that given a causal query satisfies conditions that guarantee the corresponding causal problem to be a linear program. Throws error messages detailing any conditions violated.

#### Usage

querycheck(effecttext, graphres)

#### Arguments

| effecttext | A string representing a causal query.    |
|------------|--|
| graphres   | An igraph object representing a digraph. |

#### Value

TRUE if effecttext is parsable, contains only variables in V(graphres) and satisfies conditions for linearity; else FALSE.

#### Examples

```
graphres <- graph_from_literal(X -+ Y, X -+ M, M -+ Y, Ul -+ X, Ur -+ M, Ur -+ Y)
V(graphres)$leftside <- c(1, 0, 0, 1, 0)
V(graphres)$latent <- c(0, 0, 0, 1, 1)
V(graphres)$nvals <- c(2, 2, 2, 2, 2)
V(graphres)$exposure <- c(0, 0, 0, 0, 0)
V(graphres)$outcome <- c(0, 0, 0, 0, 0)
E(graphres)$rlconnect <- c(0, 0, 0, 0, 0, 0)
E(graphres)$edge.monotone <- c(0, 0, 0, 0, 0, 0)
effecttext <- "p{Y(M(X = 0), X = 1) = 1} - p{Y(M(X = 0), X = 0) = 1}"
querycheck(effecttext = effecttext, graphres = graphres) # TRUE</pre>
```

rdirichlet

Sample from a Dirichlet distribution

#### Description

Generate a random vector from the k-dimensional symmetric Dirichlet distribution with concentration parameter alpha

#### Usage

rdirichlet(k, alpha = 1)

#### Arguments

| k     | Length of the vector     |
|-------|--------------------------|
| alpha | Concentration parameters |

## Value

a numeric vector

## Examples

```
qvals <- rdirichlet(16, 1)
sum(qvals)</pre>
```

| sample_distribution | Sample a distribution of observable probabilities that satisfy the |
|---------------------|--|
|                     | causal model   |

## Description

Sample a distribution of observable probabilities that satisfy the causal model

#### Usage

```
sample_distribution(
   obj,
   simplex_sampler = function(k) {
      rdirichlet(k, alpha = 1)
   }
)
```

## Arguments

obj

An object of class "causalmodel"

simplex\_sampler

A function to generate a random sample from the simplex in k dimensions, where k is the number of variables (q parameters, obj\$data\$variables). By default this is uniform (symmetric dirichlet with parameter 1).

## Value

A vector of observable probabilities that satisfy the causal model

#### Examples

```
graph <- initialize_graph(graph_from_literal(Z -+ X, X -+ Y, Ur -+ X, Ur -+ Y))
prob.form <- list(out = c("X", "Y"), cond = "Z")</pre>
```

```
iv_model <- create_causalmodel(graph, prob.form = prob.form)
sample_distribution(iv_model)</pre>
```

simulate\_bounds Simulate bounds

#### Description

Run a simple simulation based on the bounds. For each simulation, sample the set of counterfactual probabilities from a uniform distribution, translate into a multinomial distribution, and then compute the objective and the bounds in terms of the observable variables.

#### Usage

```
simulate_bounds(obj, bounds, nsim = 1000)
```

## Arguments

| obj    | Object as returned by analyze_graph     |
|--------|---|
| bounds | Object as returned by optimize_effect_2 |
| nsim   | Number of simulation replicates         |

## Value

A data frame with columns: objective, bound.lower, bound.upper

## Examples

```
b <- initialize_graph(graph_from_literal(X -+ Y, Ur -+ X, Ur -+ Y))
obj <- analyze_graph(b, constraints = NULL, effectt = "p{Y(X = 1) = 1} - p{Y(X = 0) = 1}")
bounds <- optimize_effect_2(obj)
simulate_bounds(obj, bounds, nsim = 5)</pre>
```

28

specify\_graph

#### Description

This launches the Shiny interface in the system's default web browser. The results of the computation will be displayed in the browser, but they can also be returned to the R session by assigning the result of the function call to an object. See below for information on what is returned.

#### Usage

specify\_graph()

## Value

If the button "Exit and return graph object" is clicked, then only the graph is returned as an aaaigraph-package object.

If the bounds are computed and the button "Exit and return objects to R" is clicked, then a list is returned with the following elements:

graphres The graph as drawn and interpreted, an aaa-igraph-package object.

**obj** The objective and all necessary supporting information. This object is documented in analyze\_graph. This can be passed directly to optimize\_effect\_2.

bounds.obs Object of class 'balkebound' as returned by optimize\_effect\_2.

constraints Character vector of the specified constraints. NULL if no constraints.

effect Text describing the causal effect of interest.

**boundsFunction** Function that takes parameters (observed probabilities) as arguments, and returns a vector of length 2 for the lower and upper bounds.

update\_effect Update the effect in a linearcausalproblem object

#### Description

If you want to use the same graph and response function, but change the effect of interest, this can save some computation time.

## Usage

```
update_effect(obj, effectt)
```

#### Arguments

| obj     | An object as returned by analyze_graph                           |
|---------|--|
| effectt | A character string that represents the causal effect of interest |

#### Value

A object of class linearcausalproblem, see analyze\_graph for details

```
b <- igraph::graph_from_literal(X -+ Y, X -+ M, M -+ Y, Ul -+ X, Ur -+ Y, Ur -+ M)
V(b)$leftside <- c(1, 0, 0, 1, 0)
V(b)$latent <- c(0, 0, 0, 1, 1)
V(b)$nvals <- c(2, 2, 2, 2, 2)
E(b)$rlconnect <- c(0, 0, 0, 0, 0, 0)
E(b)$edge.monotone <- c(0, 0, 0, 0, 0, 0)
CDE0_query <- "p{Y(M = 0, X = 1) = 1} - p{Y(M = 0, X = 0) = 1}"
CDE0_obj <- analyze_graph(b, constraints = NULL, effectt = CDE0_query)
CDE0_bounds <- optimize_effect_2(CDE0_obj)</pre>
CDE0_boundsfunction <- interpret_bounds(bounds = CDE0_bounds$bounds,</pre>
parameters = CDE0_obj$parameters)
CDE1_query <- "p{Y(M = 1, X = 1) = 1} - p{Y(M = 1, X = 0) = 1}"
CDE1_obj <- update_effect(CDE0_obj, effectt = CDE1_query)</pre>
CDE1_bounds <- optimize_effect_2(CDE1_obj)</pre>
CDE1_boundsfunction <- interpret_bounds(bounds = CDE1_bounds$bounds,</pre>
parameters = CDE1_obj$parameters)
```

# Index

aaa-igraph-package, *15*, *29* analyze\_graph, *3*, *13*, *18–21*, *28–30* 

 $btm_var, 5$ 

causaloptim(causaloptim-package), 3 causaloptim-package, 3 causalproblemcheck, 6 check\_constraints\_violated, 7 check\_linear\_objective, 8 check\_parents, 9 constraintscheck, 10 create\_causalmodel, 8, 10, 12, 13 create\_effect\_vector, 12 create\_linearcausalproblem, 13, 20 create\_q\_matrix, 14 create\_response\_function, 11, 14, 15, 16 find\_all\_paths, 16 get\_default\_effect, 16 graphrescheck, 17 igraph-package, 4 initialize\_graph, *11*, *15*, 18 interpret\_bounds, 18, 20 latex\_bounds, 19, 20 list\_to\_path, 20 opt\_effect, 21 optimize\_effect, 18 optimize\_effect (optimize\_effect\_2), 20 optimize\_effect\_2, 5, 13, 19, 20, 21, 28, 29 parse\_constraints, 22 parse\_effect, 12, 16, 20, 22 plot.linearcausalproblem, 23, 24 plot\_graphres, 23, 24 print.causalmodel, 25 print.linearcausalproblem, 25

querycheck, 26

rdirichlet, 26

sample\_distribution, 27
simulate\_bounds, 28
specify\_graph, 3, 29

update\_effect, 29