

# Package ‘uniformly’

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**Type** Package

**Title** Uniform Sampling

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**Description** Uniform sampling on various geometric shapes, such as spheres, ellipsoids, simplices.

**License** GPL-3

**URL** <https://github.com/stla/uniformly>

**BugReports** <https://github.com/stla/uniformly/issues>

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**Suggests** geometry, knitr, misc3d, rmarkdown, scatterplot3d

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|                |                        |
|----------------|------------------------|
| makeHexahedron | <i>Make hexahedron</i> |
|----------------|------------------------|

---

**Description**

Make a hexahedron for usage in [runif\\_in\\_hexahedron](#) and other functions.

**Usage**

```
makeHexahedron(p0, p1, p2, p3, p4, p5, p6, p7)
```

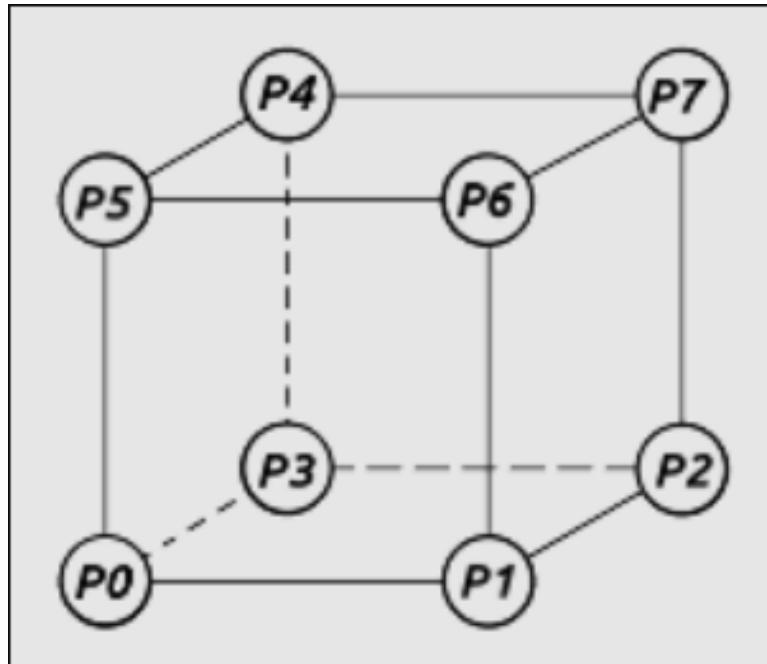
**Arguments**

p0, p1, p2, p3, p4, p5, p6, p7

the eight vertices of the hexahedron, as in the figure shown below

### Details

A hexahedron is a polyhedron having six quad faces. Its eight vertices must be placed as in the figure below.



### Value

A matrix with eight columns, the vertices.

### See Also

The function [plotHexahedron](#) is useful to check the hexahedron.

### Examples

```
library(uniformly)
# a non-convex hexahedron
hexahedron <- makeHexahedron(
  p0 = c(1.5, 1.5, 0),
  p1 = c(2, 0, 0),
  p2 = c(2, 2, 0),
  p3 = c(0, 2, 0),
  p4 = c(0, 2, 2),
  p5 = c(0, 0, 2),
  p6 = c(2, 0, 2),
  p7 = c(2, 2, 2)
)
plotHexahedron(hexahedron)
```

`plotHexahedron`

*Plot hexahedron*

## Description

Plot a hexahedron with **rgl**.

## Usage

```
plotHexahedron(hexahedron, alpha = 1)
```

## Arguments

|                         |  |
|-------------------------|--|
| <code>hexahedron</code> | a hexahedron given by a 3 times 8 matrix; see <a href="#">makeHexahedron</a> |
| <code>alpha</code>      | opacity, a number between 0 and 1  |

## Value

No returned value, called for plotting.

## Examples

```
library(uniformly)
hexahedron <- makeHexahedron(
  p0 = c(0, 0, 0),
  p1 = c(2, 0, 0),
  p2 = c(2, 2, 0),
  p3 = c(0, 2, 0),
  p4 = c(0.5, 1.5, 2),
  p5 = c(0.5, 0.5, 2),
  p6 = c(1.5, 0.5, 2),
  p7 = c(1.5, 1.5, 2)
)
plotHexahedron(hexahedron)
```

*rphong\_on\_hemisphere    Sampling on hemisphere*

## Description

Sampling on a hemisphere according to the Phong density (dimension 3).

## Usage

```
rphong_on_hemisphere(n, alpha = 0, r = 1)
```

**Arguments**

|       |   |
|-------|---|
| n     | number of simulations   |
| alpha | parameter of the Phong density, a positive number; 0 for uniform sampling (default) |
| r     | radius  |

**Value**

The simulations in a n times 3 matrix.

**Examples**

```
## Not run:
library(rgl)
sims <- rphong_on_hemisphere(400, alpha = 10)
spheres3d(0, 0, 0, color = "red", alpha = 0.5)
points3d(sims)
## End(Not run)
```

runif\_cube

*Uniform sampling on/in cube***Description**

Uniform sampling on or in a cube (arbitrary dimension).

**Usage**

```
runif_in_cube(n, d, O = rep(0, d), r = 1)

runif_on_cube(n, d, O = rep(0, d), r = 1)
```

**Arguments**

|   |                                |
|---|--------------------------------|
| n | number of simulations          |
| d | dimension                      |
| O | center of the cube             |
| r | radius (half-side) of the cube |

**Value**

The simulations in a n times d matrix.

## Examples

```
sims <- runif_on_cube(60, d = 2)
plot(sims, xlim = c(-1,1), ylim = c(-1,1), pch = 19, asp = 1)
sims <- runif_in_cube(50, d = 3)
library(scatterplot3d)
scatterplot3d(sims, pch = 19, highlight.3d = TRUE, asp = 1)
```

**runif\_ellipsoid**      *Uniform sampling on/in ellipsoid*

## Description

Uniform sampling on an ellipsoid or in an ellipsoid. The sampling *in* an ellipsoid is available in arbitrary dimension. The sampling *on* an ellipsoid is available only in dimension 2 or 3.

## Usage

```
runif_on_ellipse(n, A, r)
runif_on_ellipsoid(n, A, r)
runif_in_ellipsoid(n, A, r)
```

## Arguments

|   |  |
|---|--|
| n | number of simulations  |
| A | symmetric positive-definite matrix defining the ellipsoid (see Details), of size 2 for <code>runif_on_ellipse</code> and size 2 or 3 for <code>runif_on_ellipsoid</code> (for size 2 these are the same functions) |
| r | "radius" (see Details)   |

## Details

The ellipsoid is the set of vectors  $x$  satisfying  $t(x) \%*\% A \%*\% x == r^2$ . For example, for an axis-aligned ellipse with horizontal radius  $a$  and vertical radius  $b$ , take  $A=1/\text{diag}(c(a^2,b^2))$  and  $r=1$ .

## Value

The simulations in a matrix with n rows.

## Examples

```

library(uniformly)
set.seed(666L)
# ellipse parameters
A <- rbind(c(2, 1), c(1, 1))
r <- 2
# plot the ellipse
x1 <- seq(-2.5, 2.5, length.out = 100)
x2 <- seq(-3, 3, length.out = 100)
z <- outer(
  x1, x2, FUN = Vectorize(function(x1, x2) t(c(x1, x2)) %*% A %*% c(x1, x2)))
)
contour(x1, x2, z, nlevels = 1, levels = r^2, asp = 1, drawlabels = FALSE)
# simulations on the perimeter
sims <- runif_on_ellipse(60, A, r)
points(sims, pch = 19, col = "blue")
# simulations in the area
sims <- runif_in_ellipsoid(100, A, r)
points(sims, pch = 19, col = "green")
# 3D example #####
A <- matrix(c(5,1,1, 1,3,1, 1,1,1), ncol = 3L)
r <- 2
# draw the ellipsoid
library(misc3d)
x <- seq(-1, 1, length.out = 50)
y <- seq(-1.5, 1.5, length.out = 50)
z <- seq(-2.7, 2.7, length.out = 50)
g <- as.matrix(expand.grid(x = x, y = y, z = z))
voxel <-
  array(apply(g, 1L, function(v) t(v) %*% A %*% v), dim = c(50, 50, 50))
isosurface <- computeContour3d(voxel, max(voxel), r^2, x = x, y = y, z = z)
drawScene.rgl(makeTriangles(isosurface, alpha = 0.3))
# simulate and plot points on ellipsoid
library(rgl)
sims <- runif_on_ellipsoid(300, A, r)
points3d(sims)

```

runif\_in\_annulus      *Uniform sampling in an annulus*

## Description

Uniform sampling in an annulus (dimension 2).

## Usage

```
runif_in_annulus(n, 0, r1, r2)
```

**Arguments**

|                 |                       |
|-----------------|-----------------------|
| <code>n</code>  | number of simulations |
| <code>0</code>  | center of the annulus |
| <code>r1</code> | inner radius          |
| <code>r2</code> | outer radius          |

**Value**

The simulations in a `n` times 2 matrix.

**Examples**

```
sims <- runif_in_annulus(100, c(0, 0), 1, 2)
plot(sims, xlim = c(-2, 2), ylim = c(-2, 2), asp = 1, pch = 19)
```

**runif\_in\_hexahedron**    *Uniform sampling in a hexahedron*

**Description**

Uniform sampling in a hexahedron (polyhedron with six faces).

**Usage**

```
runif_in_hexahedron(n, hexahedron)
```

**Arguments**

|                         |  |
|-------------------------|--|
| <code>n</code>          | number of simulations  |
| <code>hexahedron</code> | a hexahedron given by a 3 times 8 matrix whose eight columns are the vertices;<br>see <a href="#">makeHexahedron</a> |

**Value**

The simulations in a `n` times 3 matrix.

**Examples**

```
library(uniformly)
hexahedron <- makeHexahedron(
  p0 = c(0, 0, 0),
  p1 = c(2, 0, 0),
  p2 = c(2, 2, 0),
  p3 = c(0, 2, 0),
  p4 = c(0.5, 1.5, 2),
  p5 = c(0.5, 0.5, 2),
  p6 = c(1.5, 0.5, 2),
```

```

p7 = c(1.5, 1.5, 2)
)
sims <- runif_in_hexahedron(200, hexahedron)
plotHexahedron(hexahedron, alpha = 0.3)
rgl::points3d(sims)

```

**runif\_in\_pball**      *Uniform sampling in a p-ball*

## Description

Uniform sampling in a p-ball (arbitrary dimension).

## Usage

```
runif_in_pball(n, d, p, r = 1)
```

## Arguments

|   |   |
|---|---|
| n | number of simulations                     |
| d | dimension                                 |
| p | exponent in the p-norm, a positive number |
| r | positive number, the radius               |

## Value

The simulations in a n times d matrix.

## Examples

```

sims <- runif_in_pball(500, d = 2, p = 1)
plot(sims, xlim = c(-1, 1), ylim = c(-1, 1), asp = 1)

```

**runif\_in\_polygon**      *Uniform sampling in a polygon*

## Description

Uniform sampling in a polygon (dimension 2).

## Usage

```
runif_in_polygon(n, vertices, center = "centroid")
```

### Arguments

|                       |  |
|-----------------------|--|
| <code>n</code>        | number of simulations  |
| <code>vertices</code> | two-columns matrix giving the vertices (rows); the vertices must be ordered (clockwise or counterclockwise)          |
| <code>center</code>   | a point with respect to which the polygon is star-shaped, or "centroid" (default) to take the centroid (see Details) |

### Details

This function works for a star-shaped polygon, that is, a polygon that contains a point from which the entire polygon boundary is visible. This point must be given in the `center` argument. If the polygon is convex, any point inside the polygon is suitable (thus the default option of the `center` argument is appropriate in this case).

### Value

The simulations in a `n` times 2 matrix.

### Examples

```
vs <- matrix(c(0.951056516295154, 0.309016994374947,
               0.224513988289793, 0.309016994374947,
               -0.951056516295154, 0.309016994374948,
               -0.363271264002681, -0.118033988749895,
               0.587785252292473, -0.809016994374948,
               0.36327126400268, -0.118033988749895,
               0, 1,
               -0.224513988289793, 0.309016994374947,
               -0.587785252292473, -0.809016994374947,
               0, -0.381966011250105),
               ncol=2, byrow=TRUE)
sims <- runif_in_polygon(500, vs)
plot(sims, xlim = c(-1, 1), ylim = c(-1, 1), pch = 19, asp = 1)
```

**runif\_in\_simplex**      *Uniform sampling in a simplex*

### Description

Uniform sampling in a simplex (arbitrary dimension).

### Usage

```
runif_in_simplex(n, simplex)
```

### Arguments

|                      |  |
|----------------------|--|
| <code>n</code>       | number of simulations  |
| <code>simplex</code> | a $(d+1)$ times $d$ matrix giving the vertices of the simplex (rows) |

**Value**

The simulations in a n times d matrix.

**Note**

In dimension 3, you can use [runif\\_in\\_tetrahedron](#) instead.

**Examples**

```
simplex <- rbind(c(0,0,0), c(1,0,0), c(1,1,0), c(1,1,2))
sims <- runif_in_simplex(1000, simplex)
library(rgl)
points3d(sims)
```

**runif\_in\_tetrahedron**    *Uniform sampling in a tetrahedron*

**Description**

Uniform sampling in a tetrahedron (in dimension 3).

**Usage**

```
runif_in_tetrahedron(n, v1, v2, v3, v4)
```

**Arguments**

|                |                             |
|----------------|-----------------------------|
| n              | number of simulations       |
| v1, v2, v3, v4 | vertices of the tetrahedron |

**Value**

The simulations in a n times 3 matrix.

**See Also**

[runif\\_in\\_simplex](#) for sampling in a simplex in arbitrary dimension.

**Examples**

```
library(rgl)
tetrahedron <- tetrahedron3d()
shade3d(tetrahedron, color = "red", alpha = 0.3)
vs <- tetrahedron$vb[1L:3L, ]
sims <- runif_in_tetrahedron(100, vs[, 1], vs[, 2], vs[, 3], vs[, 4])
points3d(sims)
```

**runif\_on\_spherePatch** *Uniform sampling on a spherical patch*

## Description

Uniform sampling on a spherical patch (in dimension 3).

## Usage

```
runif_on_spherePatch(n, r = 1, phi1, phi2, theta1, theta2)
```

## Arguments

|                |   |
|----------------|---|
| n              | number of simulations                         |
| r              | radius  |
| phi1, phi2     | numbers defining the latitudinal angle range  |
| theta1, theta2 | numbers defining the longitudinal angle range |

## Details

A sphere patch is the part of the sphere whose polar angles theta and phi satisfy  $0 \leq \text{theta1} \leq \text{theta} \leq \text{theta2} \leq 2\pi$  and  $0 \leq \text{phi1} \leq \text{phi} \leq \text{phi2} \leq \pi$ .

## Value

The simulations in a n times 3 matrix.

## See Also

[runif\\_on\\_stri](#) for sampling on a spherical triangle.

## Examples

```
# sampling on the first orthant:
sims <-
  runif_on_spherePatch(100, phi1 = 0, phi2 = pi/2, theta1 = 0, theta2 = pi/2)
## Not run:
library(rgl)
spheres3d(0, 0, 0, color = "red", alpha = 0.5)
points3d(sims)
## End(Not run)
```

`runif_on_sphericalCap` *Uniform sampling on a spherical cap*

### Description

Uniform sampling on a spherical cap (in dimension 3).

### Usage

```
runif_on_sphericalCap(n, r = 1, h)
```

### Arguments

|   |                       |
|---|-----------------------|
| n | number of simulations |
| r | radius of the sphere  |
| h | height of the cap     |

### Value

The simulations in a n times 3 matrix.

### Examples

```
sims <- runif_on_sphericalCap(500, r = 2, h = 1)
## Not run:
library(rgl)
spheres3d(0, 0, 0, radius = 2, color = "red", alpha = 0.5)
points3d(sims)
## End(Not run)
```

`runif_on_stri` *Uniform sampling on a spherical triangle*

### Description

Uniform sampling on a spherical triangle (in dimension 3).

### Usage

```
runif_on_stri(n, r = 1, v1, v2, v3)
```

### Arguments

|            |                       |
|------------|-----------------------|
| n          | number of simulations |
| r          | radius                |
| v1, v2, v3 | vertices              |

**Value**

The simulations in a n times 3 matrix.

**Examples**

```
# sampling on the first orthant:
sims <- runif_on_stri(100, v1 = c(1, 0, 0), v2 = c(0, 1, 0), v3 = c(0, 0, 1))
## Not run:
library(rgl)
spheres3d(0, 0, 0, color = "red", alpha = 0.5)
points3d(sims)
## End(Not run)
```

---

**runif\_sphere**

*Uniform sampling on/in sphere*

---

**Description**

Uniform sampling on a sphere or in a sphere, in arbitrary dimension.

**Usage**

```
runif_on_sphere(n, d, r = 1)
runif_in_sphere(n, d, r = 1)
```

**Arguments**

|   |                        |
|---|------------------------|
| n | number of simulations  |
| d | dimension of the space |
| r | radius of the sphere   |

**Value**

The simulations in a n times d matrix.

**Examples**

```
sims <- runif_on_sphere(20, d = 2)
plot(sims, xlim = c(-1, 1), ylim = c(-1, 1), asp = 1, pch = 19)
sims <- runif_in_sphere(100, d = 2)
plot(sims, xlim = c(-1, 1), ylim = c(-1, 1), asp = 1, pch = 19)
```

---

|                          |                                     |
|--------------------------|-------------------------------------|
| <code>runif_torus</code> | <i>Uniform sampling on/in torus</i> |
|--------------------------|-------------------------------------|

---

## Description

Uniform sampling on or in a torus (dimension 3).

## Usage

```
runif_on_torus(n, R, r)
runif_in_torus(n, R, r)
```

## Arguments

|   |                       |
|---|-----------------------|
| n | number of simulations |
| R | major radius          |
| r | minor radius          |

## Value

The simulations in a n times 3 matrix.

## Examples

```
R <- 3; r <- 2
sims_on <- runif_on_torus(50, R = R, r = r)
sims_in <- runif_in_torus(50, R = R, r = r)
library(misc3d)
fx <- function(u,v) (R+r*cos(u)) * cos(v)
fy <- function(u,v) (R+r*cos(u)) * sin(v)
fz <- function(u,v) r*sin(u)
parametric3d(
  fx, fy, fz, umin = 0, umax = 2*pi, vmin = 0, vmax = 2*pi, alpha = 0.3
)
library(rgl)
points3d(sims_on)
points3d(sims_in, color = "red")
```

**runif\_triangle**      *Uniform sampling on/in a triangle*

### Description

Uniform sampling on or in a triangle (dimension 2).

### Usage

```
runif_in_triangle(n, v1, v2, v3)
runif_on_triangle(n, v1, v2, v3)
```

### Arguments

|            |                          |
|------------|--------------------------|
| n          | number of simulations    |
| v1, v2, v3 | vertices of the triangle |

### Value

The simulations in a n times 2 matrix.

### Examples

```
sims <- runif_on_triangle(30, c(0,0), c(1,0), c(0,1))
plot(sims, xlim = c(0,1), ylim = c(0,1), pch = 19)
sims <- runif_in_triangle(100, c(0,0), c(1,0), c(0,1))
plot(sims, xlim = c(0,1), ylim = c(0,1), pch = 19)
```

**runif\_unitSimplex**      *Uniform sampling on/in a unit simplex*

### Description

Uniform sampling on or in a unit simplex (arbitrary dimension).

### Usage

```
runif_on_unitSimplex(n, d)
runif_in_unitSimplex(n, d)
```

### Arguments

|   |                        |
|---|------------------------|
| n | number of simulations  |
| d | dimension of the space |

**Value**

The simulations in a n times d matrix.

**See Also**

[runif\\_in\\_tetrahedron](#) for sampling in an arbitrary tetrahedron in dimension 3; [runif\\_in\\_simplex](#) for sampling in an arbitrary simplex.

**Examples**

```
library(rgl)
sims <- runif_on_unitSimplex(300, d = 3)
points3d(sims)
```

---

surface\_sphere      *Sphere surface*

---

**Description**

Surface of a sphere (arbitrary dimension).

**Usage**

```
surface_sphere(d, r = 1)
```

**Arguments**

|   |                        |
|---|------------------------|
| d | dimension of the space |
| r | radius of the sphere   |

**Value**

The surface of the sphere of radius r in the d-dimensional space.

**Examples**

```
r <- 2
surface_sphere(3, r)
4*pi*r^2
# perimeter of the unit circle:
surface_sphere(2)
```

---

**surface\_spherePatch**    *Sphere patch surface*

---

## Description

Surface of a sphere patch.

## Usage

```
surface_spherePatch(r, phi1, phi2, theta1, theta2)
```

## Arguments

r              radius

phi1, phi2     numbers defining the latitudinal angle range

theta1, theta2    numbers defining the longitudinal angle range

## Details

A sphere patch is the part of the sphere whose polar angles theta and phi satisfy  $0 \leq \theta \leq \theta_1 \leq \theta_2 \leq \pi$  and  $0 \leq \phi \leq \phi_1 \leq \phi_2 \leq \pi$ .

## Value

The surface of the sphere patch.

## See Also

[surface\\_stri](#) for the surface of a spherical triangle.

## Examples

```
# surface of the first orthant:  
surface_spherePatch(r=1, phi1=0, phi2=pi/2, theta1=0, theta2=pi/2)  
surface_stri(r=1, c(1,0,0), c(0,1,0), c(0,0,1))
```

---

surface\_sphericalCap    *Spherical cap surface*

---

**Description**

Surface of a spherical cap.

**Usage**

surface\_sphericalCap(r, h)

**Arguments**

|   |                      |
|---|----------------------|
| r | radius of the sphere |
| h | height of the cap    |

**Value**

The surface area of the spherical cap.

---

surface\_stri                  *Spherical triangle surface*

---

**Description**

Surface of a spherical triangle.

**Usage**

surface\_stri(r, v1, v2, v3)

**Arguments**

|            |          |
|------------|----------|
| r          | radius   |
| v1, v2, v3 | vertices |

**Value**

The surface of the spherical triangle of radius r with vertices v1, v2, v3.

**Examples**

```
# surface of the first orthant:  
surface_stri(r=1, c(1,0,0), c(0,1,0), c(0,0,1))
```

`surface_torus`*Torus surface***Description**

Surface of a torus.

**Usage**

```
surface_torus(R, r)
```

**Arguments**

|   |              |
|---|--------------|
| R | major radius |
| r | minor radius |

**Value**

The surface area of the torus.

`surface_triangle`*Triangle surface***Description**

Surface of a triangle.

**Usage**

```
surface_triangle(v1, v2, v3)
```

**Arguments**

|            |                          |
|------------|--------------------------|
| v1, v2, v3 | vertices of the triangle |
|------------|--------------------------|

**Value**

The surface of the triangle with vertices v1, v2, v3.

**Examples**

```
surface_triangle(c(0,0), c(0,1), c(1,0))
```

|                               |                         |
|-------------------------------|-------------------------|
| <code>volume_ellipsoid</code> | <i>Ellipsoid volume</i> |
|-------------------------------|-------------------------|

### Description

Volume of an ellipsoid (arbitrary dimension).

### Usage

```
volume_ellipsoid(A, r)
```

### Arguments

|   |   |
|---|---|
| A | symmetric positive-definite matrix defining the ellipsoid (see Details) |
| r | "radius" (see Details)  |

### Details

The (boundary of the) ellipsoid is the set of vectors  $x$  satisfying  $t(x) \%*\% A \%*\% x == r^2$ .

### Value

The volume of the ellipsoid.

### Examples

```
# dimension 2 (area), with diagonal matrix A
A <- diag(c(2,3))
r <- 2
volume_ellipsoid(A, r)
pi * r^2 / sqrt(A[1,1]*A[2,2])
```

|                                |                          |
|--------------------------------|--------------------------|
| <code>volume_hexahedron</code> | <i>Hexahedron volume</i> |
|--------------------------------|--------------------------|

### Description

Volume of a hexahedron.

### Usage

```
volume_hexahedron(hexahedron)
```

### Arguments

|            |   |
|------------|---|
| hexahedron | a 3 times 8 matrix whose columns are the eight vertices of the hexahedron; see <a href="#">makeHexahedron</a> |
|------------|---|

**Value**

The volume of the hexahedron.

**Examples**

```
library(uniformly)
# a cube with side 2 ####
hexahedron <- makeHexahedron(
  p0 = c(0, 0, 0),
  p1 = c(2, 0, 0),
  p2 = c(2, 2, 0),
  p3 = c(0, 2, 0),
  p4 = c(0, 2, 2),
  p5 = c(0, 0, 2),
  p6 = c(2, 0, 2),
  p7 = c(2, 2, 2)
)
volume_hexahedron(hexahedron) # should be 8
```

---

*volume\_pball*

*p-ball volume*

---

**Description**

Euclidean volume of a p-ball (arbitrary dimension).

**Usage**

```
volume_pball(d, p, r = 1)
```

**Arguments**

|   |   |
|---|---|
| d | dimension                                 |
| p | exponent in the p-norm, a positive number |
| r | radius of the ball                        |

**Value**

The volume of the p-ball with radius *r*.

**Examples**

```
volume_pball(d=4, p=2, r=2)
volume_sphere(d=4, r=2)
```

---

|                |                       |
|----------------|-----------------------|
| volume_simplex | <i>Simplex volume</i> |
|----------------|-----------------------|

---

**Description**

Volume of a simplex (arbitrary dimension).

**Usage**

```
volume_simplex(simplex)
```

**Arguments**

simplex        a (d+1) times d matrix giving the vertices of the simplex (rows)

**Value**

The volume of the simplex.

**Examples**

```
set.seed(666)
simplex <- matrix(rnorm(4*3), nrow=4, ncol=3)
volume_simplex(simplex)
volume_tetrahedron(simplex[1,], simplex[2,], simplex[3,], simplex[4,])
```

---

---

|               |                      |
|---------------|----------------------|
| volume_sphere | <i>Sphere volume</i> |
|---------------|----------------------|

---

**Description**

Volume of a sphere (arbitrary dimension).

**Usage**

```
volume_sphere(d, r = 1)
```

**Arguments**

d                dimension of the space  
r                radius of the sphere

**Value**

The volume of the sphere with radius  $r$  in the  $d$ -dimensional space.

**Examples**

```
r <- 2
volume_sphere(3, r)
4/3*pi*r^3
```

`volume_sphericalCap`    *Spherical cap volume*

**Description**

Volume of a spherical cap.

**Usage**

```
volume_sphericalCap(r, h)
```

**Arguments**

|                |                      |
|----------------|----------------------|
| <code>r</code> | radius of the sphere |
| <code>h</code> | height of the cap    |

**Value**

The volume of the spherical cap.

`volume_tetrahedron`    *Tetrahedron volume*

**Description**

Volume of a tetrahedron (dimension 3).

**Usage**

```
volume_tetrahedron(v1, v2, v3, v4)
```

**Arguments**

`v1, v2, v3, v4`    vertices of the tetrahedron

**Value**

The volume of the tetrahedron.

**See Also**

[volume\\_simplex](#) for the volume of a simplex in arbitrary dimension.

**Examples**

```
v1 <- c(0,0,0); v2 <- c(1,0,0); v3 <- c(0,1,0); v4 <- c(0,0,1)
volume_tetrahedron(v1, v2, v3, v4)
volume_unitSimplex(3)
```

---

**volume\_torus***Torus volume***Description**

Volume of a torus.

**Usage**

```
volume_torus(R, r)
```

**Arguments**

|   |              |
|---|--------------|
| R | major radius |
| r | minor radius |

**Value**

The volume of the torus.

---

**volume\_unitSimplex***Unit simplex volume*

---

**Description**

Volume of the unit simplex (arbitrary dimension).

**Usage**

```
volume_unitSimplex(d)
```

**Arguments**

|   |                        |
|---|------------------------|
| d | dimension of the space |
|---|------------------------|

**Value**

The volume of the unit simplex in the space of dimension d.

**See Also**

[volume\\_simplex](#) for the volume of an arbitrary simplex.

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